

# High-Occupancy-Toll (HOT) lanes: potential benefits and modeling challenges

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# Outline

- Case study (the “fast lane” to Tel-Aviv)
- Traveler choice models (LOGIT/VOT)
- Toll algorithms
- Basic stochastic model
- Departure time choice

# The “fast-lane to Tel-Aviv” package

- Dedicated bus lane
- High occupancy vehicles (HOV)
- Low occupancy vehicles pay toll (HOT)
- Auxiliary lane
- Carpool parking lot
- Free parking & downtown shuttle

Potential Pareto  $\Rightarrow$  Full Pareto

# Dates and costs

- Government decision: 1997
- Construction started: January 2009
- Opened to the public: January 7, 2011
  
- Construction cost: 300-500 MNIS (~150 M\$)
- BOT winning offer: -182 MNIS (~ -50 M\$)  
i.e. operator pays the government

# Toll system specifications

**Public statement:** one lane (of three) will carry half of the people and quarter of the vehicles.

**Contract:**

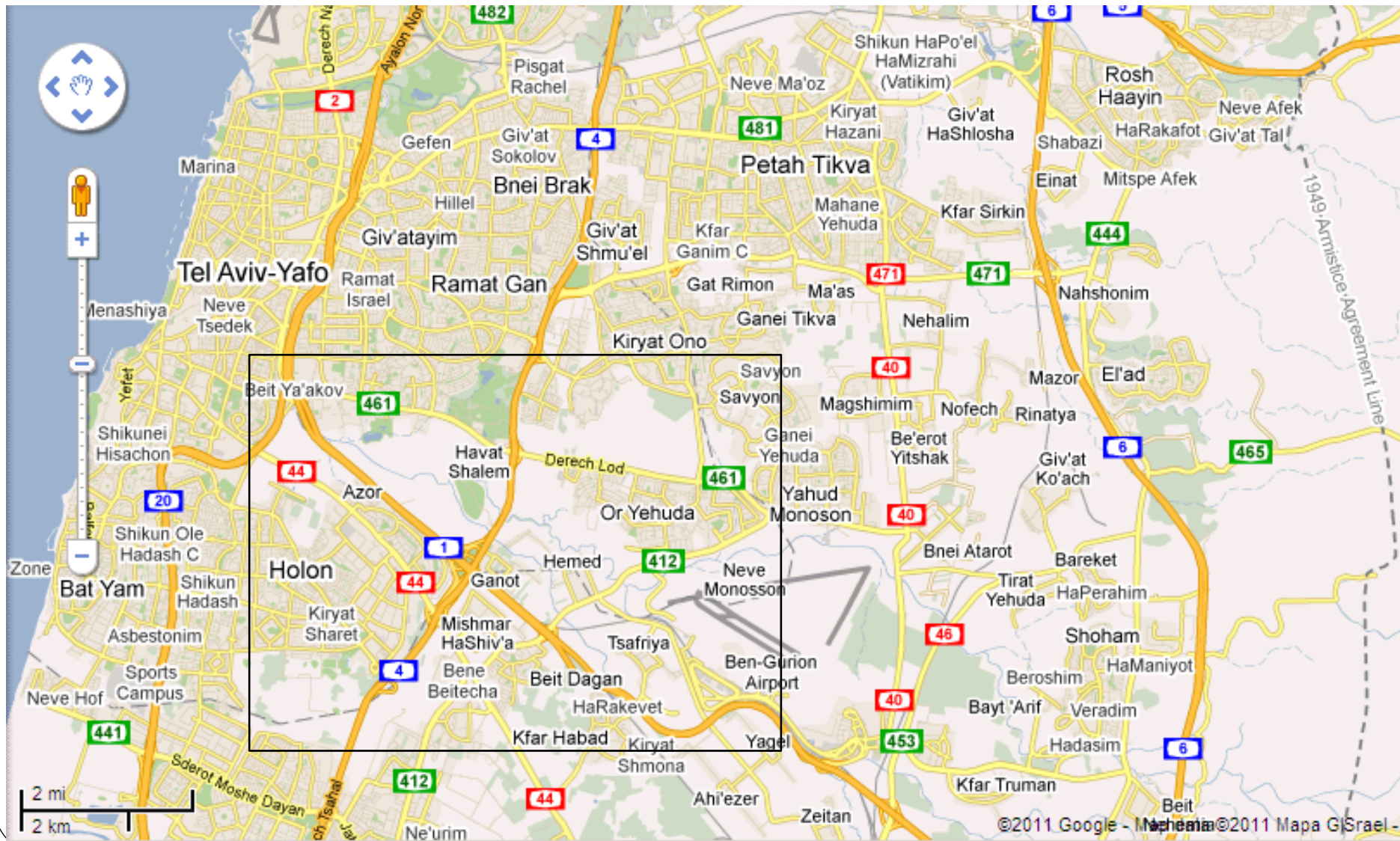
Speed above 70 km/h

Flow above 1600 vehicles per hour



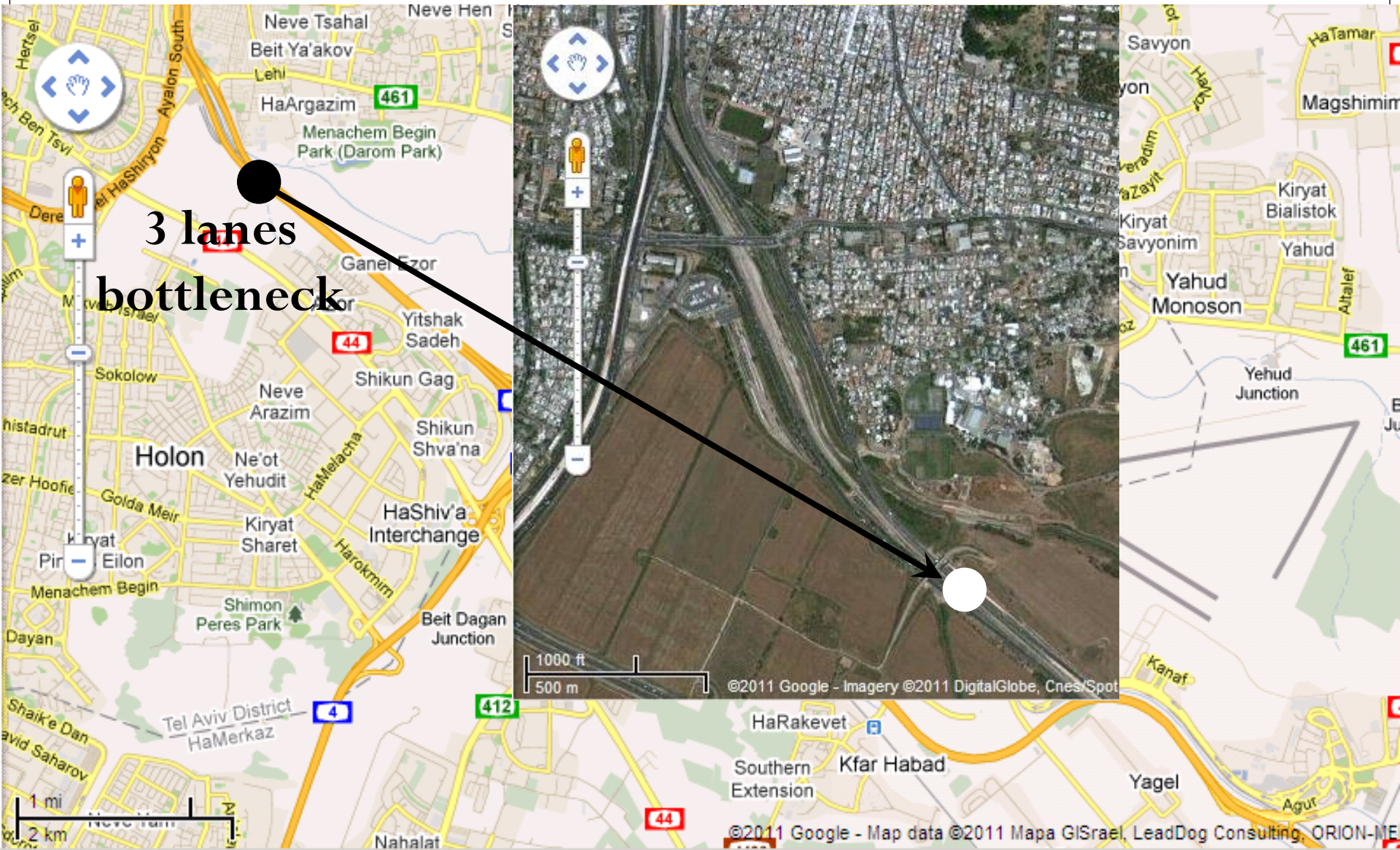
**Real-time responsive toll**

# The location



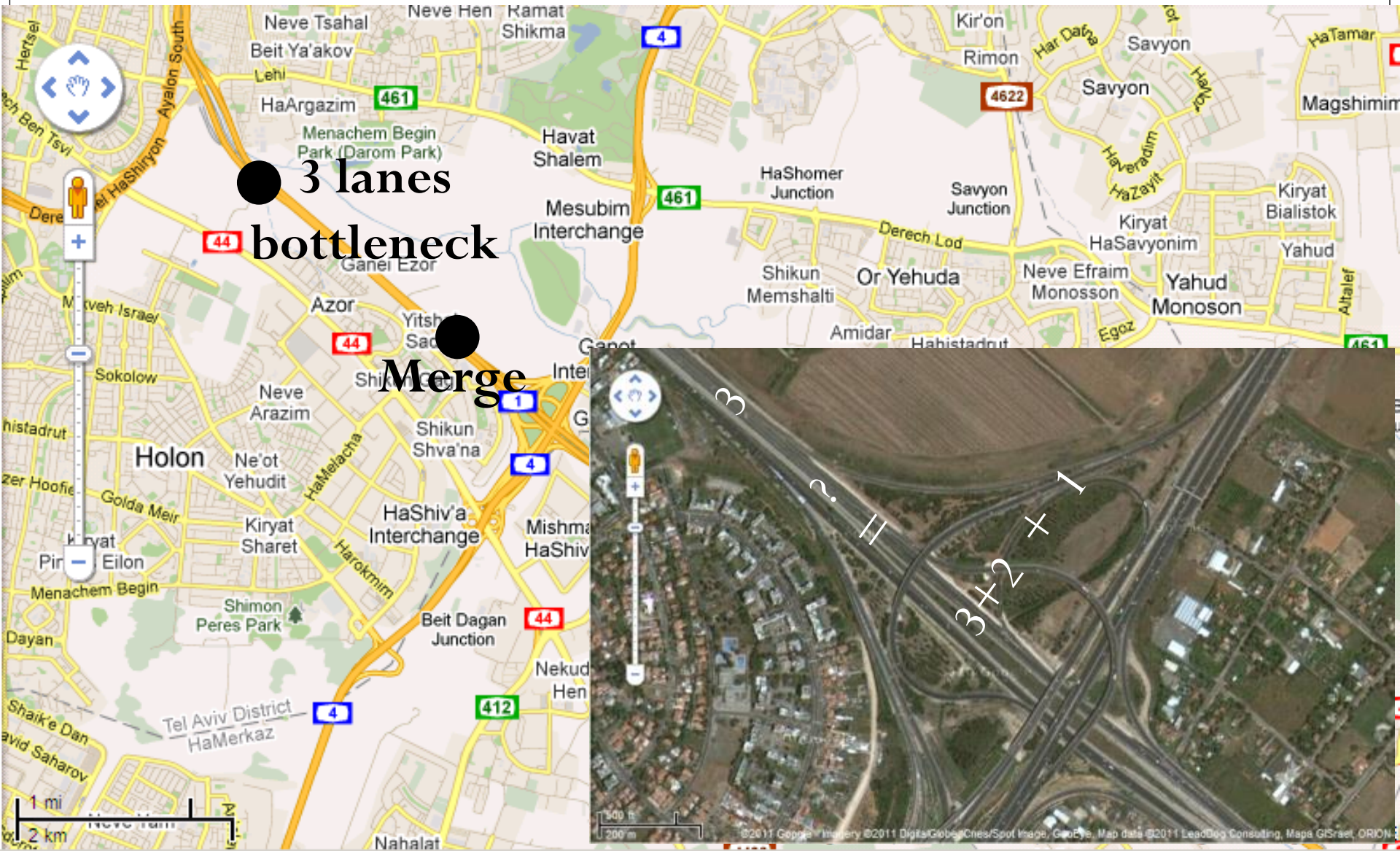


# The corridor





# The corridor





# The corridor





# The corridor: 13 km length



# Entrance and exit





# Entrance rules

- ❖ Public transport, mainly busses, 200/h
- ❖ HOV – 4 (or 3) persons or more, 100/h
- ❖ Responsive toll: 7-75 shekels (~2-20\$)
- ❖ E-toll (zero delay) for registered users

