

Generating timetables with partial periodicity

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Operated timetable in Switzerland

| | | | | | | |
|--------|-------|-------|-------|-------|-------|-------|
| Zürich | xx:04 | xx:35 | 16:41 | 17:41 | 18:41 | 00:07 |
| Luzern | xx:49 | xx:25 | 17:39 | 18:39 | 19:39 | 01:07 |
| Time | 0:45 | 0:50 | 0:58 | 0:58 | 0:58 | 1:00 |

Standard
offer

Peak hour
Additional
offer

| | | | | | | | |
|------------|-----------------------------|------------------|-----------------------------|--------|-----------------------------|--------|------------------|
| Wil | 6:25 | 6:54 | 7:25 | 7:54 | xx:25 | xx:54 | 22:54 |
| St. Gallen | 6:53 | 7:17 | 7:53 | 8:15 | xx:53 | xx:15 | 23:17 |
| stops | Uzwil, Flawil, Gossau | Uzwil, Gossau | Uzwil, Flawil, Gossau | Gossau | Uzwil, Flawil, Gossau | Gossau | Uzwil, Gossau |
| Time | 0:28 | 0:23 | 0:28 | 0:21 | 0:28 | 0:21 | 0:23 |

Off-peak
hour
offer

Operated timetable abroad

Standard
offer

| | | | | | | | | |
|-----------|-------|-------|-------|-------|-------|-------|-------|-------|
| Milano | 7:15 | 7:45 | 8:15 | 8:30 | 8:45 | 9:30 | 10:30 | 11:30 |
| Roma | 10:45 | 11:15 | 11:45 | 12:29 | 12:59 | 13:29 | 14:29 | 15:29 |
| Time | 3:30 | 3:30 | 3:30 | 3:59 | 4:14 | 3:59 | 3:59 | 3:59 |
| Paris | 10:10 | 12:10 | 14:10 | 14:40 | 15:15 | 15:50 | 16:10 | 17:20 |
| Bordeaux | 13:11 | 15:24 | 17:14 | 17:38 | 18:48 | 18:52 | 19:17 | 20:23 |
| Time | 3:01 | 3:14 | 3:04 | 2:58 | 3:33 | 3:02 | 3:07 | 3:03 |
| Stuttgart | 12:07 | 14:07 | 14:40 | 16:07 | 16:42 | 18:07 | 18:40 | -:- |
| Nürnberg | 14:16 | 16:16 | 17:25 | 18:16 | 19:25 | 20:16 | 21:25 | -:- |
| Time | 2:09 | 2:09 | 2:45 | 2:09 | 2:43 | 2:09 | 2:45 | -:- |

Arising questions

- How should we consider the presented timetables?
Periodic or **non-periodic**?
- **Why** were these timetables so generated?
- **How** are they generated?

Remarks on periodicity

- Periodicity is important for the passengers
 - It should be **part of the offer**
- Irregularities are necessary to face **changing demand** over the day
 - Additional services in peak hours
 - Different demand in the evening
- Currently:
 - **Manually**, or
 - **Manual postprocessing** of automatic periodic timetabling

Why?

How?

Current approaches

- **Periodic timetabling**
 - + Good for regularity
 - Needs postprocessing for irregularities
 - Optimises only a part of the day
- **Non-periodic timetabling**
 - + Good for irregularities
 - Loses offer of periodicity
 - Larger size
- **New approach: Partial periodic timetabling**

Partial periodic timetabling

1. Consider service intention for a whole day, with **periodicity and exceptions as part of the offer**
2. Formalise it in the **partial periodic service intention**
3. Generates partial periodic timetables
 - Advantages:
 - No need of postprocessing
 - Allows optimisation all over the day

Partial periodic service intention

- Description of intended transport services for one day
- Set of services:
 - Train runs, connections, time dependencies
- Reference periodicity T
- Spatial-temporal graph

