

Accuracy Study of Parking Duration Data from Patrol Survey

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Patrol Survey

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Introduction**Model****Simulation****Conclusions**

Patrol Survey

Average parking duration



Patrol Survey



Introduction

Model

Simulation

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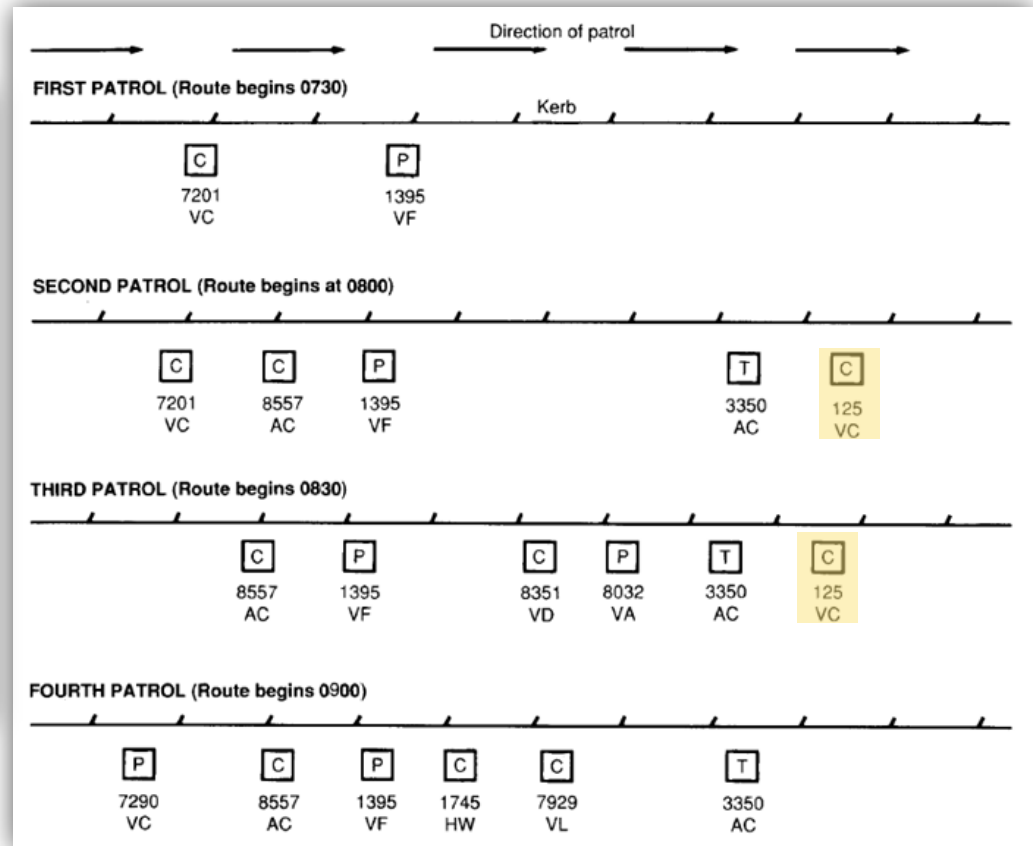
Patrol Survey

Figure 4.3 Parking Patrol Survey form: Example

Registration Number	Time at Start of Route																	
	hh	mm		hh	mm		hh	mm		hh	mm		hh	mm				
	07	30	V	07	45	V	08	00	V	08	15	V	08	30	V	08	45	V
1	7201	VC	C	7201	VC	C	8557	AC	C	7290	VC	P	7290	VC	P	7290	VC	P
2	1395	VF	P	8557	AC	C	1395	VF	P	8557	AC	C	8557	AC	C	8557	AC	C
3				1395	VF	P	8351	VD	C	4579	VC	Ⓢ	4579	VC	Ⓢ	4579	VC	Ⓢ
4				3350	AC	T	8032	VA	P	1395	VF	P	1395	VF	P	1395	VF	P
5				125	VC	C	3350	AC	T	1745	HW	C	2223	VL	C	2223	VL	C
6							125	VC	C	7929	VL	C	7929	VL	C	3350	AC	T
7										3350	AC	T	3350	AC	T	1234	VC	C
8																		
9																		
10																		
11																		
Total	2			5			6			7			7			7		
New Arrivals	N/APP			3			2			4			1			1		
Departures	N/APP			0			1			3			1			1		
Notes	←			Heavy rain			→			←			rain stop					

(Circled letters indicate double-parked vehicles)

e.g., interval $\delta=30$ minutes



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Patrol Survey

Reg. No.	number of times seen	Duration (m)
		known
7201 VC	2	
1395 VF	7	
8557 AC	5	150
3350 AC	6	
125VC	2	60
8351 VD	1	30
2223 VL	3	
1234 VD	1	30
TOTALS	37	480 / 7

Average parking duration (APD)
Estimated APD \approx Real APD

Accurate?