Manual HOV  
inspection and cash  
toll booths



# Access control at wide cross sections

2 lanes entrance



Typical cross section  
with rigid barrier



Traffic with rigid barrier



Emergency exit



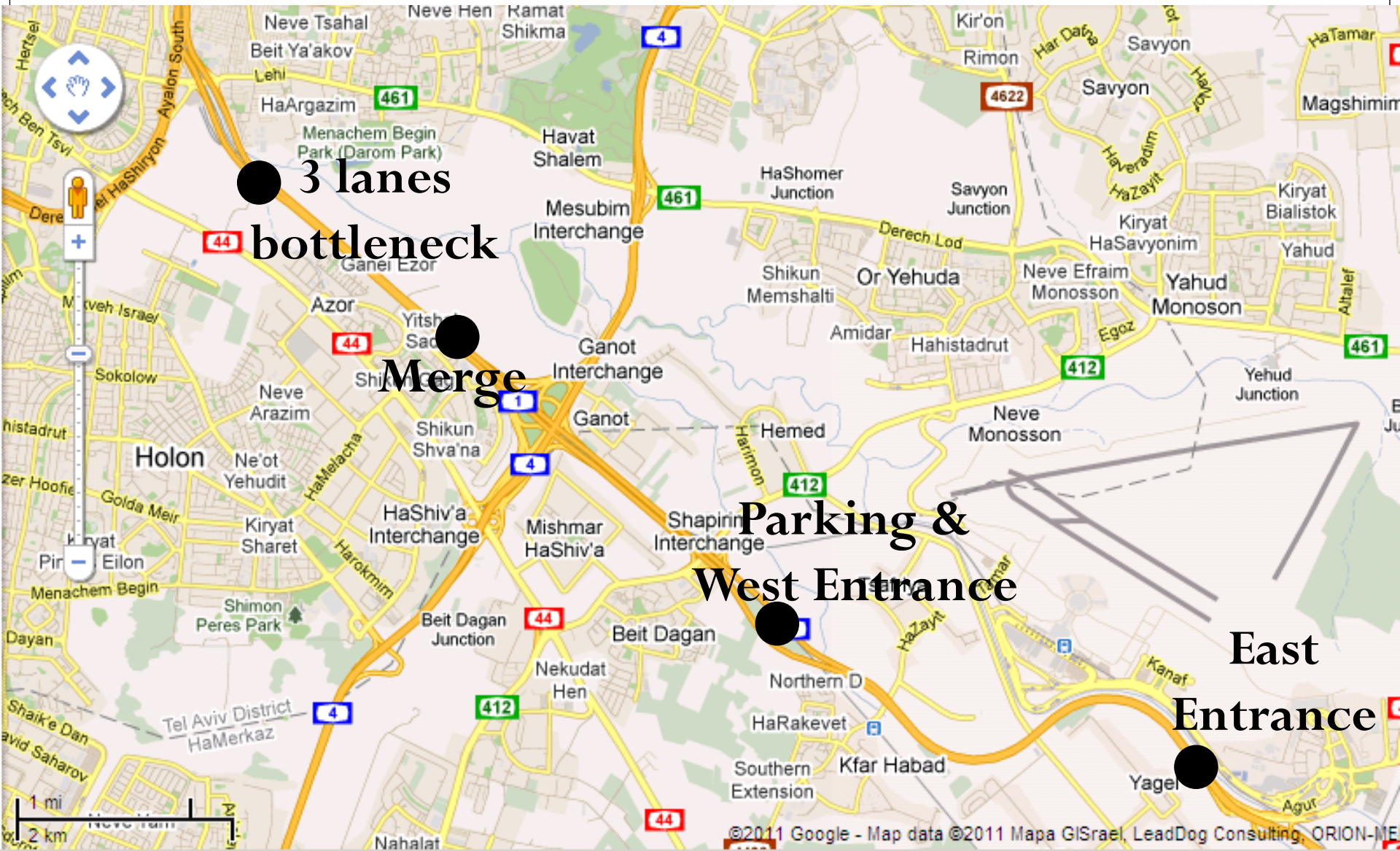
# “Soft” access control at the bottleneck



Pictures taken from the  
west bridge



# The parking lot





# The parking lot



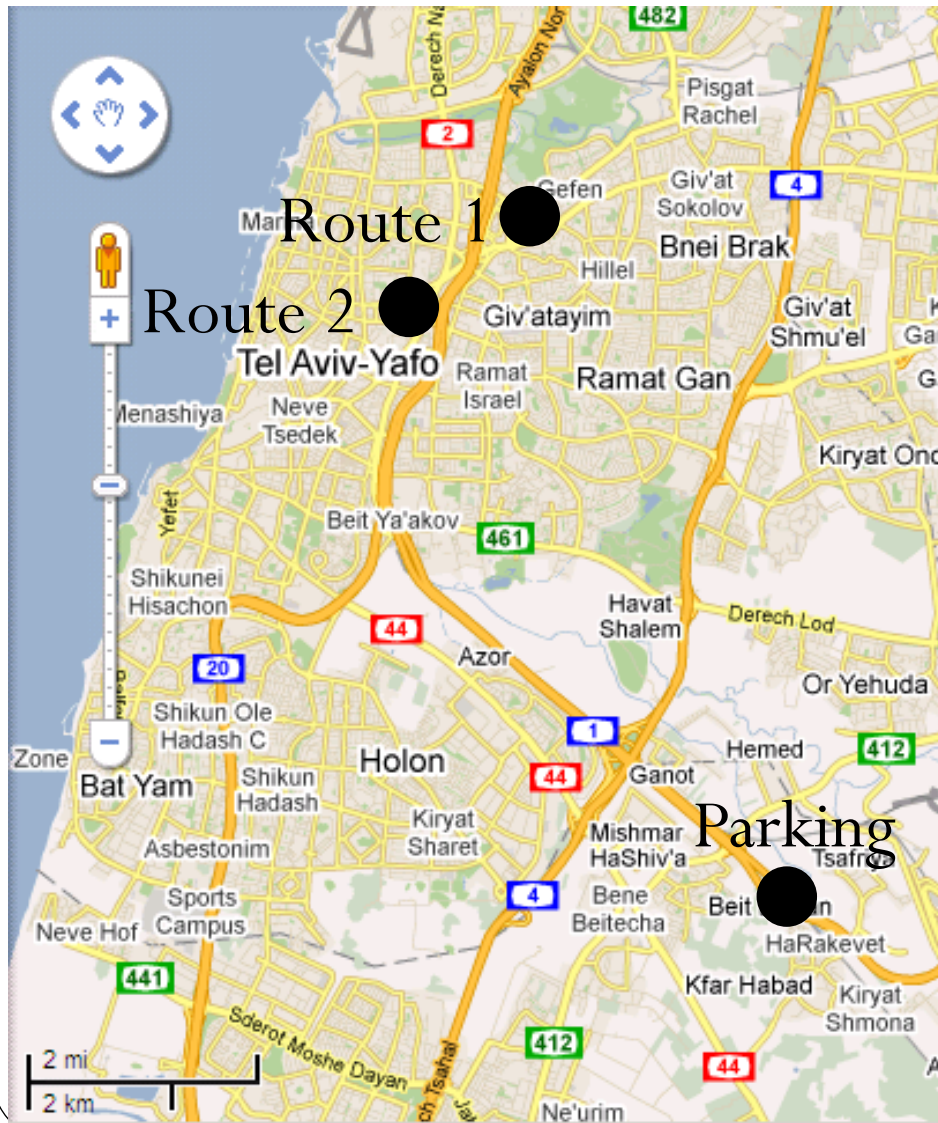
**2000 spots parking  
& West Entrance**

Photograph by Rodi Almog

1 mi  
2 km



# The downtown shuttle



Every 5 minutes  
6:30-9:30 & 15:30-19:00

Every 15 minutes  
6:00-23:00



# The downtown shuttle



Photographs by Rodi Almog

# The downtown shuttle





# The parking lot



In the first months, on a typical day **by 12:00AM** there were about **900 vehicles** in the parking lot



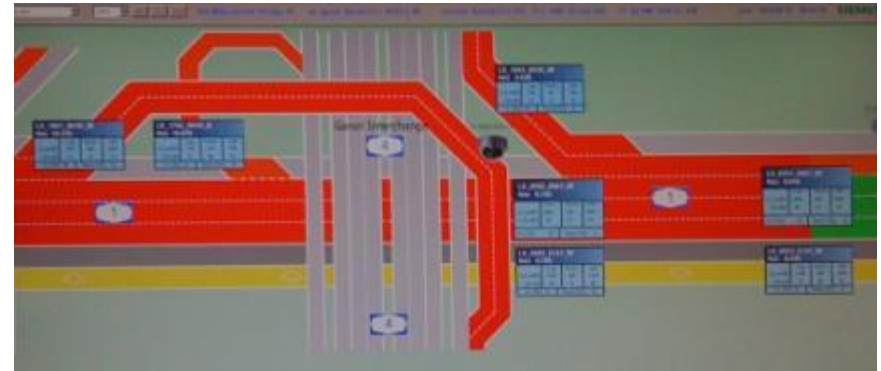
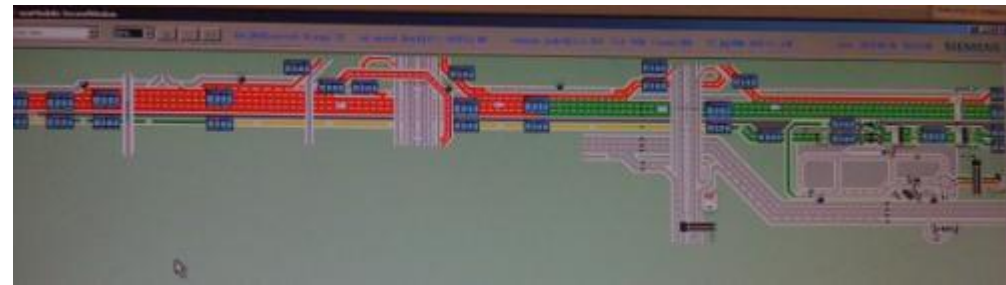


# Before





# After (Thursday, June 16, 2011)



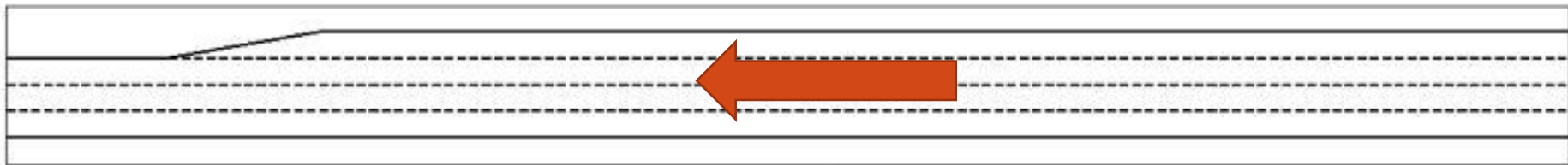
# Research Motivations

- The use of high-occupancy-toll (HOT) lanes increases continuously.
- A key challenge in HOT operation is how to set the tolls.
- Variability in travel demand creates additional complexity.
- A successful tolling scheme, whether fixed or time-varying, must be robust to changes in travel demand.

