

# Macroscopic Modelling of Parking Dynamics in Urban Networks

SVT

Jin Cao, Monica Menendez  
IVT, ETHZ, Switzerland

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# Urban Parking & Traffic Performance

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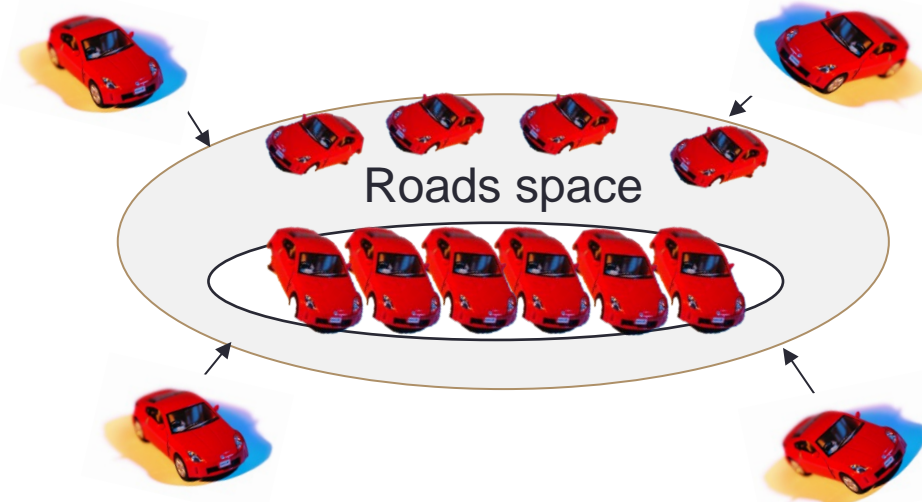
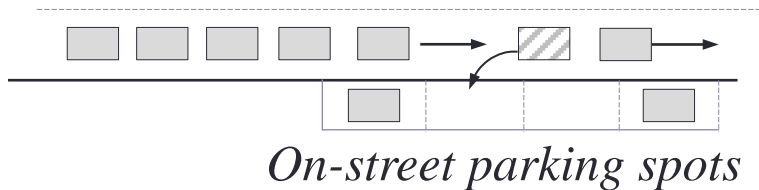
Introduction

Model

Conclusions

Parking affect traffic through:

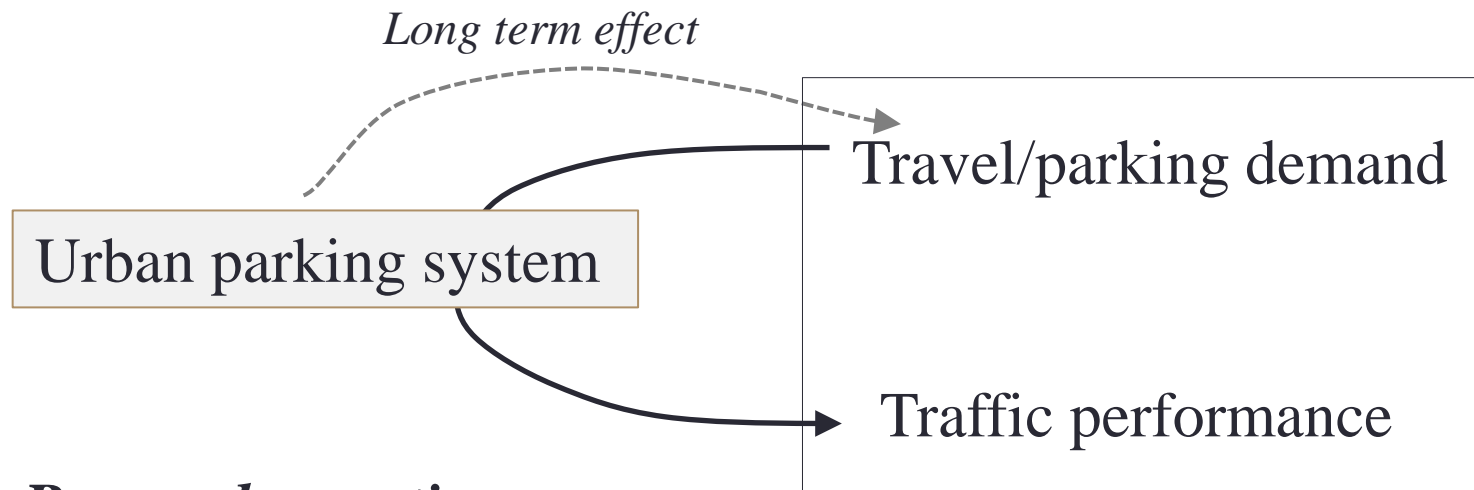
1. "Searching/cruising for parking" traffic
2. Extra traffic delay caused by parking maneuvers