Train run

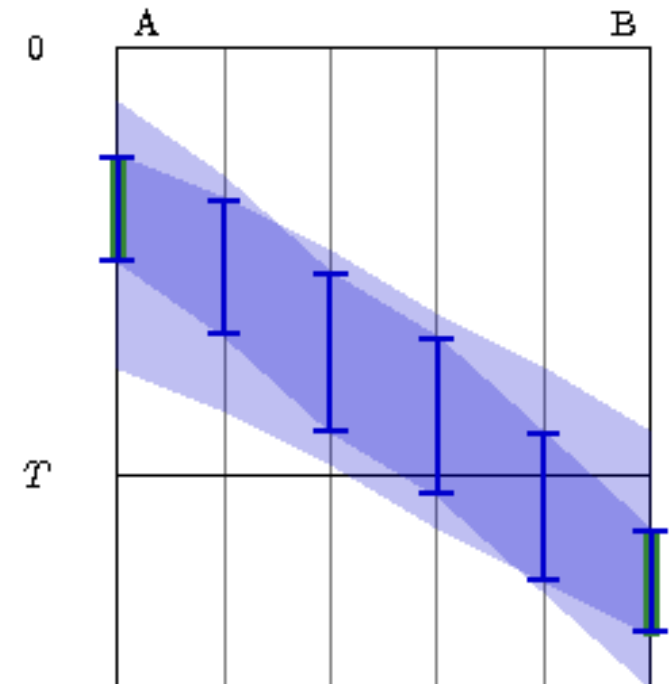
Service Intention

- Train run
- Connection
- Time dependency

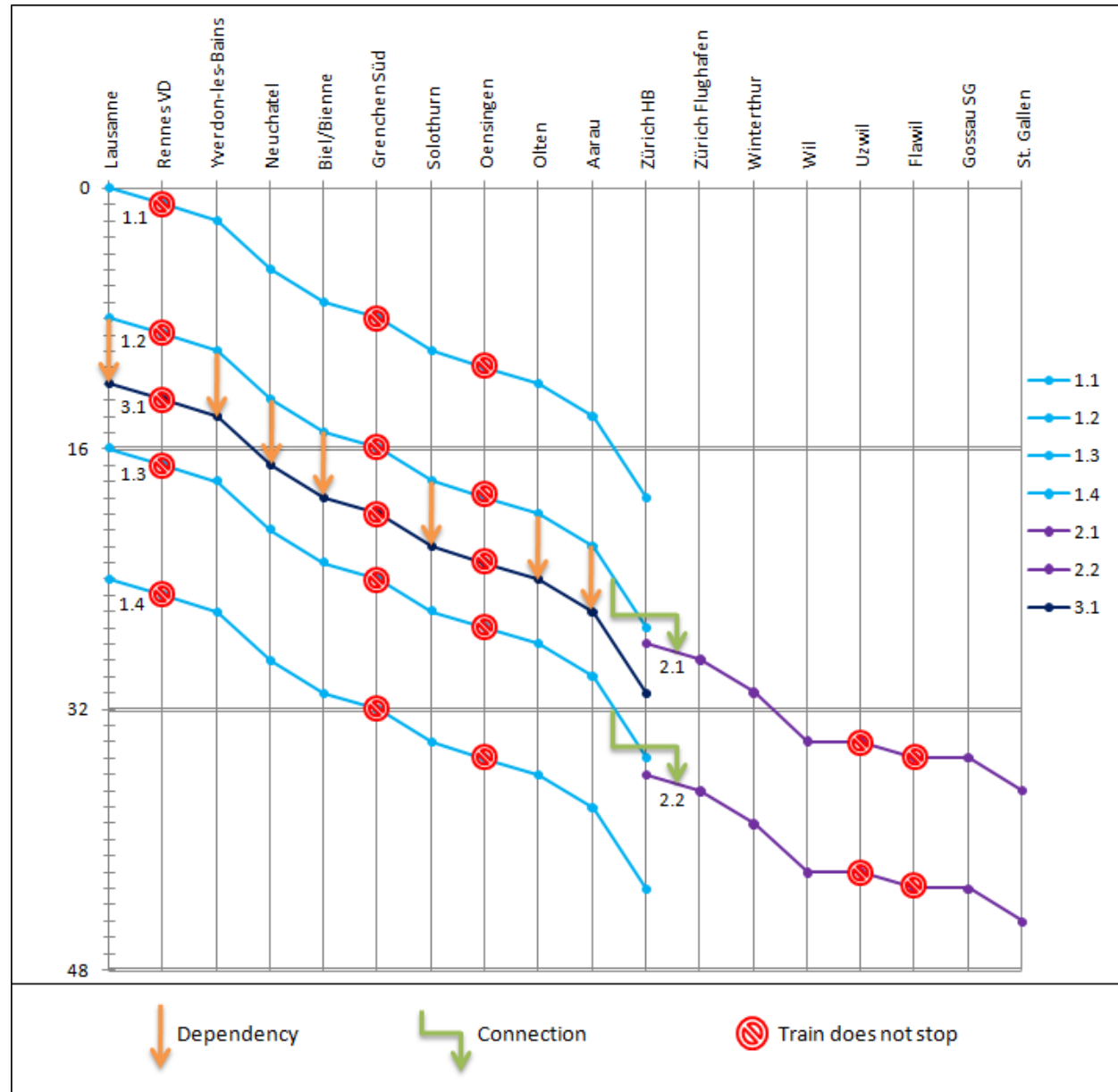
■ Sequence of stations with:

- Time slot for arrival / departure (at least one)
- Lower/upper bounds for:
 - Trip time
 - Dwell time (= 0 if train does not stop)
- Periodicity
- First recurrence
- Number of recurrences

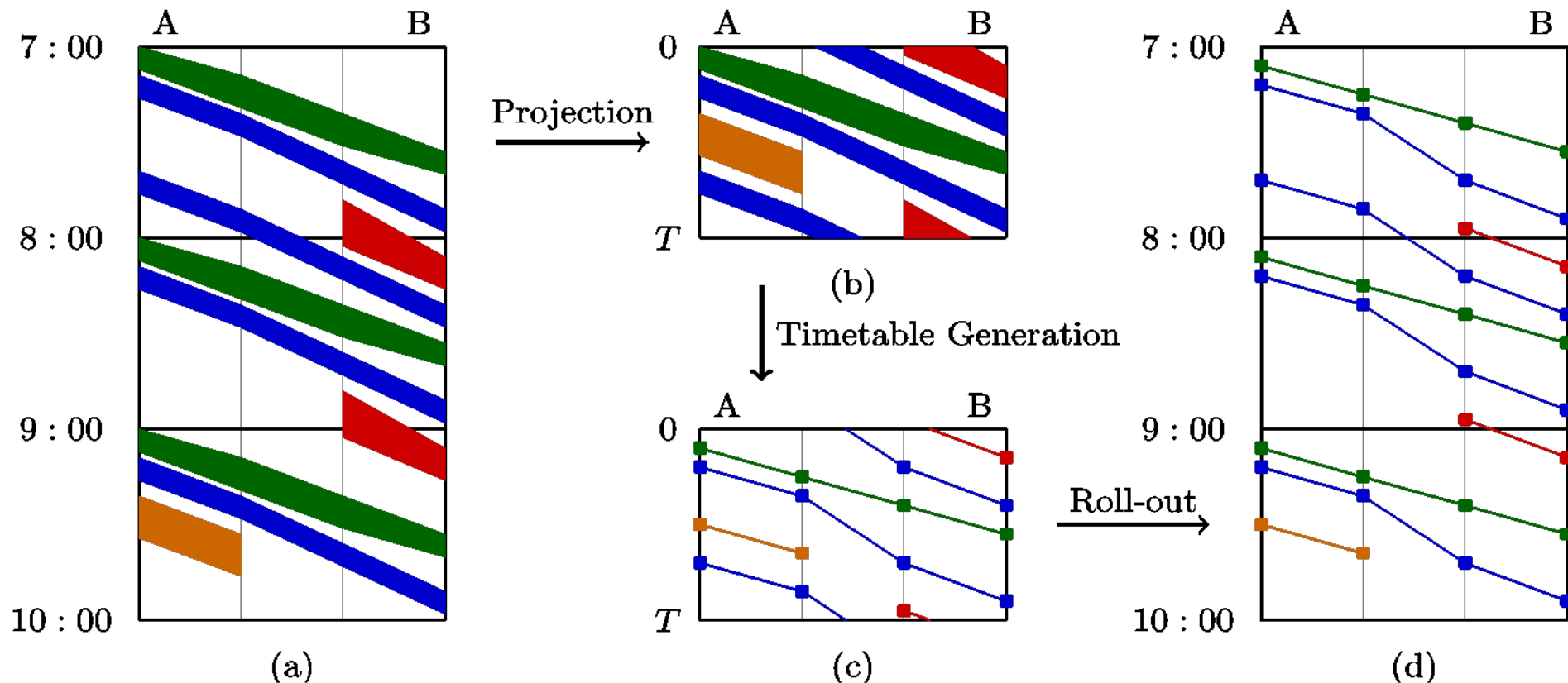
■ Similar for connections and time dependencies