Expensive?

Current solution:
Tradeoff

Goals

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- The necessity to make a tradeoff is unknown as the current accuracy is unknown.  Find the current accuracy
- What did the tradeoff brought? In other words, how much did the accuracy increase by more investment?  Find the improvement of accuracy from a tradeoff
- Is there another way to increase the accuracy besides a higher budget?  Find another method to improve the accuracy

Assumptions

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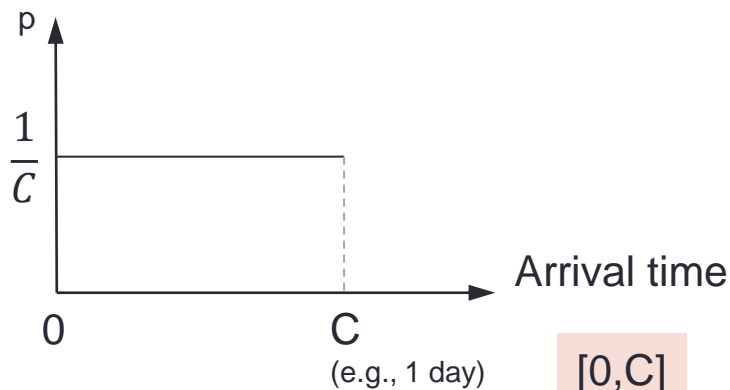
Introduction

Model

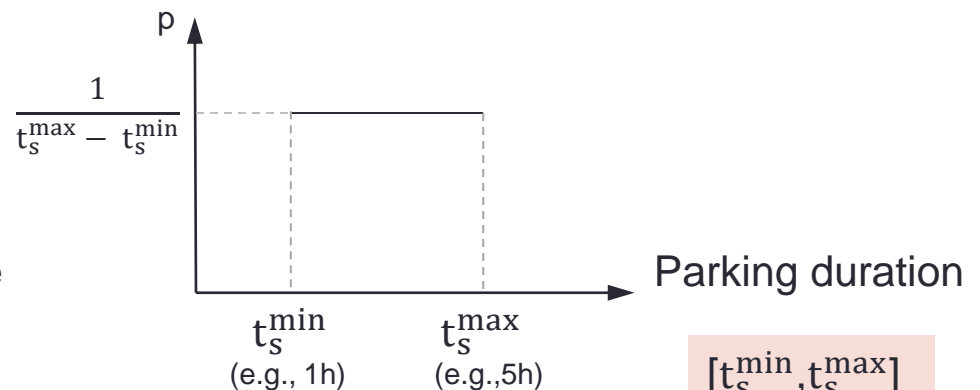
Simulation

Conclusions

- Imagine a simple parking scenario, a public parking area with enough supply and no restrictions of time and payment.


 $[0, C]$

cycle


 $[t_s^{\min}, t_s^{\max}]$

Minimum time of stay

Maximum time of stay

Model

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δ observation interval

APD
average parking duration

β the ratio of t_s^{max} and t_s^{min}

$$= \frac{b}{a}$$

\bar{T}^{real} real APD

$$= \delta \cdot \frac{a+b}{2}$$

\tilde{T}^{obs} estimated APD

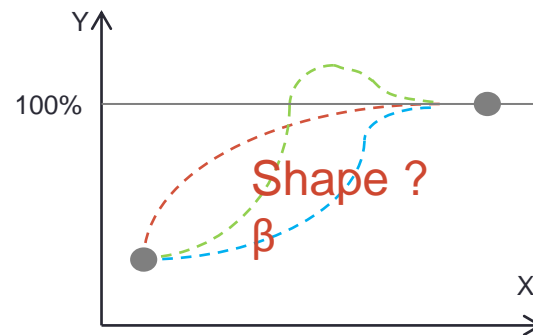
$$= \delta \cdot \sum_{i=1}^{|b|} i \cdot \left(\frac{p_i}{p^{obs}} \right)$$