Data related: Shoup (2005); IBM Global Parking Survey (2011); Cao (2014)



# Urban Parking & Traffic Performance



## *Research question:*

Under a given travel demand,

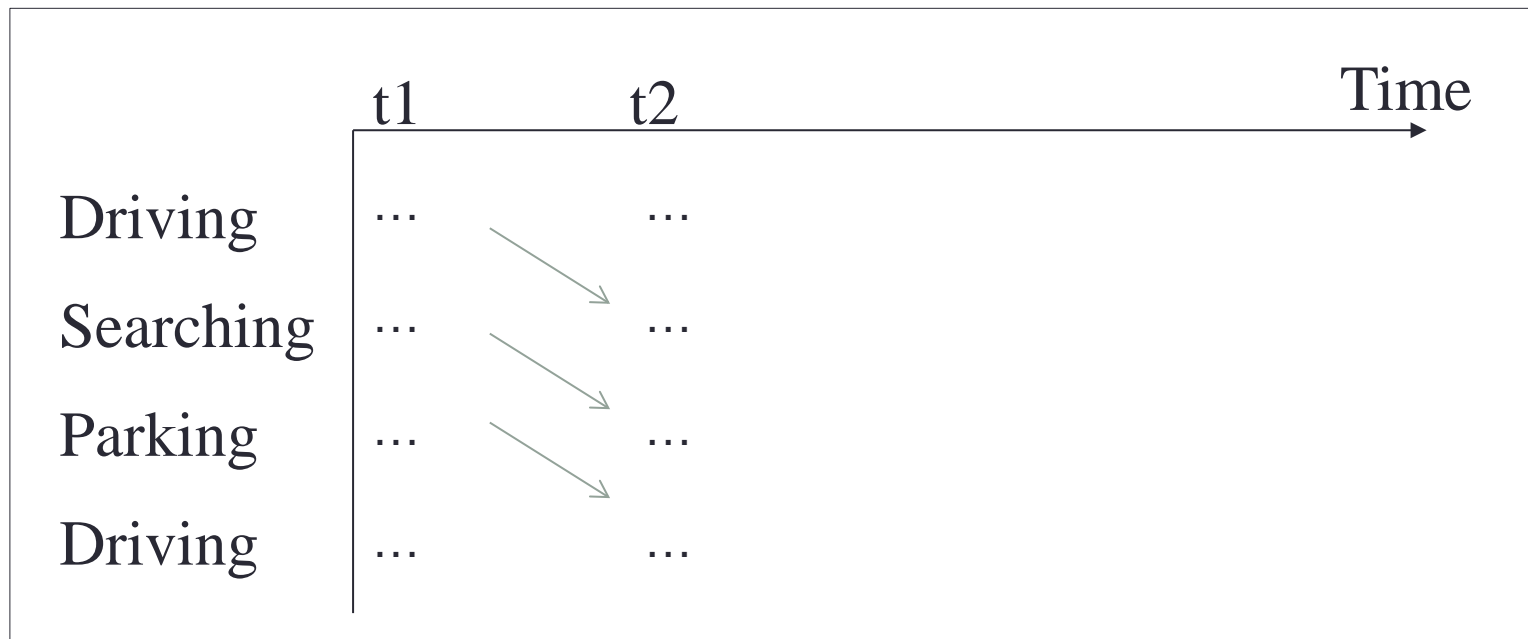
- How does parking system affect traffic performance?
- How does traffic affect parking system?

**Microscopic**

**Macroscopic** modelling of parking dynamics in urban networks

# Parking-state-based Transition Matrix

The parking-state-based transition matrix of vehicles on network



In the matrix, the number of cars in each parking-state is shown.