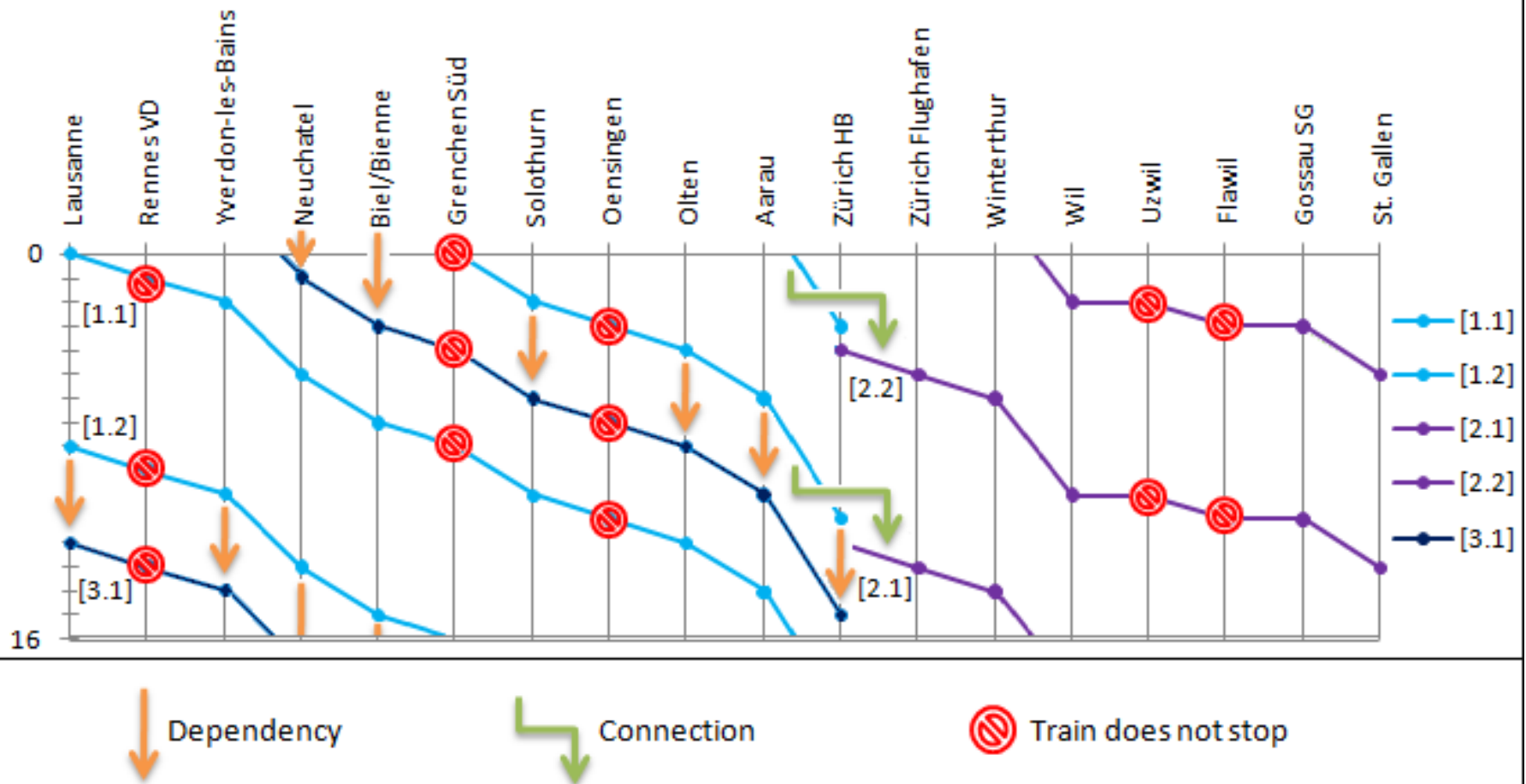
Example



Solution approach: basic idea



Projection: example



Model for projected problem

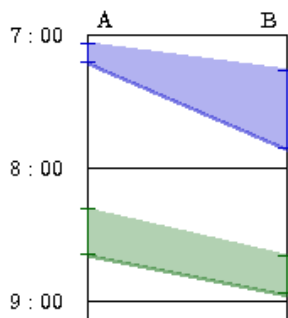
- Projected problem is modeled as a **Periodic Event Scheduling Problem** (PESP)
- Decision variables are event times (departure and arrival) of projected equivalence classes
- Train service constraints are easily modeled in PESP
- **Headway constraints** are different than classical PESP

Introduction (or not) of headway constraints

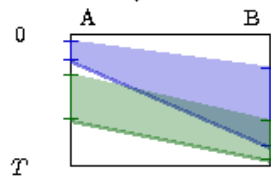