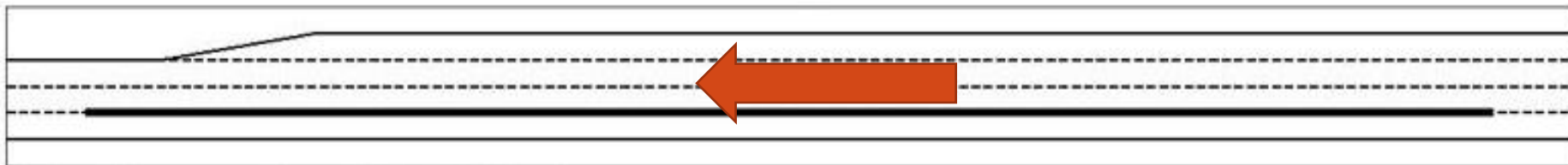


# Case Study Facility

- Freeway with two lane groups: general purpose (GP) lanes, and a managed lane.
- Managed lane scenarios: GP (Base), HOV or HOT.
- Bottlenecks exist at the downstream end (deterministic point queue model).



(a) Base case



(a) Bottleneck with Managed Lane

# Case Study Inputs

	Average Occ.	7:00- 8:00	8:00- 9:00	9:00- 10:00
LOV	1.2	6300	5100	3900
HOV	4	600	600	600
Transit	40	300	300	300
Total		<b>7200</b>	<b>6000</b>	<b>4800</b>

HOT capacity: 1800 vphpl; GP capacity: 2100 vphpl;  
Length: 10 km; Free flow speed: 100 km/h.



# Modeling Travelers' Lane Choice

LOGIT (conventional):

- Assumes choice probability is dictated by an i.i.d. random additive cost component per route, due to imperfect information for example.

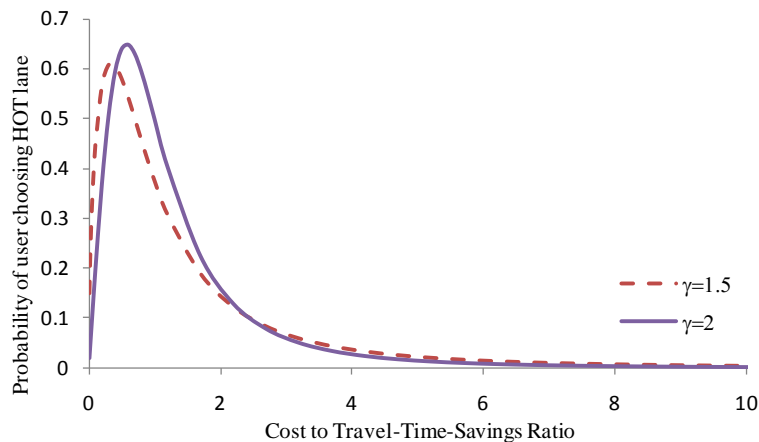
Value Of Time – VOT (proposed):

- Assumes primary variation in lane choice is due to VOT distribution (e.g. Burr).
- The proportion of travelers choosing the HOT lane is exactly the proportion of travelers whose VOT exceeds the current ratio of cost to time difference.

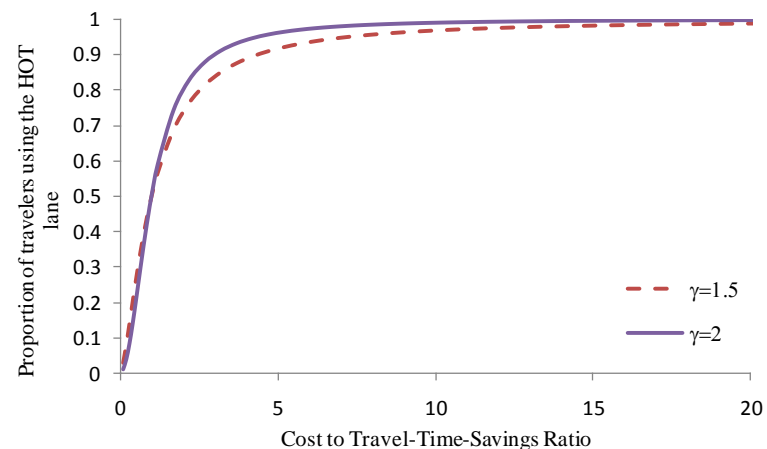
# VOT-Based Distribution

**Burr Distribution:** Used to model household income distribution in a population

$$P_v^{VOT}(\Delta\tau, c) = 1 - F_v(c/\Delta\tau) \quad \text{where} \quad F\left(\frac{c}{\Delta\tau}; \zeta, \gamma\right) = 1 - \frac{1}{\left[1 + \left(\frac{c}{\zeta \cdot \Delta\tau}\right)^\gamma\right]}$$



The *probability* of a traveler choosing the HOT lane

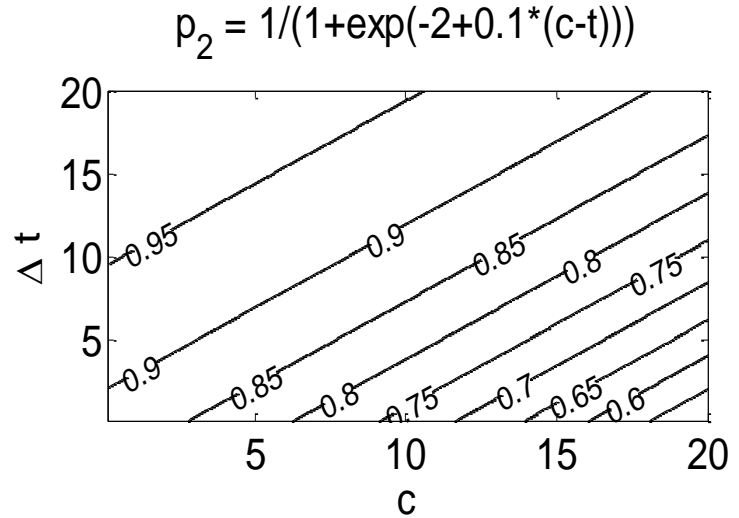
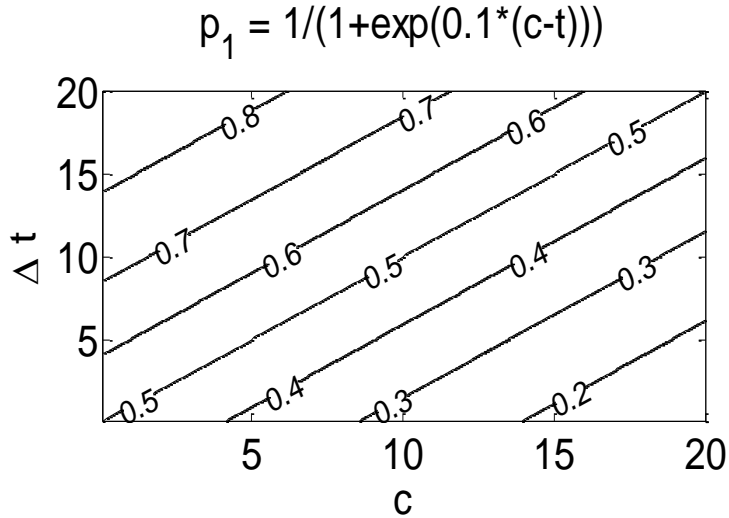


The *proportion* of travelers choosing the HOT lane, relative to the cost to travel-time-savings ratio

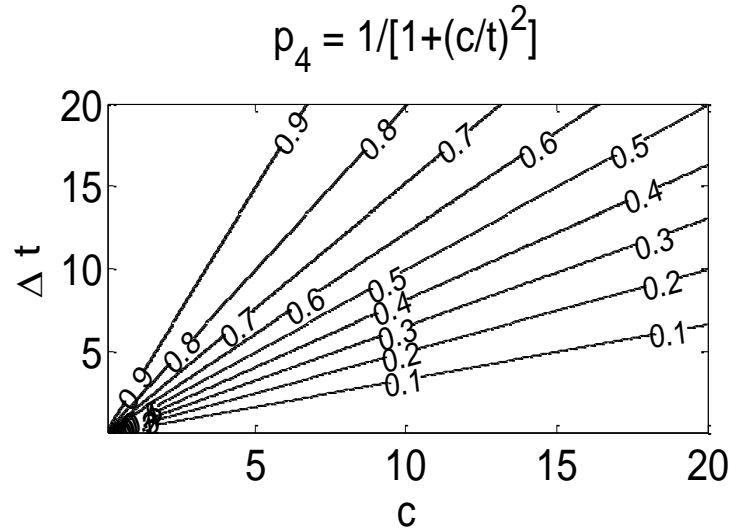
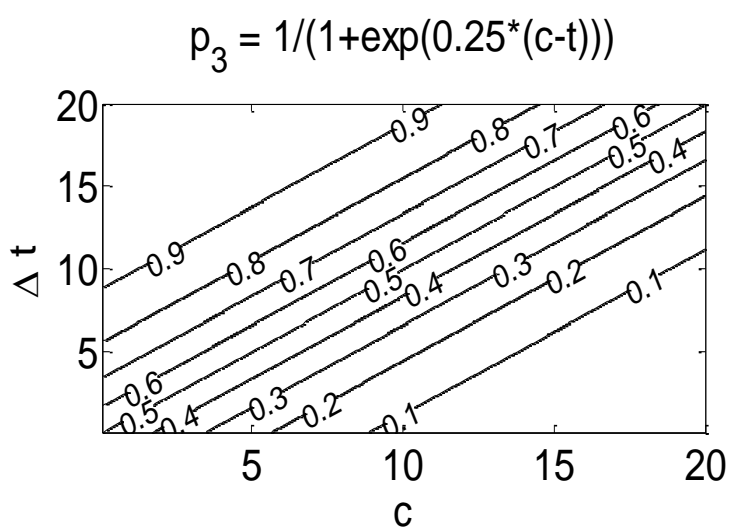