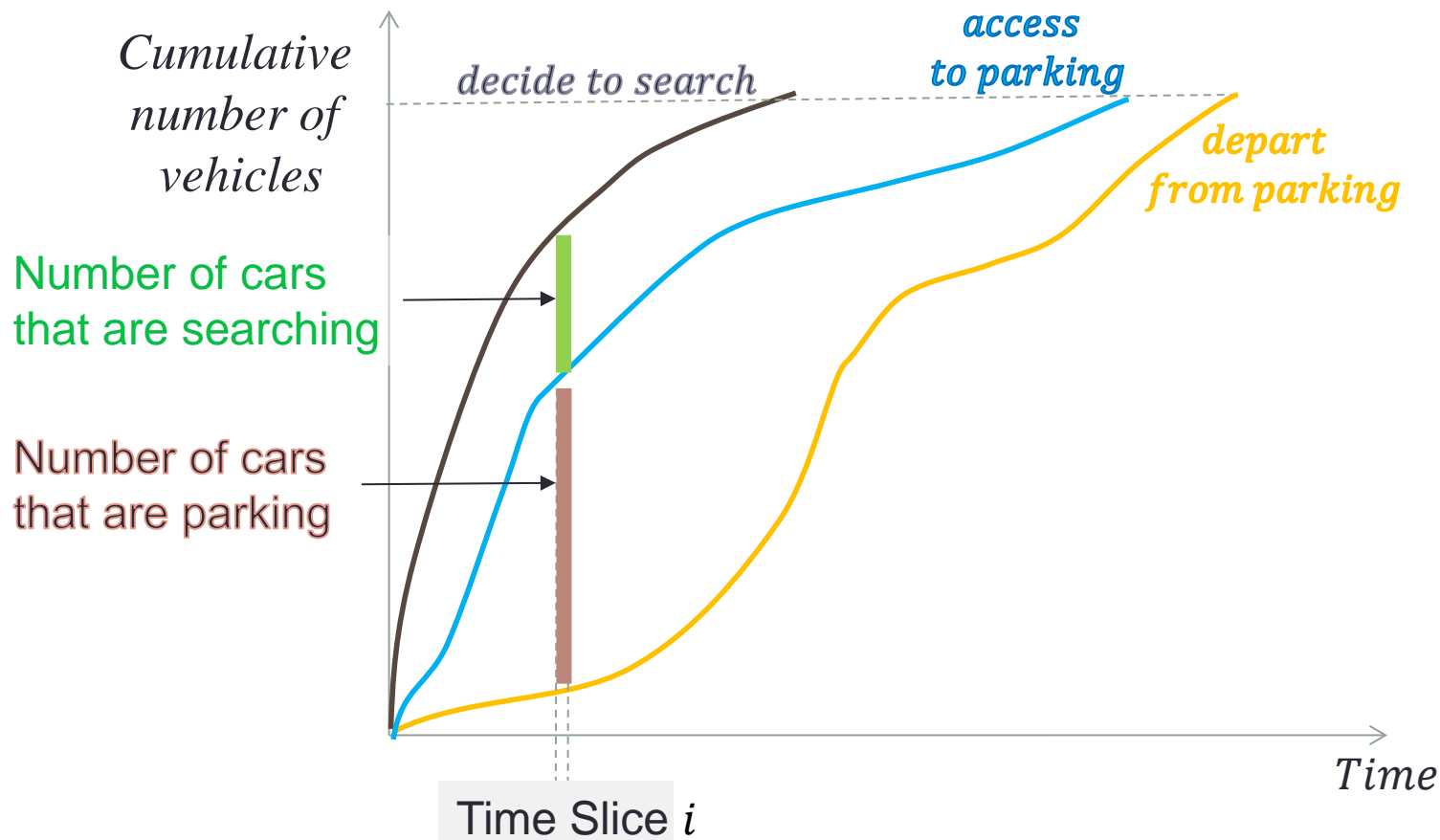
# Parking-state-based Transition Matrix

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“Queuing diagram” of vehicles on urban networks