- If projection does not need headway
→ do **not** introduce **headway** constraint
- If projection needs headway
→ **check** original train service intention

Introduction (or not) of headway constraints

■ Headway necessary in the original version?

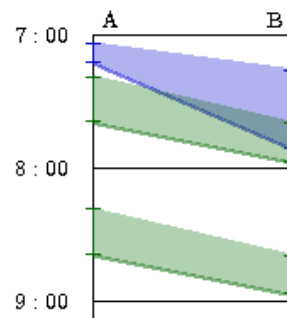


Projection

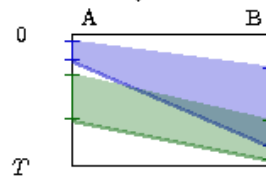


(a)

No → No headway

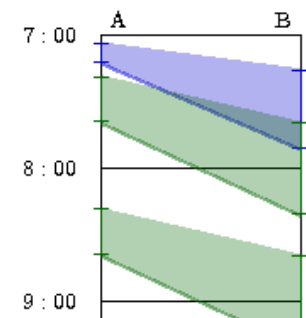


Projection

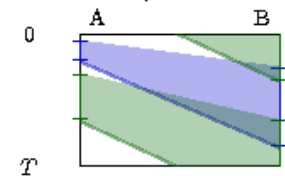


(b)

Yes → headway



Projection



(c)

Once yes and once no
→ special situation (*)