# Travelers Indifference Curves

LOGIT 1



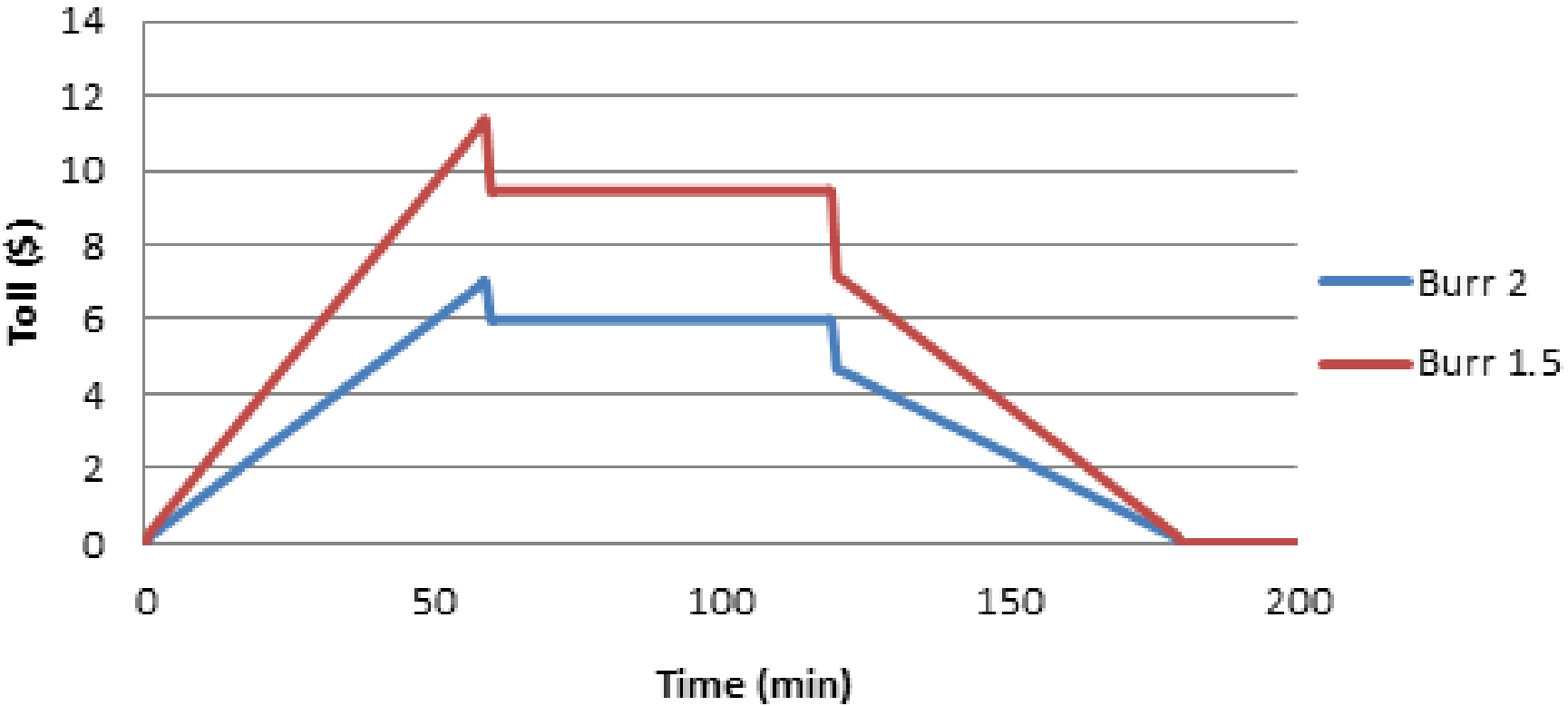
LOGIT 3



LOGIT 2

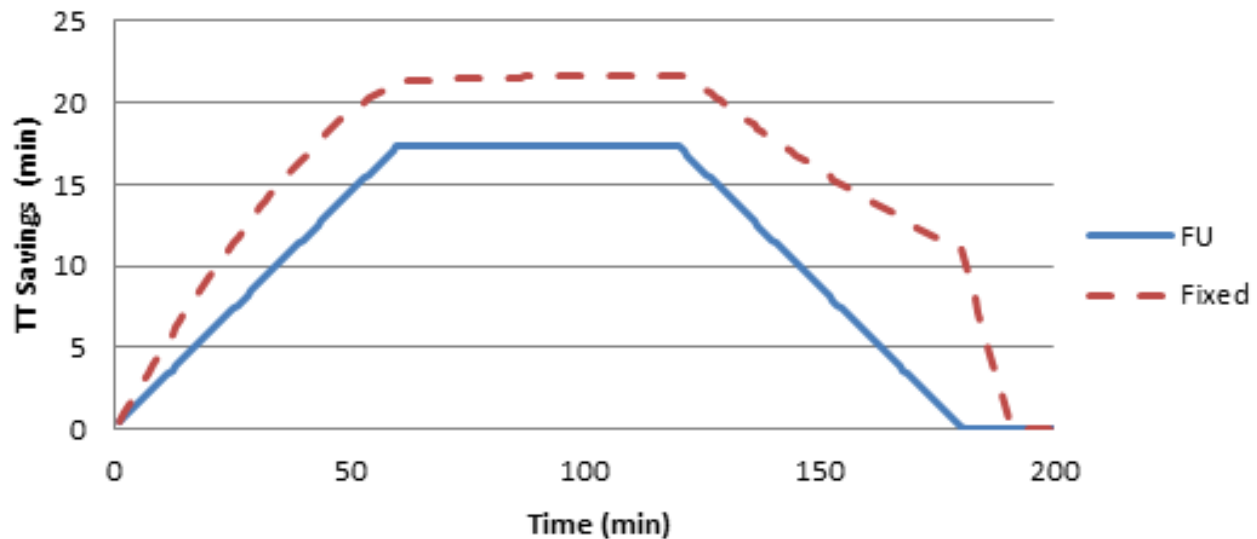
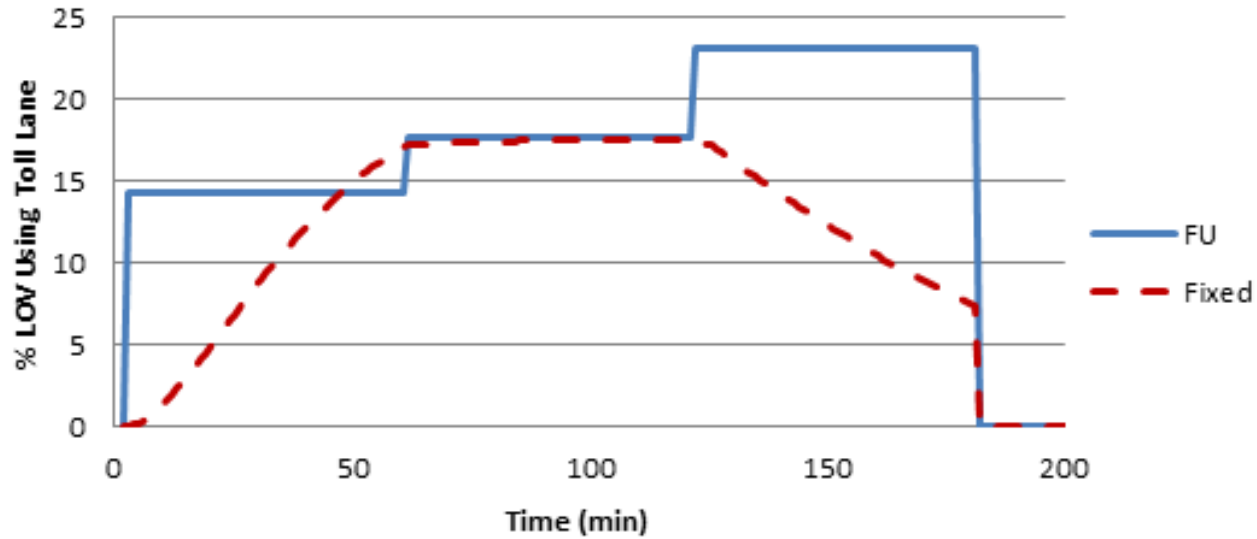
VOT