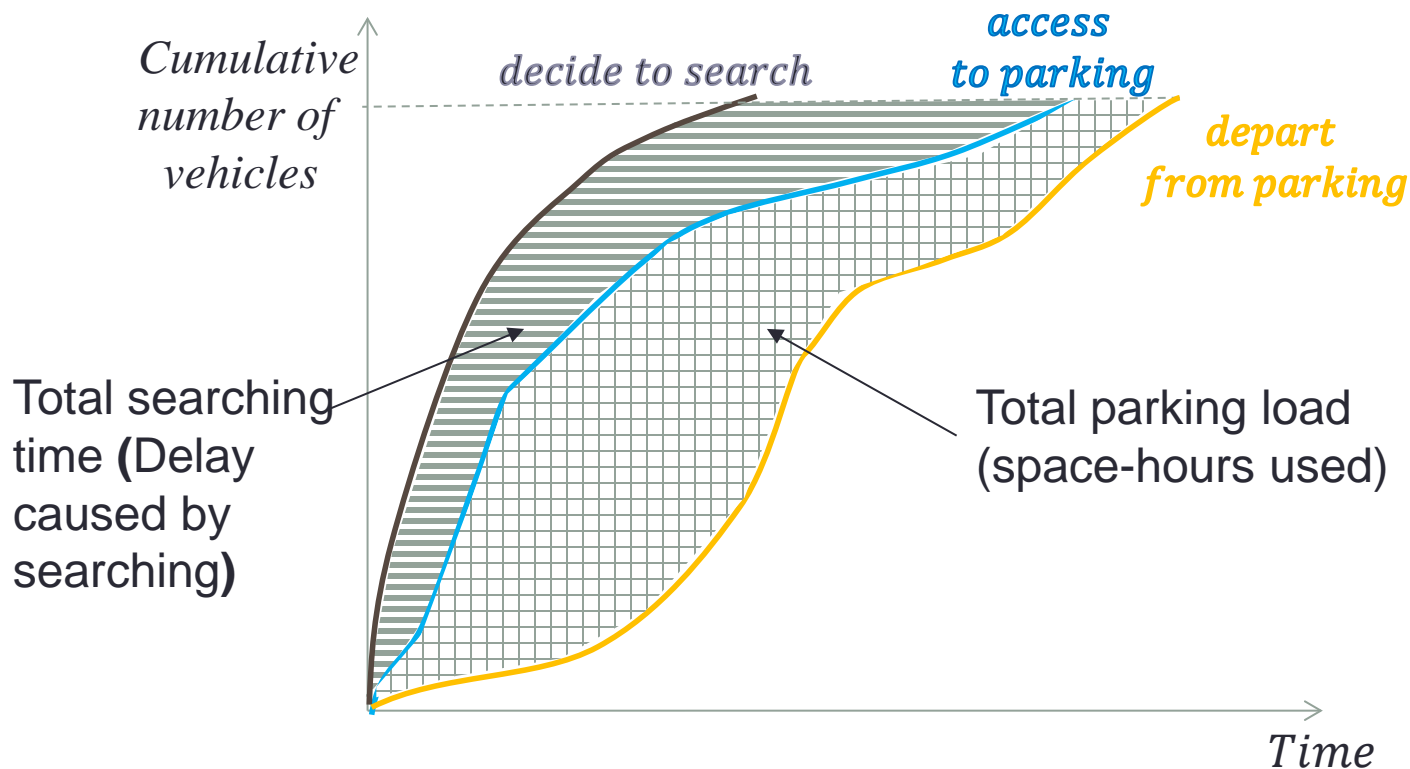
# Parking-state-based Transition Matrix

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“Queuing diagram” of vehicles on urban networks