“survey intensity”

$$X = \frac{\tilde{T}^{obs}}{\delta}$$

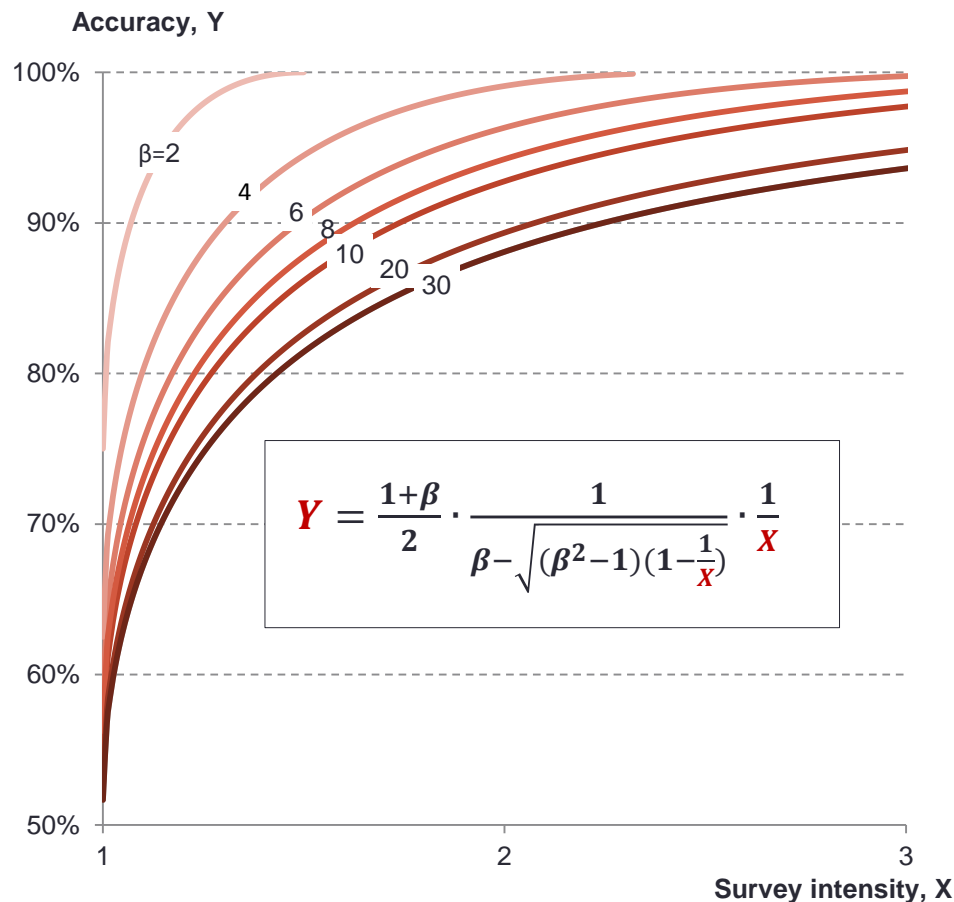
“accuracy”

$$Y = \frac{\bar{T}^{real}}{\tilde{T}^{obs}}$$



$$Y = \frac{1+\beta}{2} \cdot \frac{1}{\beta - \sqrt{(\beta^2-1)\left(1-\frac{1}{X}\right)}} \cdot \frac{1}{X}$$

Model



While $\delta \in [t_s^{\min}, t_s^{\max}]$

- For a given β , the value of X varies from 1 to $\frac{1+\beta}{2}$, a higher X corresponds to a lower δ .
- The average parking duration is always overestimated, the minimum value of the accuracy is $\frac{1}{2} + \frac{1}{2\beta}$.
- For a given survey intensity X, the accuracy is higher with a smaller β . Hence, one can find the lowest possible accuracy for a given range of β .

Numerical Example

- A basic range of β could be obtained in a survey by approximating the longest and shortest parking duration.
- A patrol survey with interval $\delta=3$ hours, the data and results are analyzed.

