

Improved Local Freight Train Classification

Jens Maue¹

Joint Work with Peter Márton² and Marc Nunkesser¹

¹Institute of Theoretical Computer Science, ETH Zürich, Switzerland

²Department of Transportation Networks, University of Žilina, Slovakia

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Local Freight Train Classification



Local freight train

- ▶ multi-destination freight train
- ▶ cars ordered by destinations

Train classification

- ▶ special sorting problem
- ▶ classification yard

Outline

Train Classification in General

Classification Schedules

IP Formulation

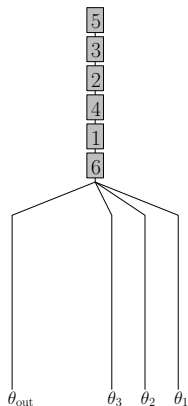
- Basic Model

- Real-World Instance

- Real-World Restrictions

Concluding Remarks

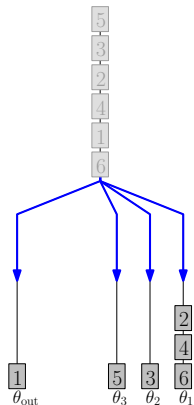
Example Classification Process



Train Classification

- ▶ **goal**: ascendingly **ordered train** on θ_{out}
- ▶ use available tracks θ_1 , θ_2 , and θ_3

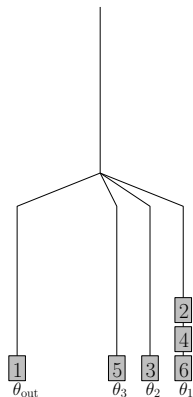
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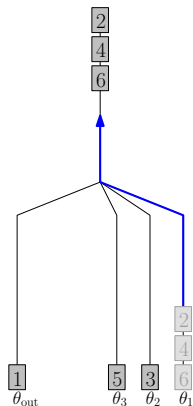
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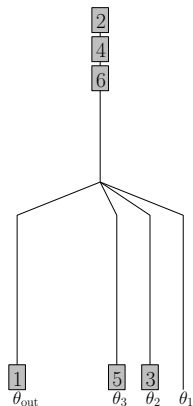
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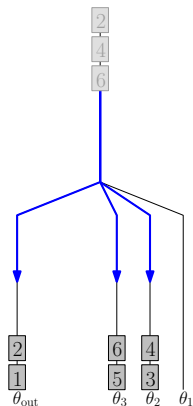
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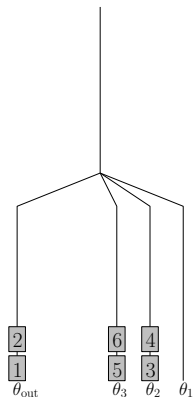
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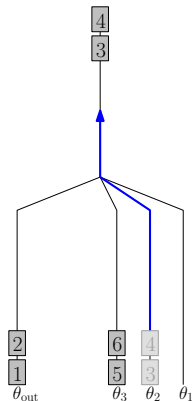
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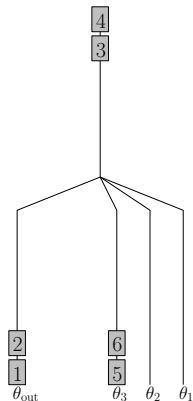
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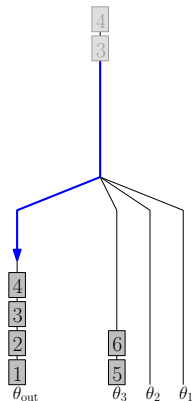
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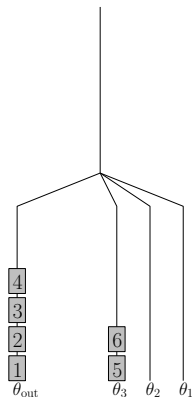
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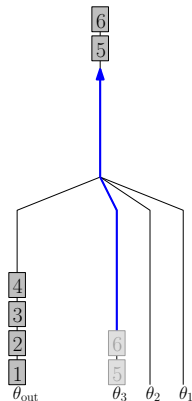
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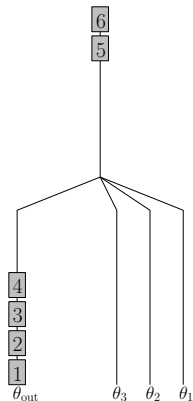
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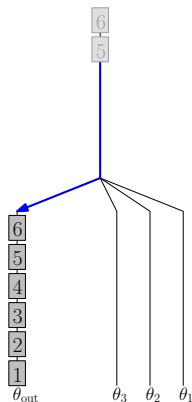
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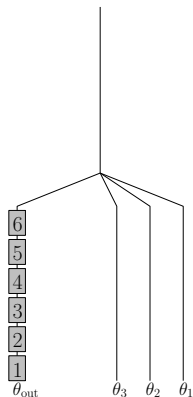
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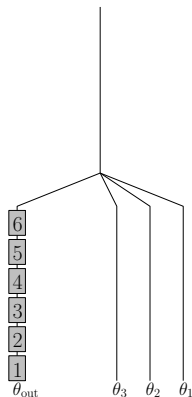
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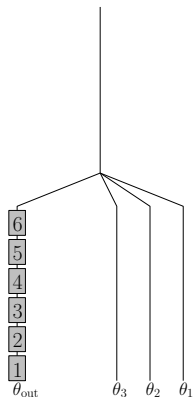
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Classification Process

1. initially roll-in input train
2. alternately **pull out** and **roll in**
3. finish with **ordered train**