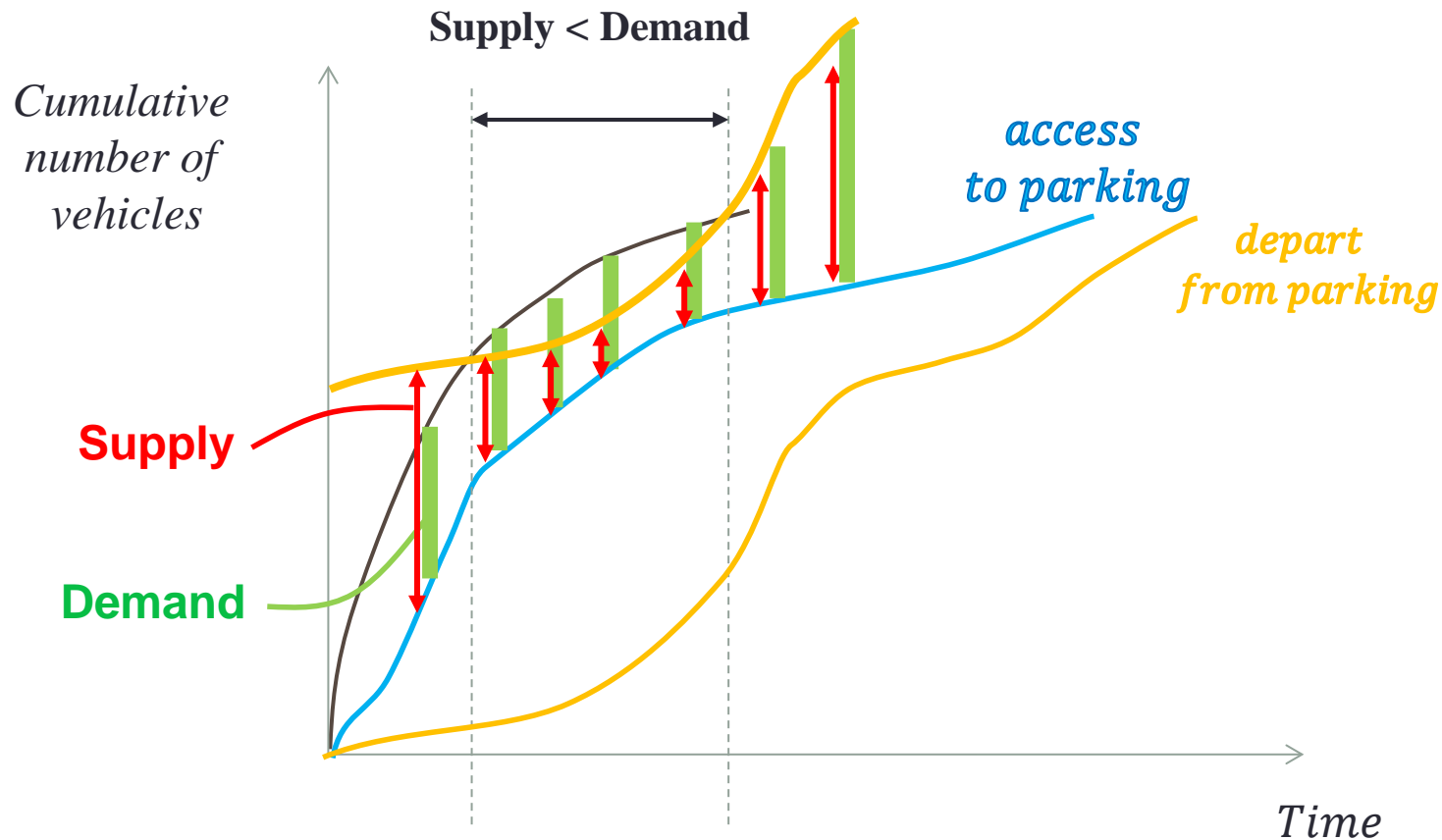
# Parking-state-based Transition Matrix

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“Queuing diagram” of vehicles on urban networks