Table 1 Survey results of the numerical example

No.	δ	No. of vehicles observed	Percentage/times			\bar{T}^{obs}	X
			1	2	3		
1	$\delta_1 = 3$	271	38%	45%	17%	5.4	1.79
2	$\delta_2 = 6$	199	92%	8%	-	6.5	1.08
3	$\delta_3 = 9$	164	100%	-	-	9	1

$$t_s^{\min} < 3$$

$$t_s^{\max} \leq 9$$

$$t_s^{\max} \in [6, 12]$$

Numerical Example

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- We can assume a conservative value (i.e., 0.3 hours) as a minimum duration for vehicles base on real life experience. It means that, a person only parks the car when he/she needs to stay for more than 0.3 hours.

$$t_s^{\max} \in [6,9]$$

$$t_s^{\min} \in [0.3,3]$$

$$\beta \in [2,30]$$

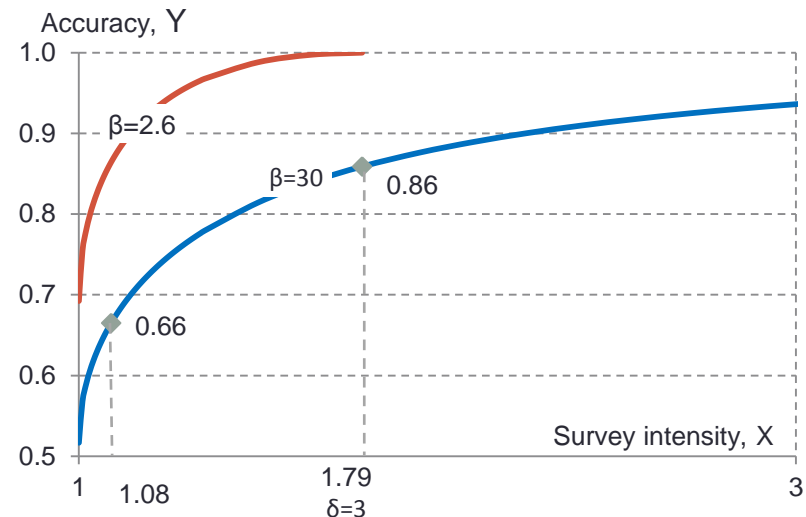
No.	δ	\bar{T}^{obs}	X
1	$\delta_1 = 3$	5.4	1.79
2	$\delta_2 = 6$	6.5	1.08
3	$\delta_3 = 9$	9	1

$$X \in \left[1, \frac{1 + \beta}{2} \right]$$

$$\beta > 2.58$$

$$X = 1.79 \text{ when } \delta = 3$$

So $\beta \in [2.58, 30]$, then we can find both the lower and upper bounds for the accuracy of the survey as a function of X.



Results and correction

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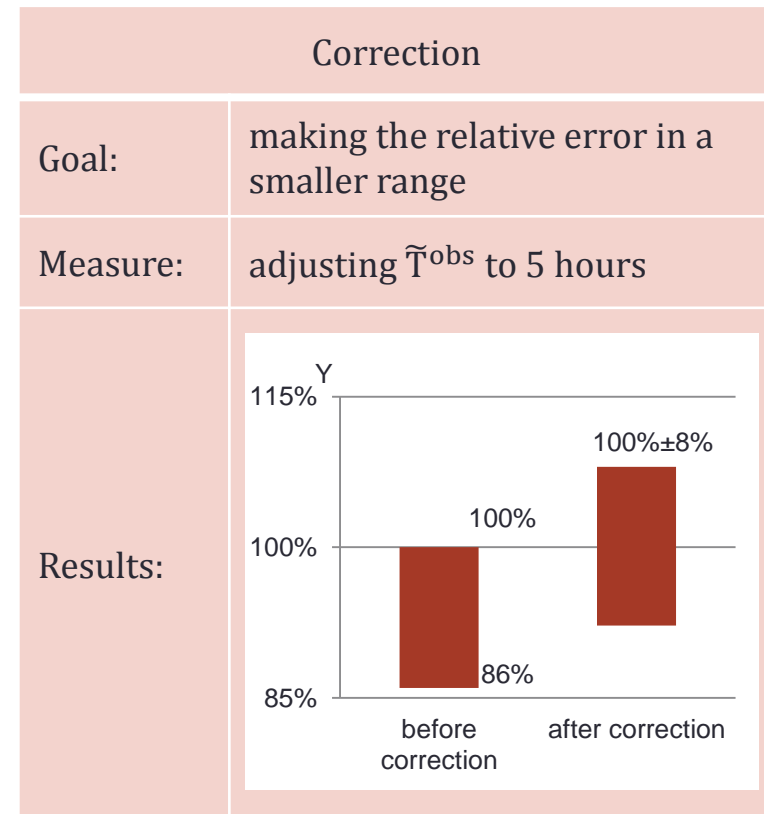
Model