# Full Utilization (Optimal) Tolls

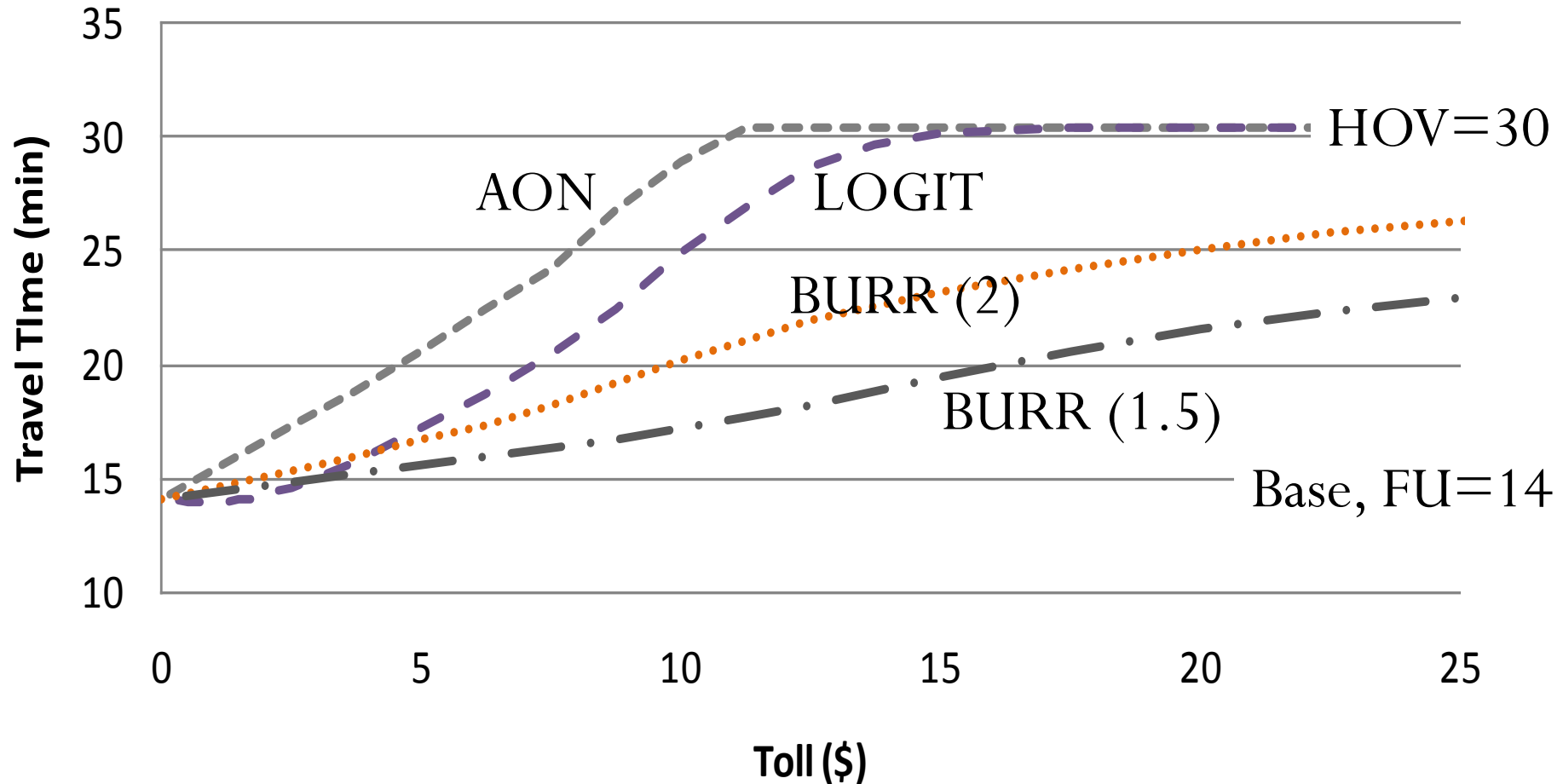




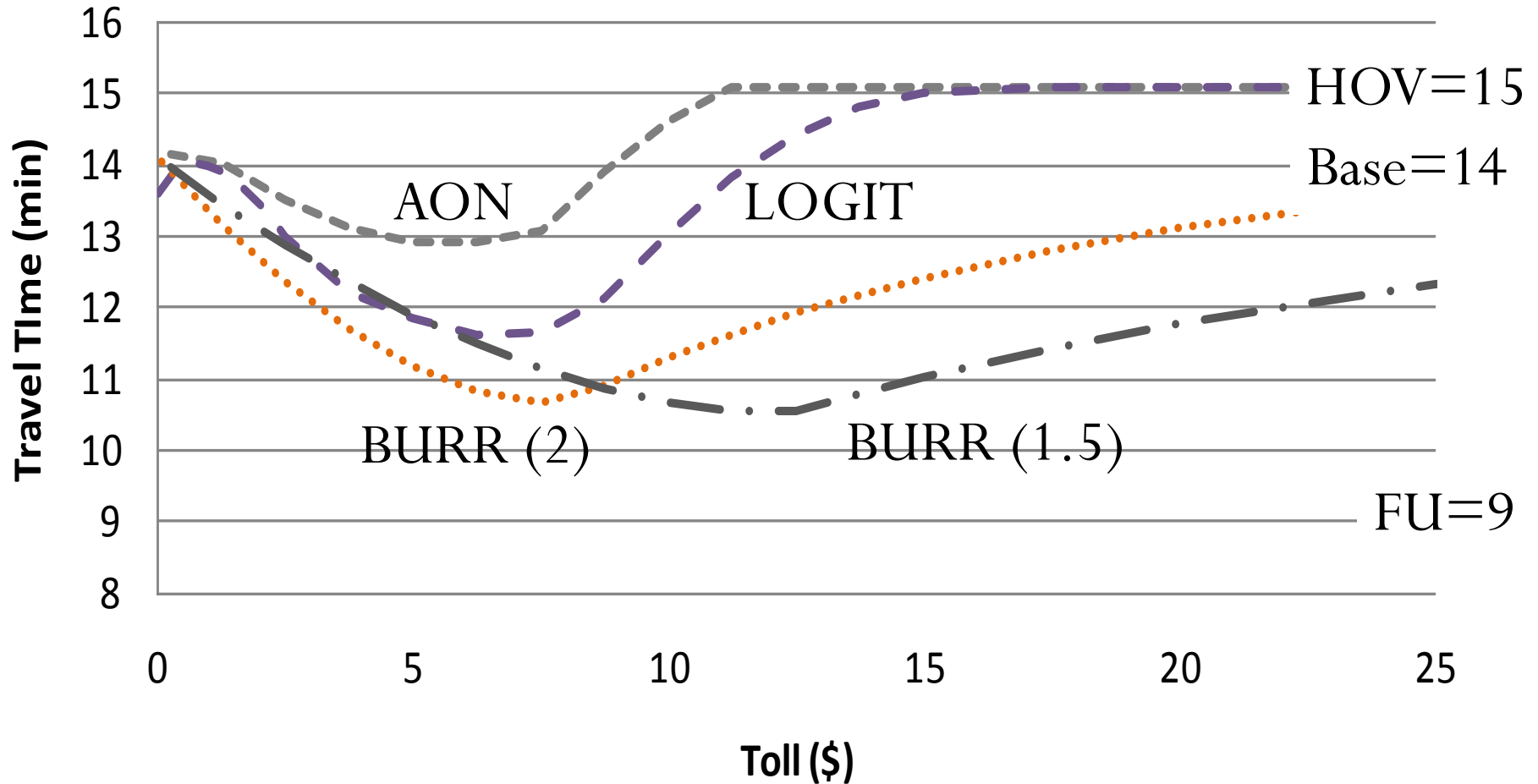
# HOT lane usage and time saving



# Average Vehicle Travel Time (AVTT)

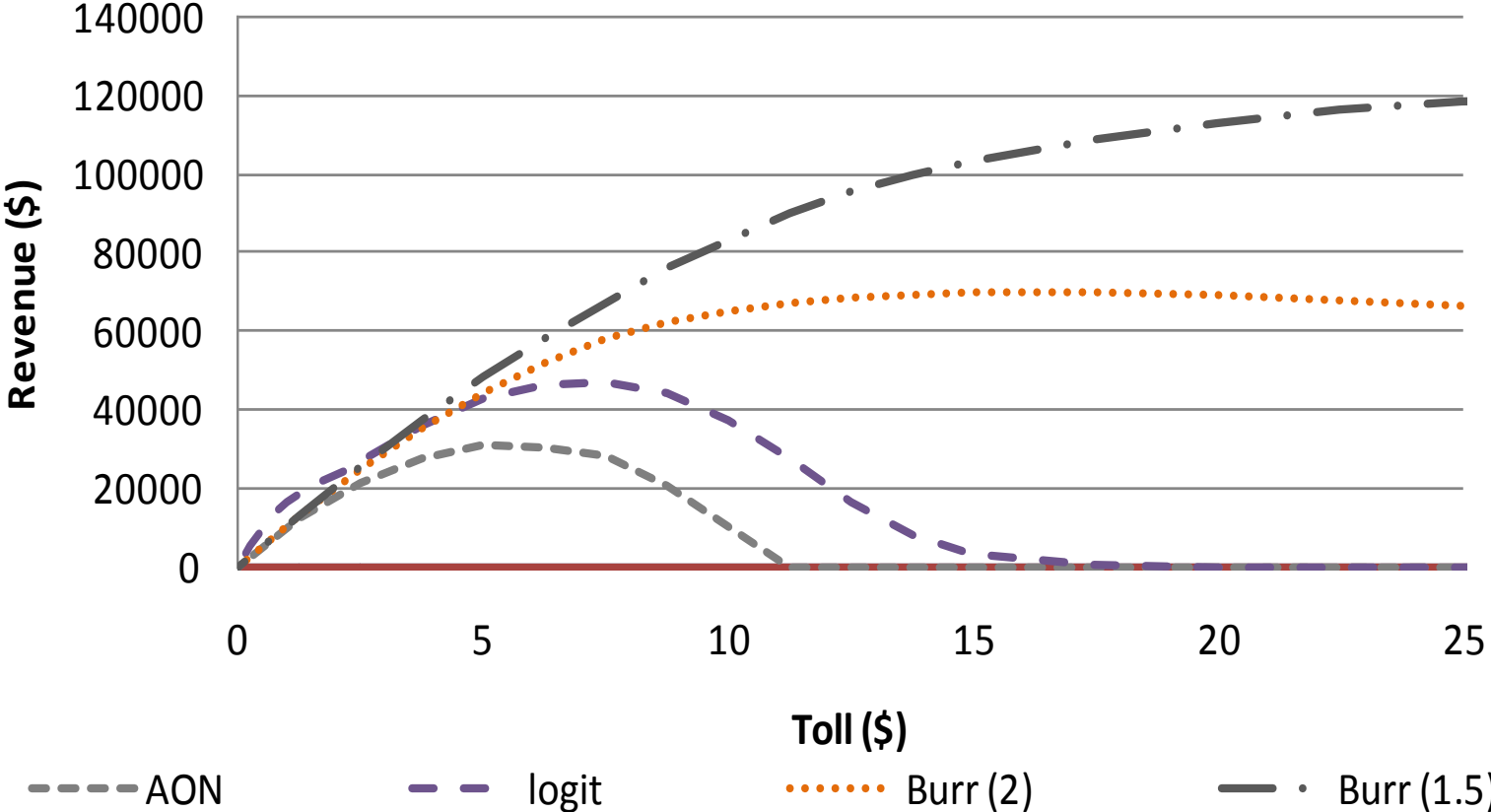


# Average Person Travel Time (APTT)





# Revenue



# Stochastic Context

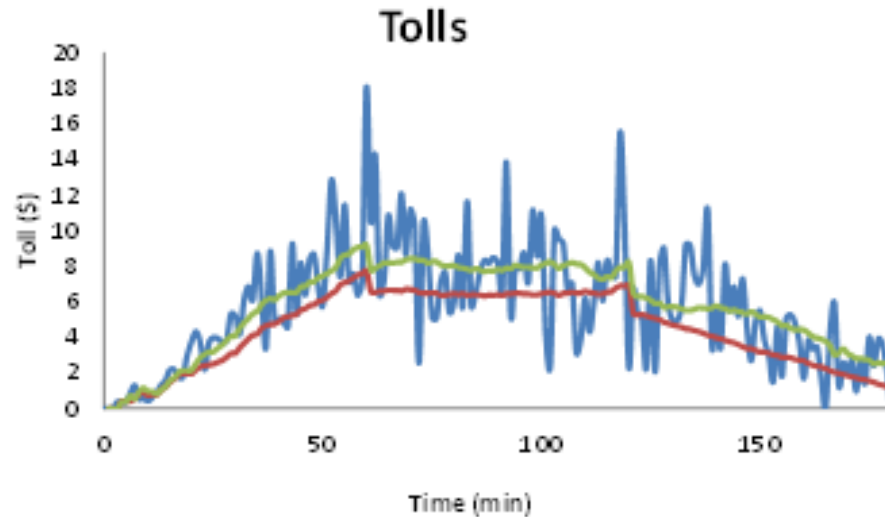
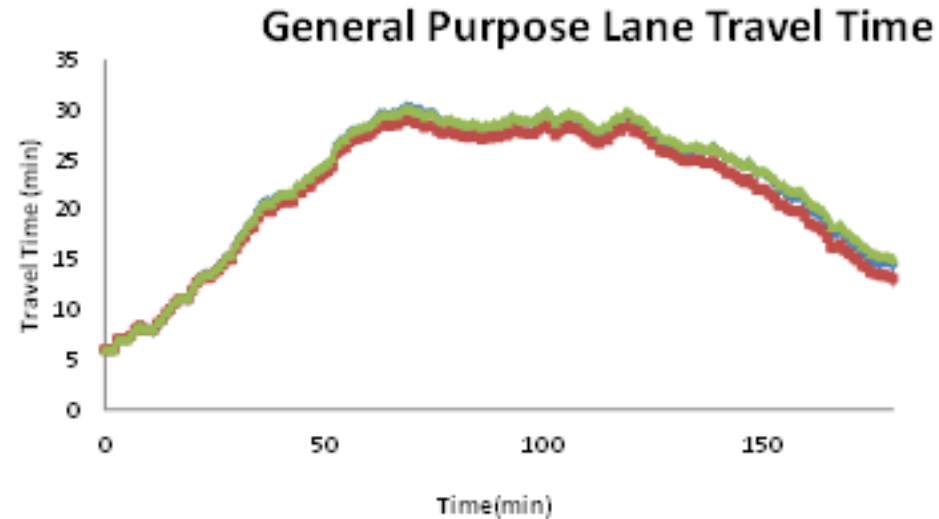
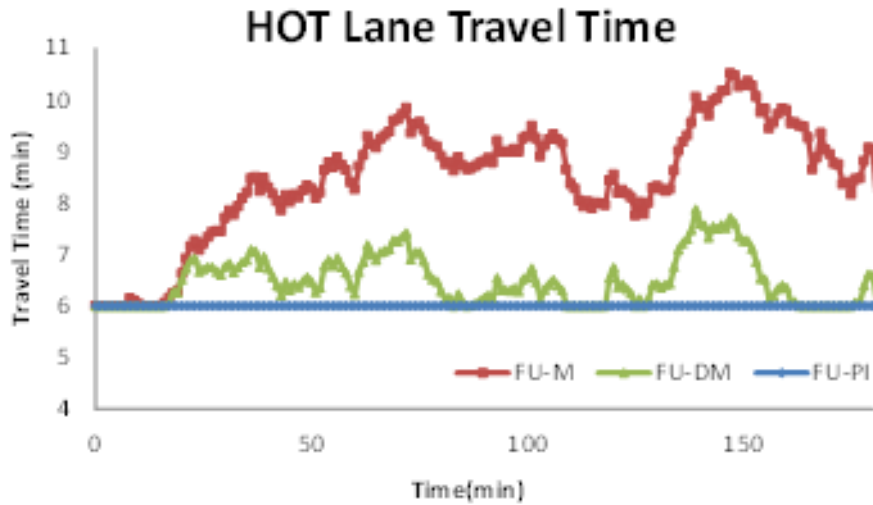
- Focus on demand uncertainty.
- Assume non-correlated day-to-day demand uncertainties.
- Implementation:
  - Arriving flow per minute is an independent random variable
  - Normally distributed.
  - The mean is determined by the time of day.
  - Scenario-specific Coefficient of Variation (CV).
- Assume a deterministic traffic flow model.