# Parking-state-based Transition Matrix

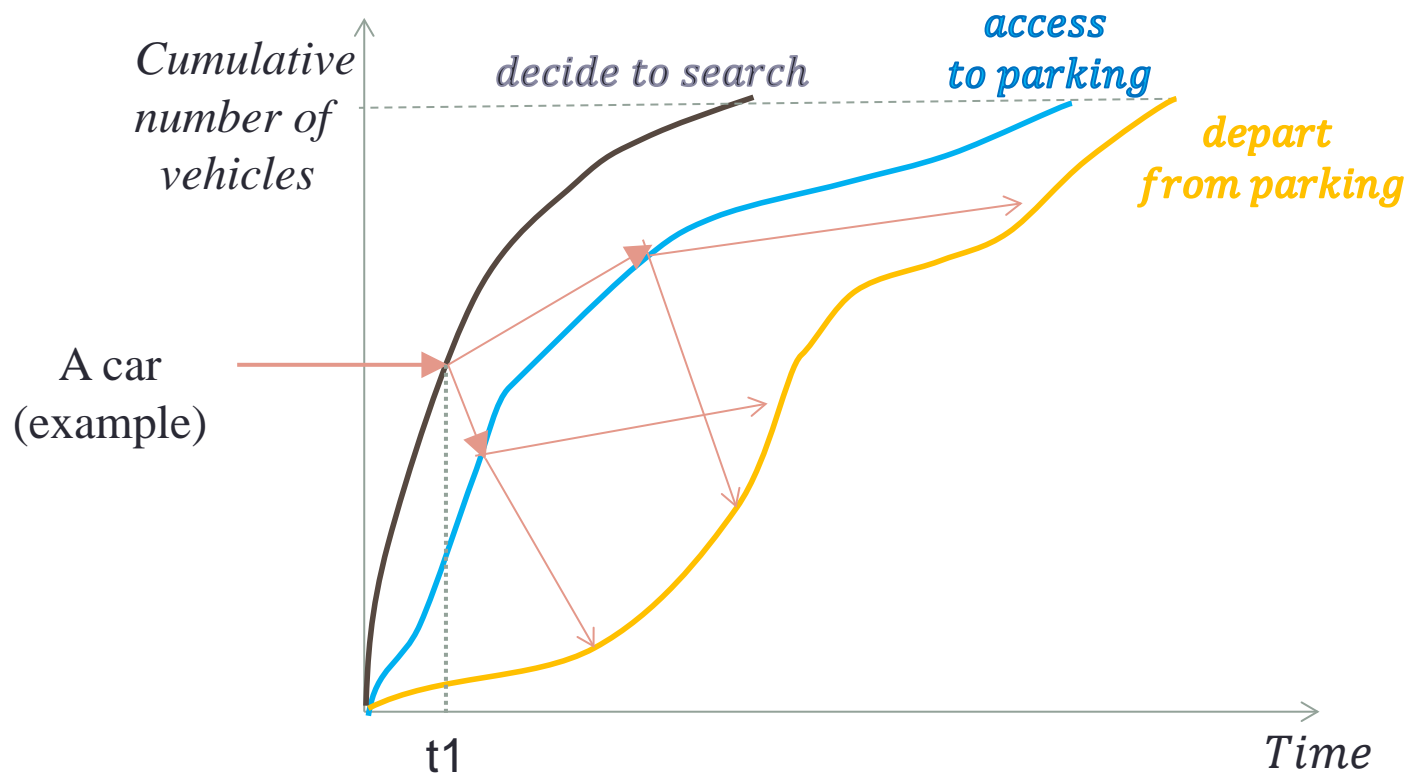
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Info shortage for any individual trip, as the system is not a FIFO.