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Conclusions

interval	δ	3	hours
estimated APD	\tilde{T}^{obs}	5.4	hours
survey intensity	X	1.79	
accuracy of APD	Y	above 86%	
real APD	\bar{T}^{real}	[4.64, 5.4]	hours

APD: average parking duration

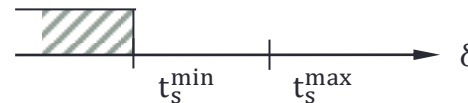


Model

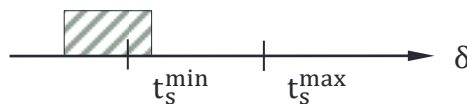
Note that the conclusions above only hold when $\delta \in [t_s^{\min}, t_s^{\max}]$. Fortunately, it is possible to verify this condition using the same survey data:



- When $X=1$, then $\delta \geq t_s^{\max}$ and clearly the accuracy is low.



- When all the observed cars are observed at least twice, then $\delta \leq t_s^{\min}$ and the survey intensity is simply higher than needed, survey cost could be reduced by extending the observation interval.



- When the percentage of cars being observed only once (i.e., $\frac{p_1}{p_{\text{obs}}}$) is very low, then $\delta \approx t_s^{\min}$ and it's possible to reduce the survey intensity without losing much accuracy.

Assumptions

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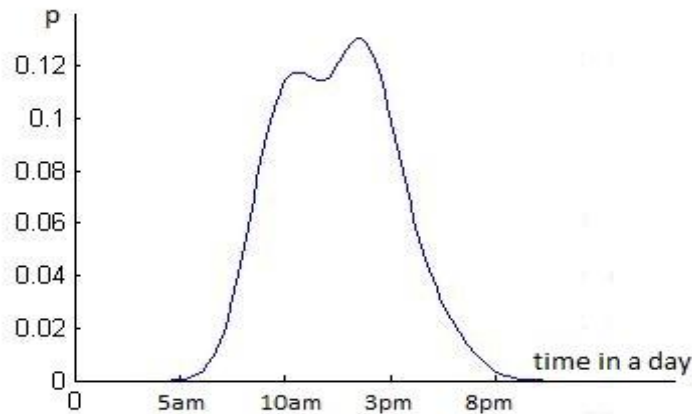
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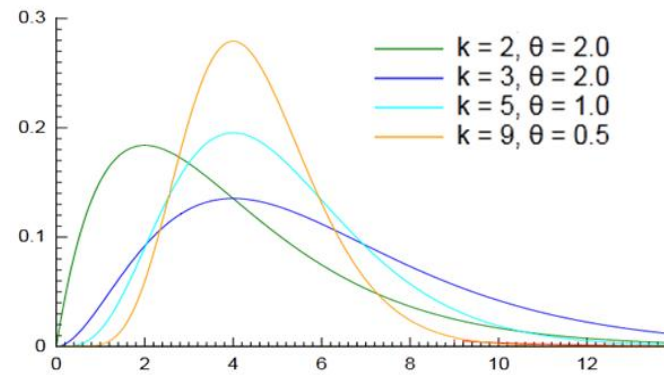
Arrival time

500 vehicles arrive the parking area during a day following a continuous double peak distribution.



Parking duration

Gamma distribution is denoted by $G(k, \theta)$, the probability density function (PDF) is $f(x; k, \theta) = \frac{1}{\theta^k \Gamma(k)} x^{k-1} e^{-\frac{x}{\theta}}$.