# Dynamic Tolling Schemes

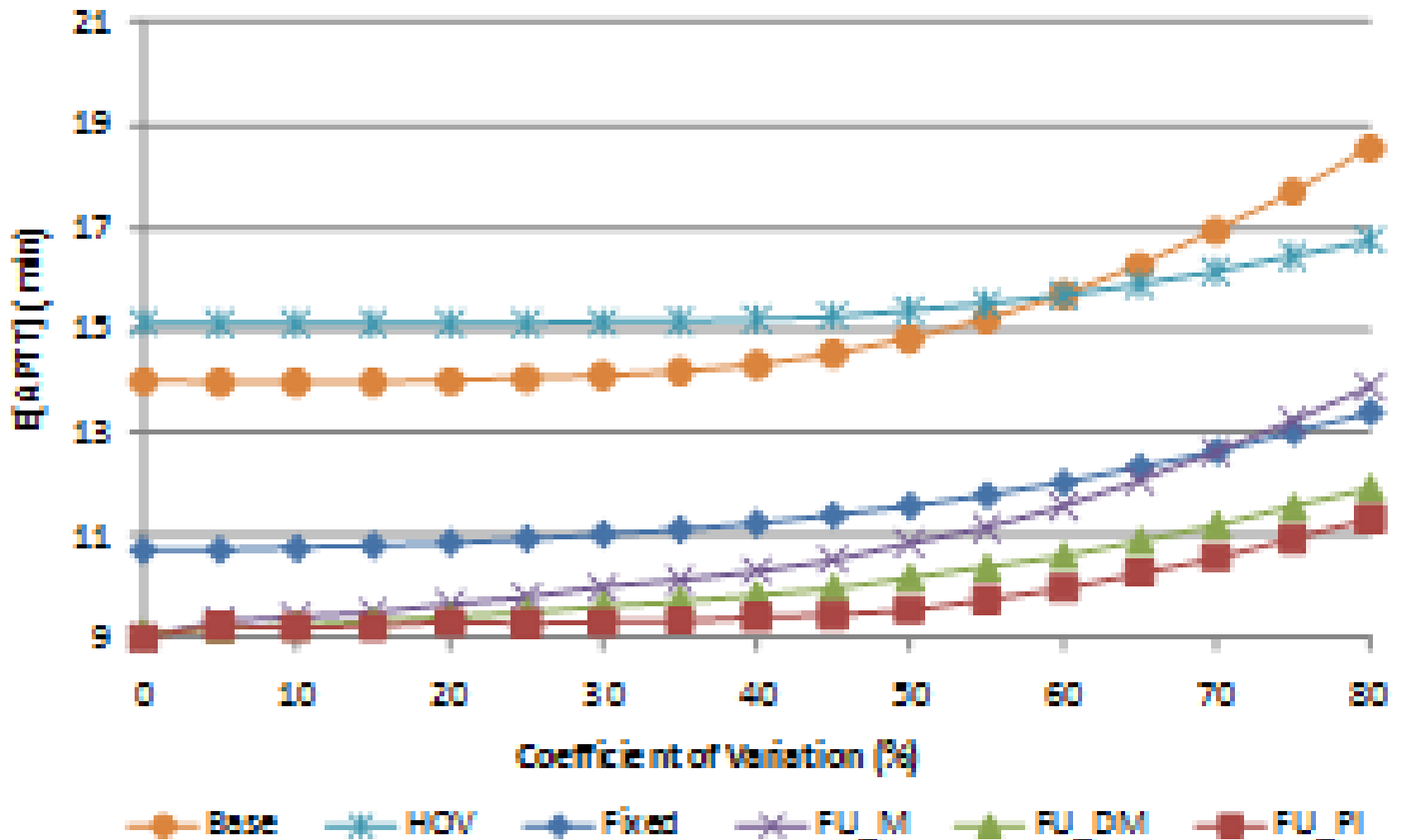
1. Fixed tolls (constant across time)
2. Pre-scheduled full-utilization tolls based on the mean demand values (**FU-M**).
3. Real-time density-modified full utilization toll (**FU-DM**). Tolls are set in ignorance of the current demand value, but modified based on the number of vehicles in the HOT lane.
4. Perfect information full-utilization tolls (**FU-PI**), where the demand realization is known to the operator before tolls are set.



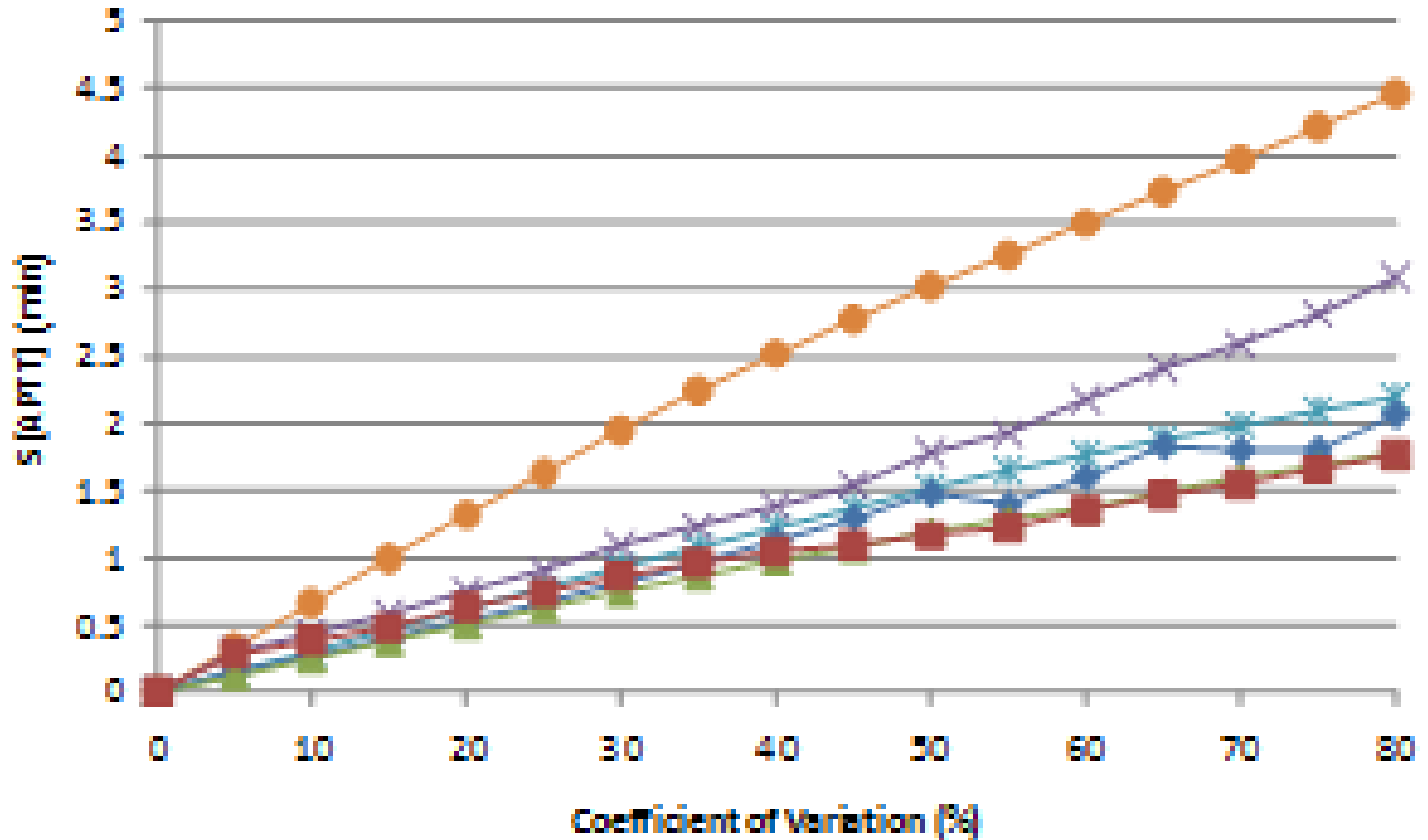
# Behavior (CV=0.3)



# Expected Average Person Travel Time



# Performance Measures (Stochastic)





# Departure Time Choice Model

- Travelers are either “strategic” or “captive”
- Captive drivers can only use the GP lanes. Their demand can be stochastic.
- Strategic drivers can choose between GP lanes and the HOT lane. Their demand is deterministic.
- Strategic drivers are divided into discrete “classes” by VOT and target arrival time.
- 1 min early arrival penalty = 0.5 min travel time
- 1 min late arrival penalty = 1 min travel time
- Two-stage decision process: departure time in view of expected generalized cost, lane by revealed conditions.

# Scenario

- Overall demand profile equivalent to case without departure time choice.
- Captive demand C.V is 0.4.
- 10 discrete VOT values, representing percentiles (counted from the top) according to Burr distribution.
- Target arrival time resolution is one minute.
- Full utilization toll schemes: Perfect Information (PI); Mean (factor=1.0); Density Modified (DM, factor=5).
- 300 MSA iterations of departure time choice.

# Main Metrics

Metric	All GP	Fixed (\$30)	Mean	DM	PI
AVTT	19.6	21.8	17.9	17.7	17.5
APTT	20.1	13.8	10.5	10.4	10.3
ANTD	24.1	22.7	18.3	18.1	17.9
Revenue ( $\times 10^3$ )	0	144	143	146	140

AVTT: Average vehicle travel time

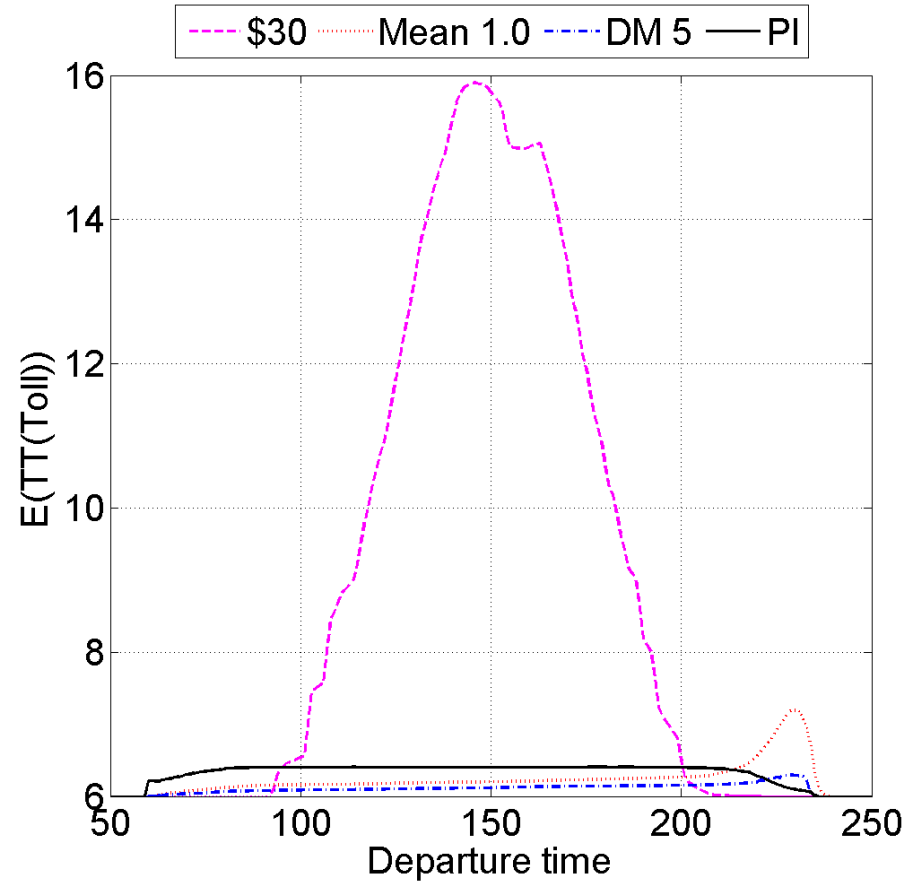
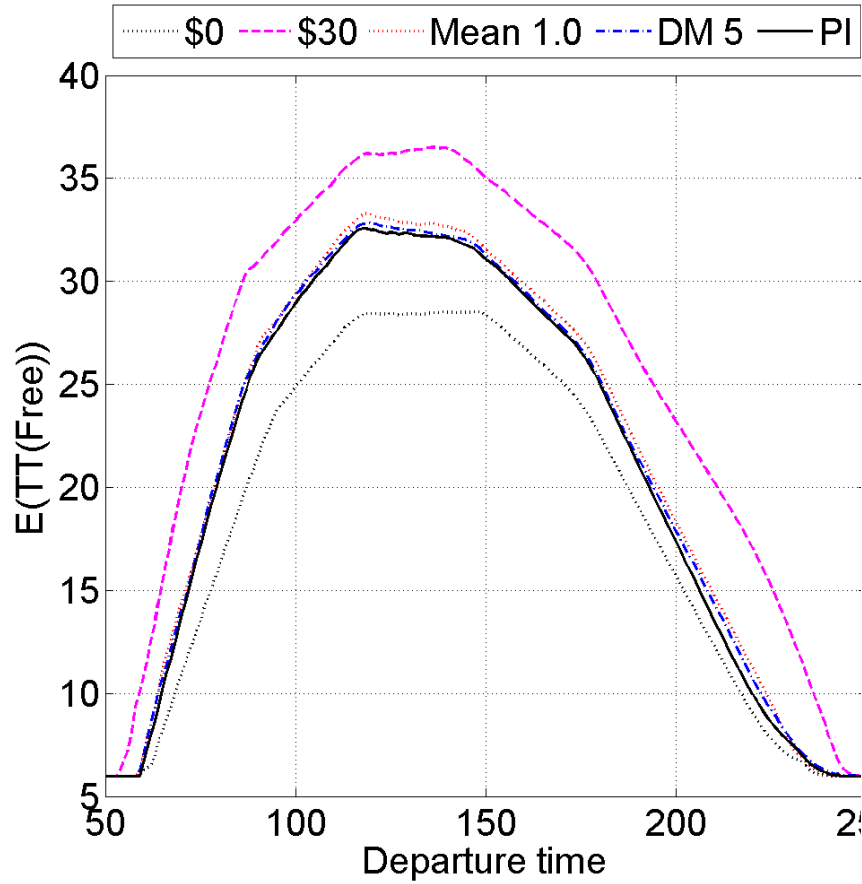
APTt: Average person travel time