“Queuing diagram” of vehicles on urban networks

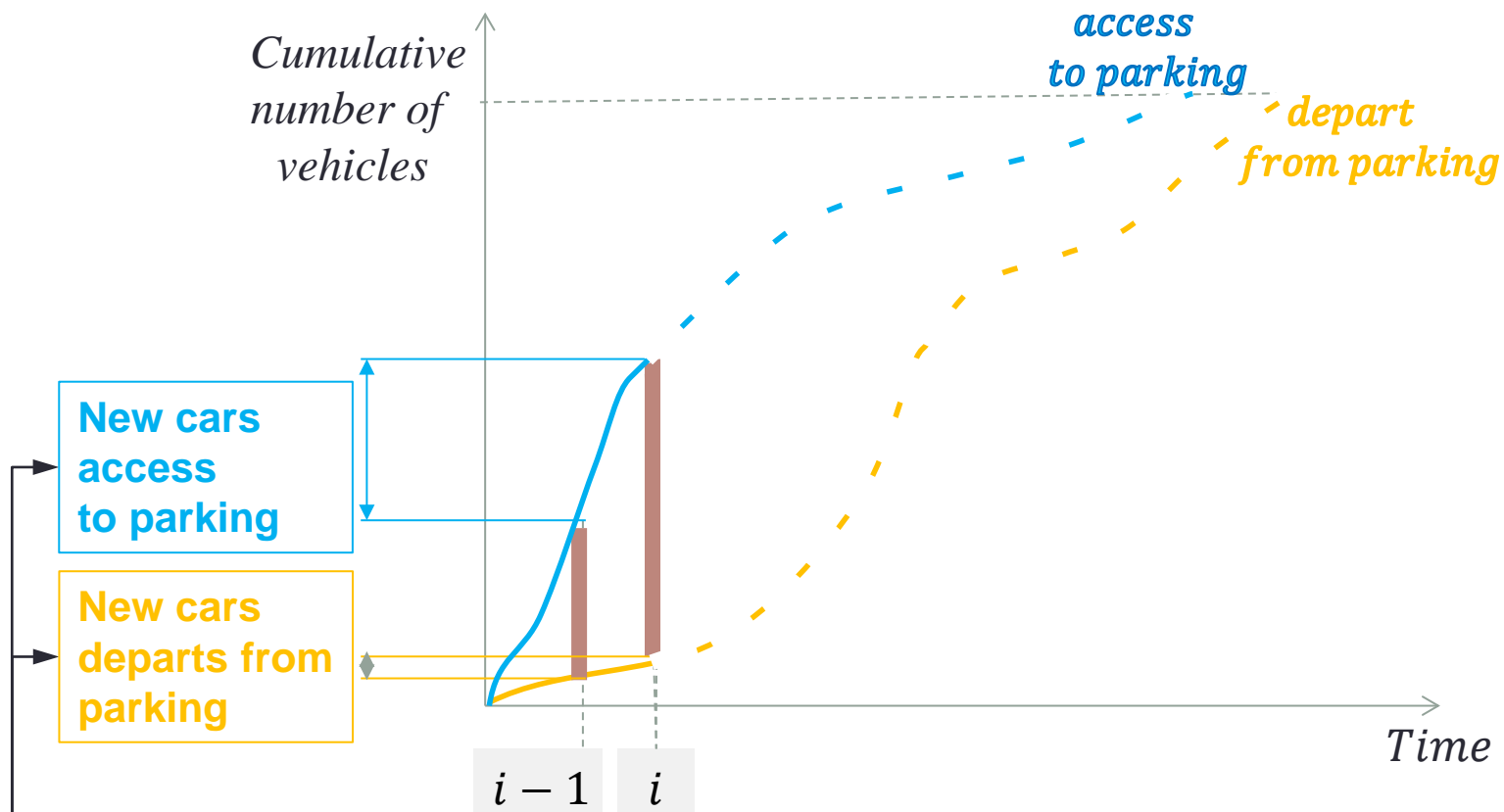
# Construct the Matrix

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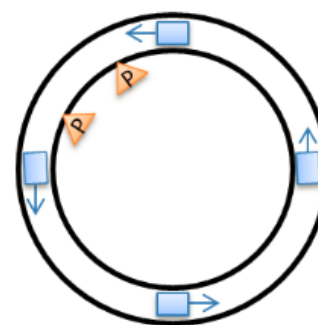
Conclusions



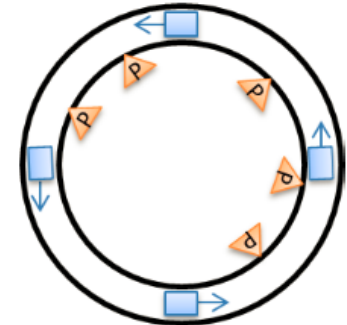
Incrementally construct the curves/matrix

# Model

New cars  
access  
to parking  $\rightarrow n_{access}=?$



(a)



(b)

Basic assumption.

Basic variables:

$d$  the maximum driving distance of each car is  $d = vt$ .

$L$  the size of the network is  $L$  (the total length of the ring road).

$N$  at the beginning of the period, there are  $N$  cars searching for parking.

$A$  at the beginning of the period, a number of  $A$  parking spots are available.

# Model (results)

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$$\text{when } d \in [0, s], n = N \cdot \left[1 - \left(1 - \frac{d}{L}\right)^A\right].$$

Eq 1(a)

$$\text{when } d \in (s, L), n =$$

Eq 1(b)