Findings from Simulations

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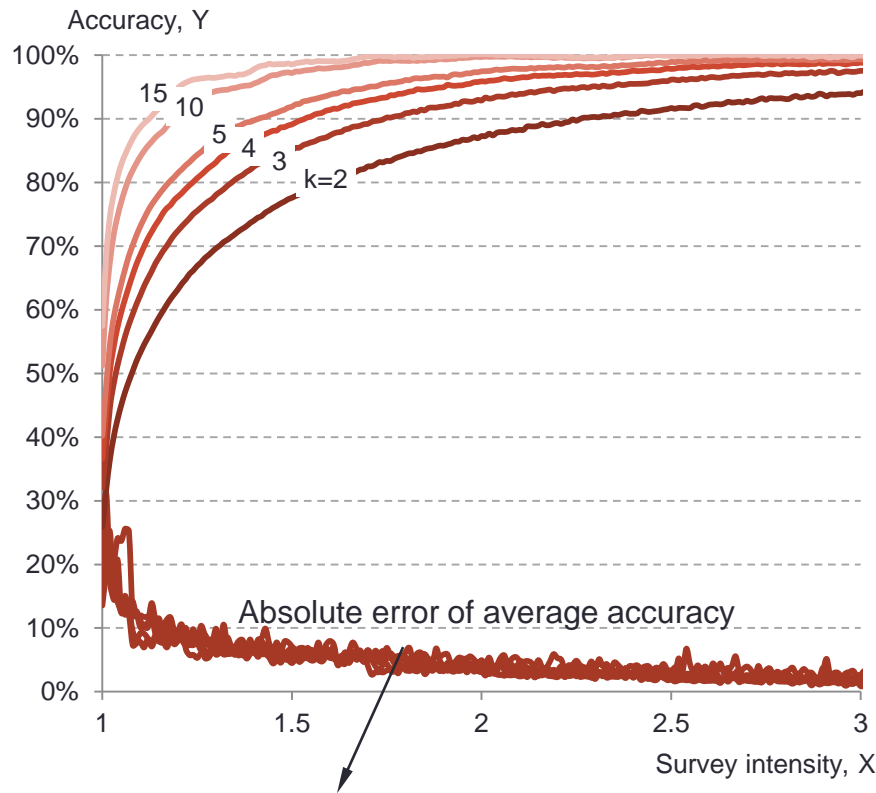
Introduction

- For each value of k among $\{2, 3, 4, 5, 10, 15\}$, 3500 simulations have been ran with a changing value of θ .

Model

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Conclusions



Caused by natural variations

- The real average duration is typically overestimated.
- For a given X , the accuracy is very much influenced by k . (the “shape parameter” of gamma distribution)
- For a given X , a higher accuracy corresponds to a larger k .
- The absolute error of average accuracy is up to 30% in the simulation, but it becomes quite small (below 8%) for $X > 1.5$. For instance, accuracy is $90\% \pm 8\%$.

Conclusions

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Introduction**Model****Simulation****Conclusions**

- A method is supplied to estimate the accuracy
 - The balance of survey input (intensity & cost) and accuracy is illustrated
 - A method to obtain on average a higher accuracy is used in the numerical example
-
1. We have found that the most influential factor to the accuracy is the shape parameter of the parking duration distribution. Former survey experiences or results can be used to support fitting the distribution and estimating this value.
 2. The coordination between survey costs and accuracy could be done by choosing a proper value of survey intensity. Higher survey intensity means a more expensive survey while it also gives better accuracy. Based on the model, we could find a proper value of survey intensity to guarantee that both are acceptable, or the minimum possible cost for a desired level of accuracy.
 3. Through our study, it is proved that when survey intensity is below 1.5, the survey could be quite misleading, not only because a comparatively low accuracy, but also because the data recorded have with large natural variations.

Definitions

δ observation interval

$$a = \frac{t_s^{\min}}{\delta}$$

$$b = \frac{t_s^{\max}}{\delta}$$

$$M = \frac{C}{\delta}$$

$$\beta = \frac{t_s^{\max}}{t_s^{\min}} = \frac{b}{a}$$

p_i Probability of a vehicle been observed i times

$$p^{obs} = \sum_{i=1}^{[b]} p_i$$

$$= \sum_{m=1}^M \left\{ \begin{array}{l} \int_{(m-1)\delta}^{m\delta - t_s^{\min}} f(t_a) \left[\int_{m\delta - t_a}^{t_s^{\max}} f(t_s) dt_s \right] dt_a \\ + \\ \int_{m\delta - t_s^{\min}}^{m\delta} f(t_a) \left[\int_{t_s^{\min}}^{t_s^{\max}} f(t_s) dt_s \right] dt_a \end{array} \right\}$$