Example Classification Process



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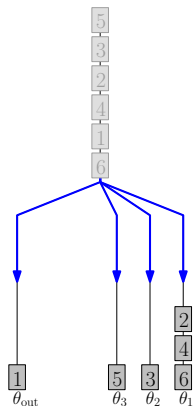
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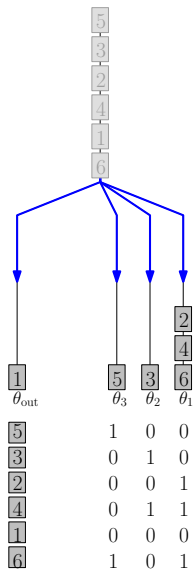
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Objective: **number h of pull-out steps**

Schedule Encoding [JMMN07]



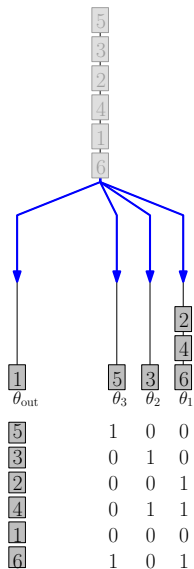
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Schedule representation

- ▶ **assignment** of cars to bitstrings of length h
- ▶ rows: **bitstring** b^j encodes journey of j th **car**
- ▶ columns: **bits** encode **sequence of pull-out steps**
- ▶ bit $b_i^j = 1$ iff j th car visits track pulled in i th step

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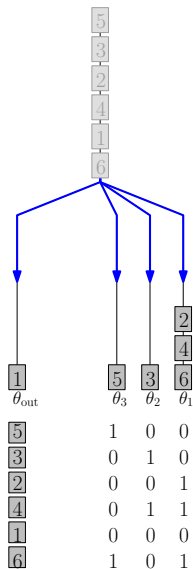
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Schedule derivation: two **consecutive** cars τ and $\tau + 1$

- ▶ correct order: assign **same** bitstring
- ▶ reversed order: assign **bigger** bitstring to $\tau + 1$

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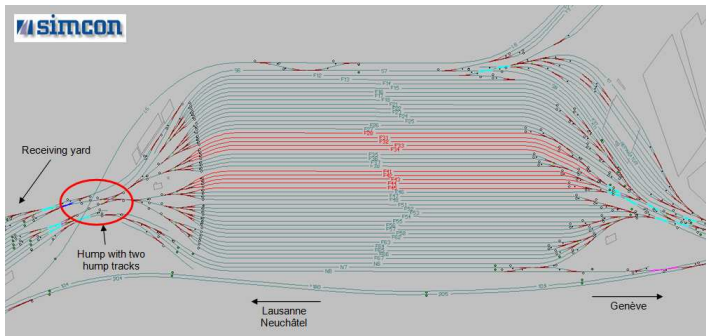
- ▶ correct order: assign **same** bitstring
- ▶ reversed order: assign **bigger** bitstring to $\tau + 1$
- ▶ objective: **length h of schedule**

Basic IP Model [MN09]

$$\begin{aligned}
 \min \quad & \sum_{\substack{1 \leq i \leq n \\ 0 \leq j < h}} b_i^j \\
 \text{s.t.} \quad & \sum_{0 \leq j < h} 2^i b_i^j \geq \text{rev}(j-1, j) + \sum_{0 \leq j < h} 2^i b_i^{j-1} \quad \forall j \in \{1, \dots, n\} \setminus F \quad (1) \\
 & \sum_{1 \leq i \leq n} b_i^j \leq C \quad \forall i \in \{0, \dots, h-1\} \quad (2) \\
 & b_i^j \in \{0, 1\} \quad \forall j \in \{1, \dots, n\} \\
 & \quad \quad \quad \forall i \in \{0, \dots, h-1\} \quad (3)
 \end{aligned}$$

- ▶ $\text{rev}(j-1, j) = 1$ iff cars $j-1$ and j in **reversed** order in incoming train
- ▶ F subset of cars that are **first in** their respective **outgoing train**
- ▶ classification tracks have **capacity** C

Real-World Instance: Lausanne-Triage



Traffic data

- ▶ single day in 2005
- ▶ volume 328 cars
- ▶ 23 outgoing trains

Infrastructure and operation

- ▶ two parallel humps
- ▶ local freight trains: collect on ten tracks
- ▶ time window for pull-out steps
- ▶ further tracks for outgoing train formation

Extended IP Model [MN09]

Additional constraints for Lausanne-Triage

- ▶ **initial roll-in restricted** to ten tracks
- ▶ assignment of outgoing trains to **either hump**
- ▶ respect **departure times**

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Additional constraints for Lausanne-Triage

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Resulting schedule

- ▶ one step shorter
- ▶ one track less required
- ▶ verification by computer simulation in progress (not finished yet)

Concluding Remarks

Conclusion

- ▶ encoding yields **flexible IP model**
- ▶ adapts to various **real-world restrictions**
- ▶ Lausanne-Triage: save **one step and track**

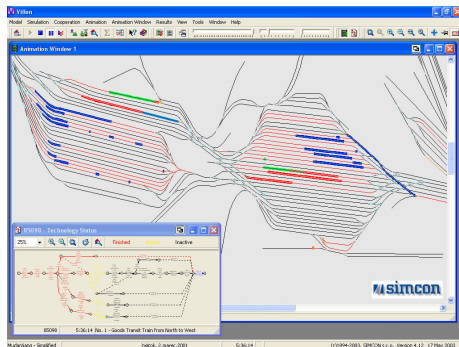
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Ongoing work

- ▶ **computer simulation** for Lausanne-Triage (Villon)
- ▶ evaluation of **2-approximation**
- ▶ **time-dependent input**
- ▶ **robustness** questions



References



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