$$n_{\text{access}} = \left\{ \begin{array}{l} A \cdot \left\{ 1 - \frac{N}{L} \cdot \left\{ \int_{d-(m-1)s}^s \left\{ \sum_{i_{m-1}=m-1}^{A-1} C_{A-1}^{i_{m-1}} \left[ \frac{(N-m+2)s-x}{L} \right]^{A-1-i_{m-1}} \right\} dx \right\} \right. \\ \left. \left\{ \int_{d-(m-1)s}^s \left\{ \sum_{i_{m-2}=m-2}^{i_{m-1}} C_{i_{m-1}}^{i_{m-2}} \dots \sum_{i_1=1}^{i_2} C_{i_2}^{i_1} \left[ \left(\frac{x}{L}\right)^{i_1} \cdot s^{(i_{m-1}-i_1)} \right] \right\} \right\} dx \right\} \right. \\ \left. \left\{ \int_0^{d-(m-1)s} \left\{ \sum_{i_m=m}^{A-1} C_{A-1}^{i_m} \left[ \frac{(N-m+1)s-x}{L} \right]^{A-1-i_m} \right\} dx \right\} \right. \\ \left. \left\{ \sum_{i_{m-1}=m-1}^{i_m} C_{i_m}^{i_{m-1}} \dots \sum_{i_1=1}^{i_2} C_{i_2}^{i_1} \left[ \left(\frac{x}{L}\right)^{i_1} \cdot s^{(i_m-i_1)} \right] \right\} dx \right\} \right. \\ \left. \left\{ \int_{d-(m-1)s}^s \left\{ \sum_{i_{m-1}=m-1}^{A-1} C_{A-1}^{i_{m-1}} \left[ \frac{(N-m+2)s-x}{L} \right]^{A-1-i_{m-1}} \right\} dx \right\} \right. \\ \left. \left\{ \sum_{i_{m-2}=m-2}^{i_{m-1}} C_{i_{m-1}}^{i_{m-2}} \dots \sum_{i_1=1}^{i_2} C_{i_2}^{i_1} \left[ \left(\frac{x}{L}\right)^{i_1} \cdot s^{(i_{m-1}-i_1)} \right] \right\} dx \right\} \right\} \end{array} \right. \begin{array}{l} \text{if } A < m \\ \text{if } A = m \\ \text{if } A > m \end{array}$$

$$\text{when } d \in [L, \infty), n = \min\{A, N\}.$$

Eq 1(c)

# Model (results)

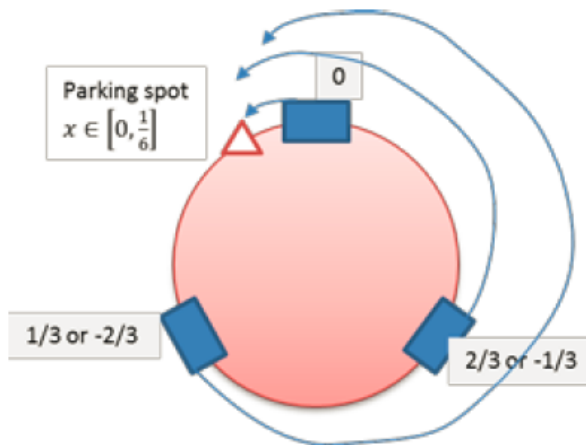
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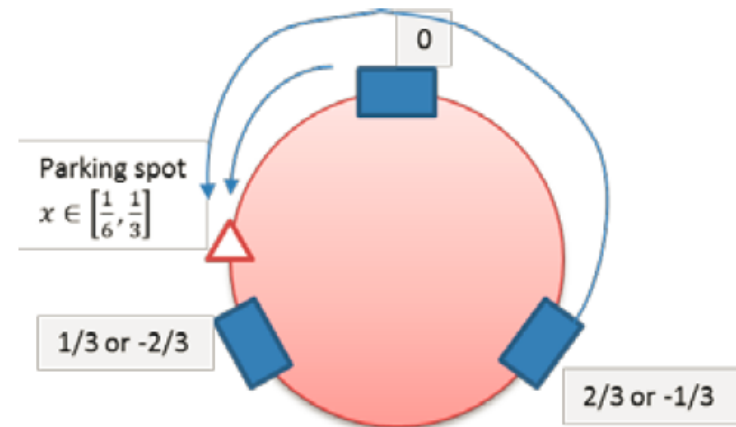
Model

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## Examples



(a) if  $x \in [0, \frac{1}{6}]$ , a number of  $m=3$  cars can reach  $x$ .



if  $x \in [\frac{1}{6}, \frac{1}{3}]$ , a number of  $m-1=2$  cars can reach  $x$ .

For validation: the results (equation) is compared to the average value given by programmed experiments.

# Summary

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- The model for  $n_{access}$  allow us to imitate a practical situation with the imbalance between parking availability and demand, as well as the parking search phenomenon.
- But the model neglects the influence of the network shape (by assuming all streets have the same likelihood of being visited), and personal requirements for parking.
- Next step, to find the value of  $n_{depart}$  , number of cars departs from the parking facilities. Then build the matrix under the current framework and assumptions.
- Explore information from the transition matrix (or queuing diagram), relax the assumptions and improve the model to more generalized conditions.