ANTD: Average non-transfer disutility

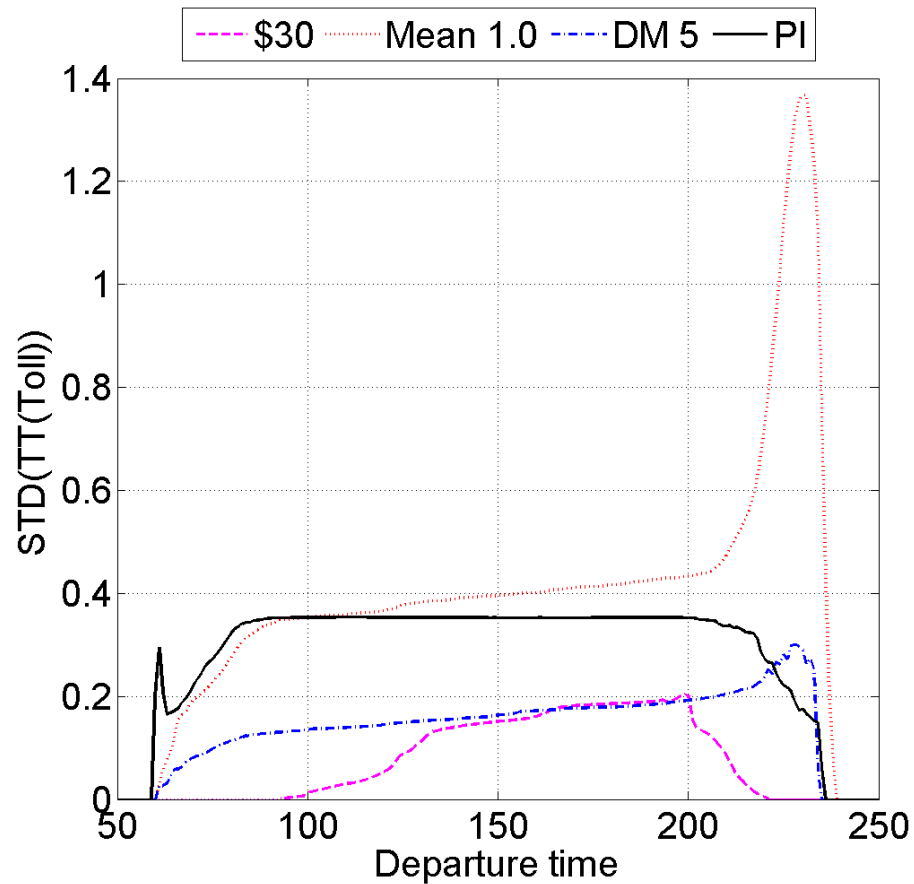
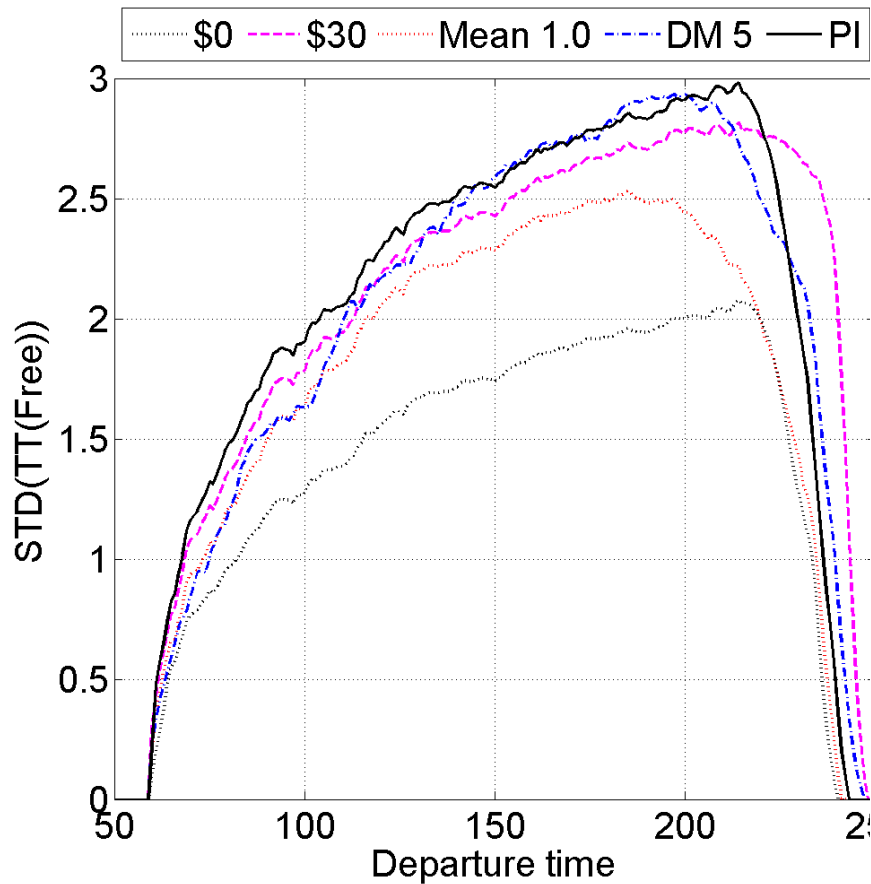
Calculations are based on 200 Samples