headway

Equivalence of the problem

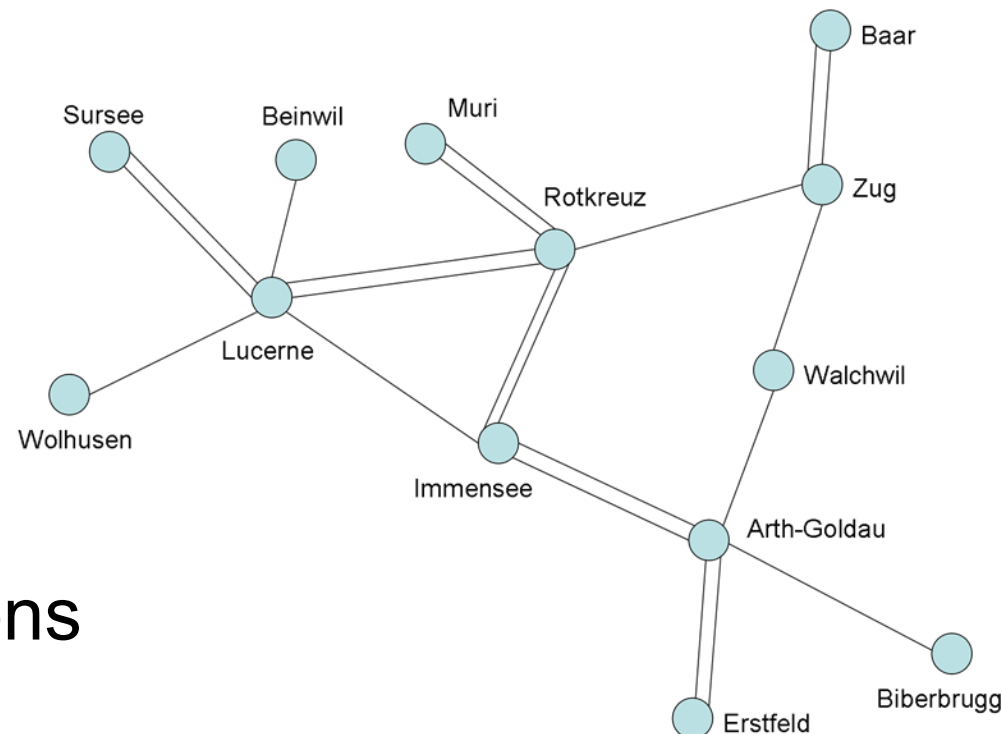
- If (situation $(*)$ does not occur) and (all time slots have size $< T$), then:

Original Problem
is **equivalent** to
Projected Problem

- i.e. Solution Spaces are equivalent

Test scenario

- Central Switzerland: Zug – Lucerne – ArthGoldau
- Reverse-Engineering from 2008 SBB-Schedule
- Trains:
intercity, local, cargo
- Compare with **fully periodic variant**
without peak hours
or late evening exeptions



Computational results

| Scenario | T | # variables | # integer | # constraints | CPU time [s] |
|---------------------------|-----|-------------|-----------|---------------|--------------|
| Partial periodic SI | 60 | 2206 | 963 | 3449 | 24# |
| | 120 | 2936 | 1278 | 4594 | 23 |
| | No | 12 122 | 5168 | 19 076 | 130 |
| Fully periodic | 60 | 802 | 341 | 1263 | 6 |
| | 120 | 1344 | 568 | 2120 | 2 |
| | No | 10 732 | 4544 | 16 920 | 70 |

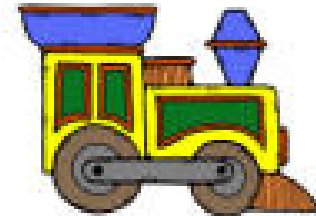
Situation (*) occurred, resulting in infeasible problem

In all other tests situation (*) did not occur

Conclusions

- Formalise partial periodicity, which is most common situation in practice
- Projection method enables the use of established methods for periodic timetabling
- The stronger the periodicity, the larger the size reduction
- Optimises over whole day, no need for post-processing

Thank You!



Time for questions!

Problem definition

■ INPUT

- Train service intention (incl. periodicity properties)
- Railway network
- Dynamic properties of rolling stock

■ OUTPUT

- Conflict-free train schedule
- Fulfilling service intention

Connection

Service Intention

- Train run
- **Connection**
- Time dependency

- Connects 2 train runs at a common station
- **Minimum** changing time from **station layout**
- **Maximal** changing time from **service intention**
- Periodicity
- First recurrence
- Number of recurrences

Time dependency

Service Intention

- Train run
- Connection
- **Time dependency**

- Between two 2 train runs
- Lower and upper bound for departure time difference
- e.g. to enhance the service during peak hours, or coordinate two different train runs on same (sub-)line

Solution approach: basic idea

1. **Project** all train runs on the periodic time $[0,T]$
 - Create **equivalence classes** of train runs
2. Apply existing solvers for **periodic scheduling**
3. **Roll out** the created timetable on the complete day
 - **Reduces** problem size

Train service intention

- List of train services offered to the customers, including:
 - Train lines with stop and frequencies
 - Interconnection possibilities
 - Rolling stock
- TSI can be generated by planners manually or partially automatic (e.g. line planning)