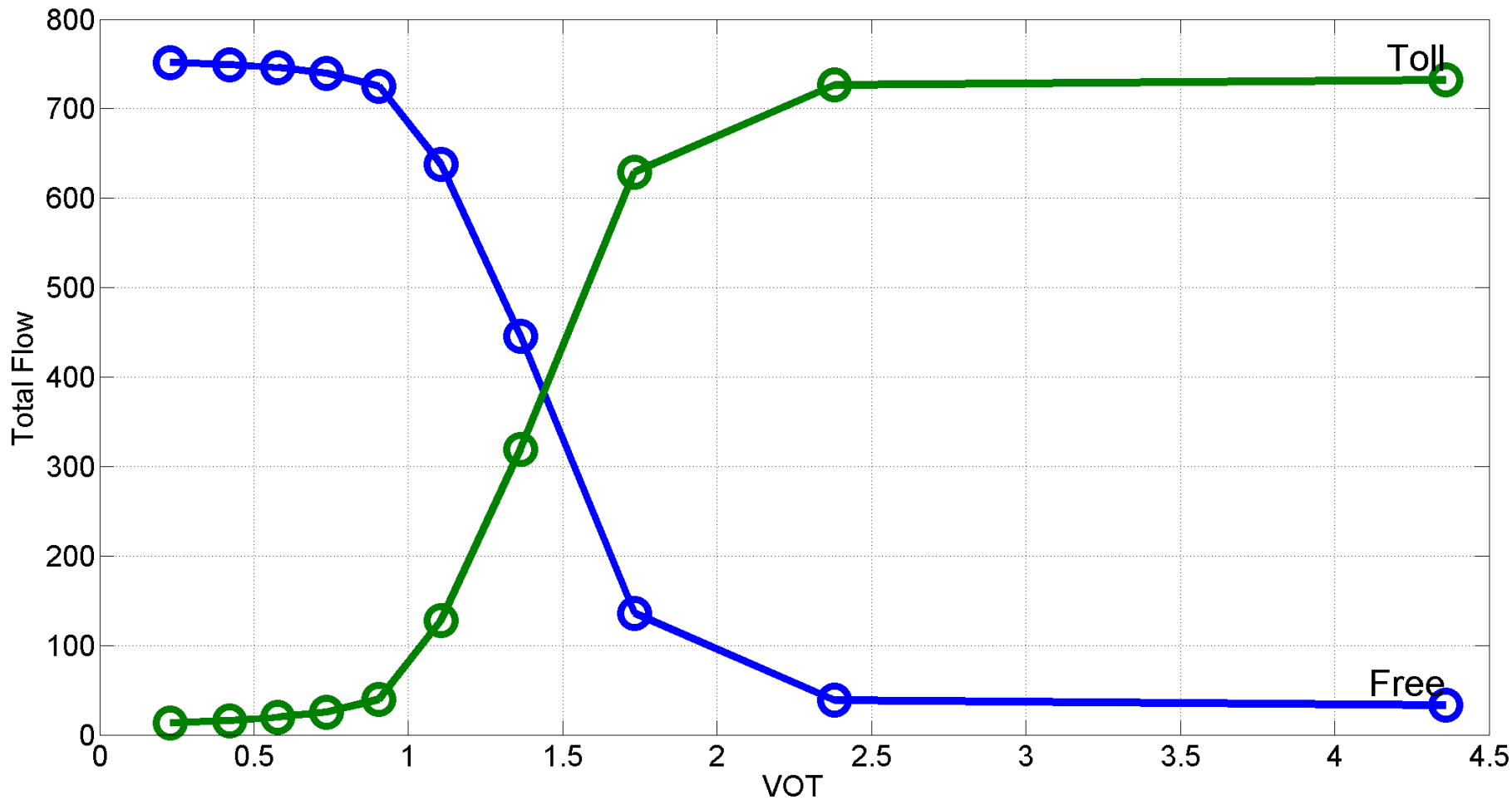
# Travel Time Profile



# Travel Time Variability



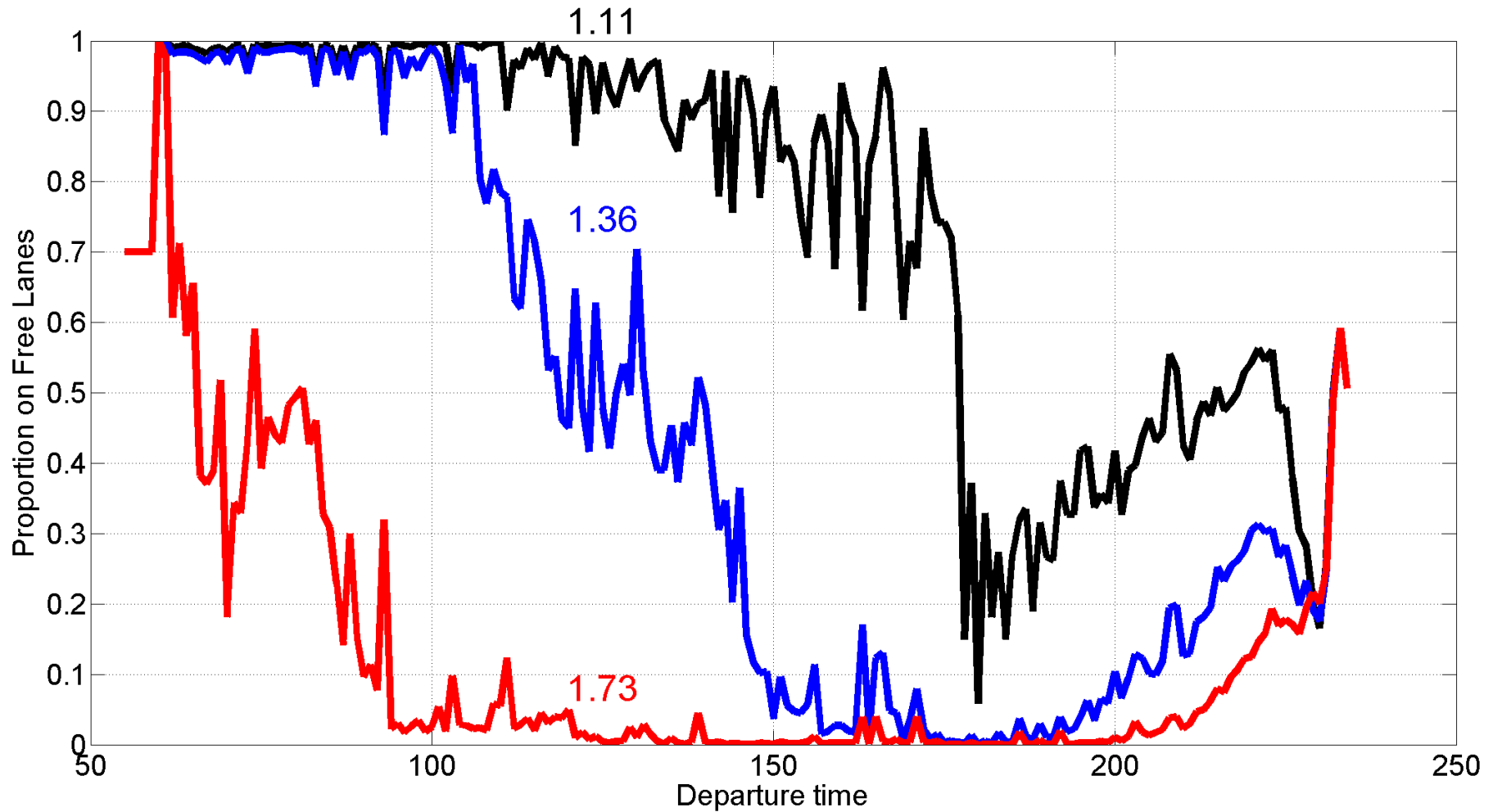
# Overall lane choice by VOT



Toll scheme is PI

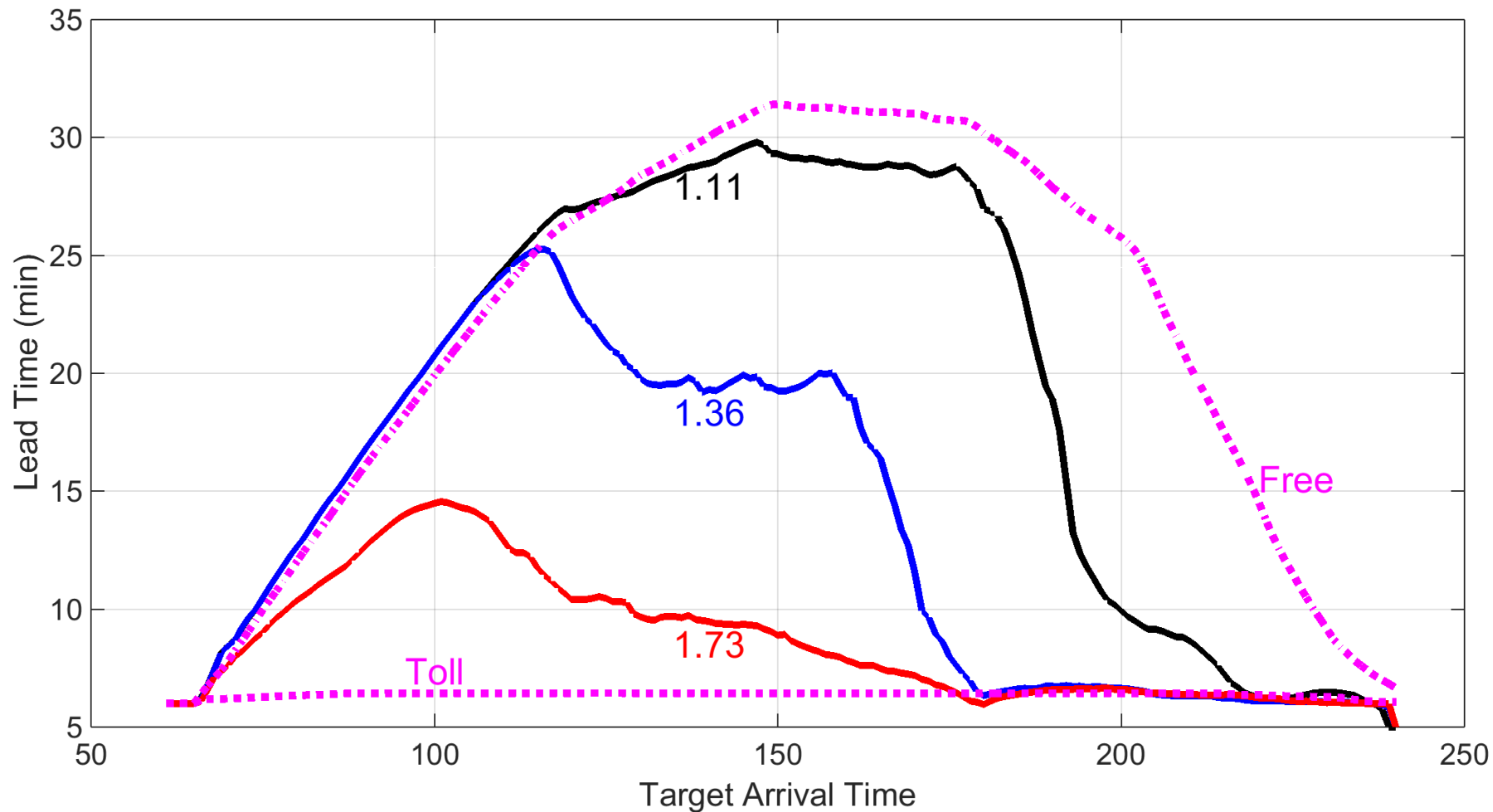


# Free lane usage by departure time and VOT



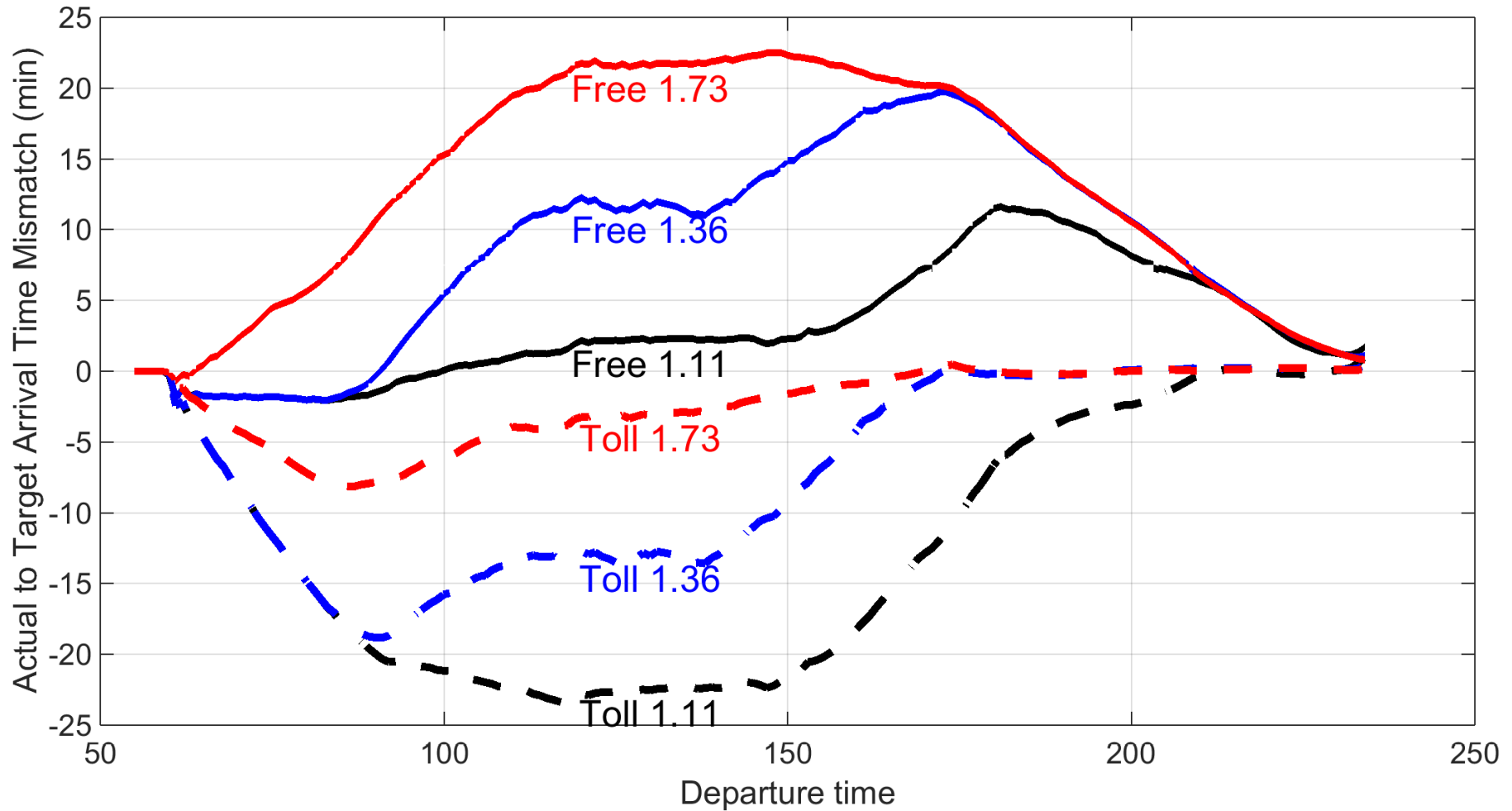
Toll scheme is PI

# Lead time by target arrival time and VOT



Toll scheme is PI

# Arrival time mismatch by lane and VOT



Toll scheme is PI



# Conclusions

- HOT lanes are a promising option for Pareto improvements of freeway corridors.
- A fixed toll value (24/7) may achieve a decent portion (2/3 in the examined case studies) from the theoretical potential benefit in terms of average passenger travel time.
- Pre-determined toll profile can handle reasonably well non-trivial uncorrelated demand uncertainties (up to  $CV=0.3$ ).
- Departure time choice reduces real time toll elasticity.