

## Preferred citation style

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# Similarities in air transport connection choice

Nadine Schuessler

IVT  
ETH  
Zurich

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Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich

# Problem and objectives

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## Two main objectives

- Modelling air transport connection choice
- Investigate similarity measures for public transport connection choice

# Accounting for the IIA property of the MNL

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In general, there are three different ways:

- Probit models and Mixed Multinomial Logit models  
(e.g. Yai et al. 1997, Ben-Akiva and Bolduc 1996, Walker 2002, Guo and Bhat 2005, Hess et al. 2005, Frejinger and Bierlaire 2007)
- Nested Approaches  
(Voshva and Bekhor 1998, Wen and Koppelman 2001, Bierlaire 2002)
- Similarity measures

## Similarity measures

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Based on the Implicit Availability and Perception (IAP) model by Cascatta et al. (1996)

The utility of an alternative is extended by a term  $q_{Cin}$  representing its degree of membership in the individual choice set  $C_n$ :

$$U_{in} = V'_{in} + q_{Cin} + \varepsilon_{in}$$

The similarity of an alternative with other alternatives

- decreases its probability to be perceived as separate alternative
- decreases its probability to be included in the individual choice set

=> Thus decreases its probability to be chosen

# Existing formulations for similarity measures

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## **Private transport route choice**

- C-Logit Cascetta et al. (1996)
- Path Size Logit Bierlaire and Ben-Akiva (1999),  
Ramming (2002)

## **Multimodal route choice**

- Path Size Logit Hoogendoorn-Lanser and Bovy (2007)

## **Public transport Connection Choice**

- Autonomy of a connection Friedrich et al. (2000)

## **Spatial Correlations**

- Competing Destinations Fotheringham (1988)
- Spatial Dependency Parameter Mohammadian et al. (2005)
- Field Effect Variable Dugundji and Walker (2005)

## Autonomy of a connection

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Choice probability depending on the independence of a connection

$$P_{in} = \frac{e^{V_{in}} \cdot IND(i)}{\sum_{j \in C} e^{V_{in}} \cdot IND(j)} = \frac{e^{V_{in} + \ln(IND(i))}}{\sum_{j \in C} e^{V_{in} + \ln(IND(j))}}$$

Independence of a connection as reciprocal sum of similarities:

$$IND(c) = \frac{1}{\sum_{c' \in C} f_c(c')} = \frac{1}{1 + \sum_{c' \in C; c' \neq c} f_c(c')}$$

Similarity takes into account similarities in departure and arrival times  $x_c(c')$ , perceived journey time  $y_c(c')$  and fare  $z_c(c')$

$$f_c(c') = \left(1 - \frac{x_c(c')}{s_x}\right)^+ \cdot \left(1 - \gamma \cdot \min\left(1, \frac{|y_c(c')|}{s_y} + \frac{|z_c(c')|}{s_z}\right)\right)$$

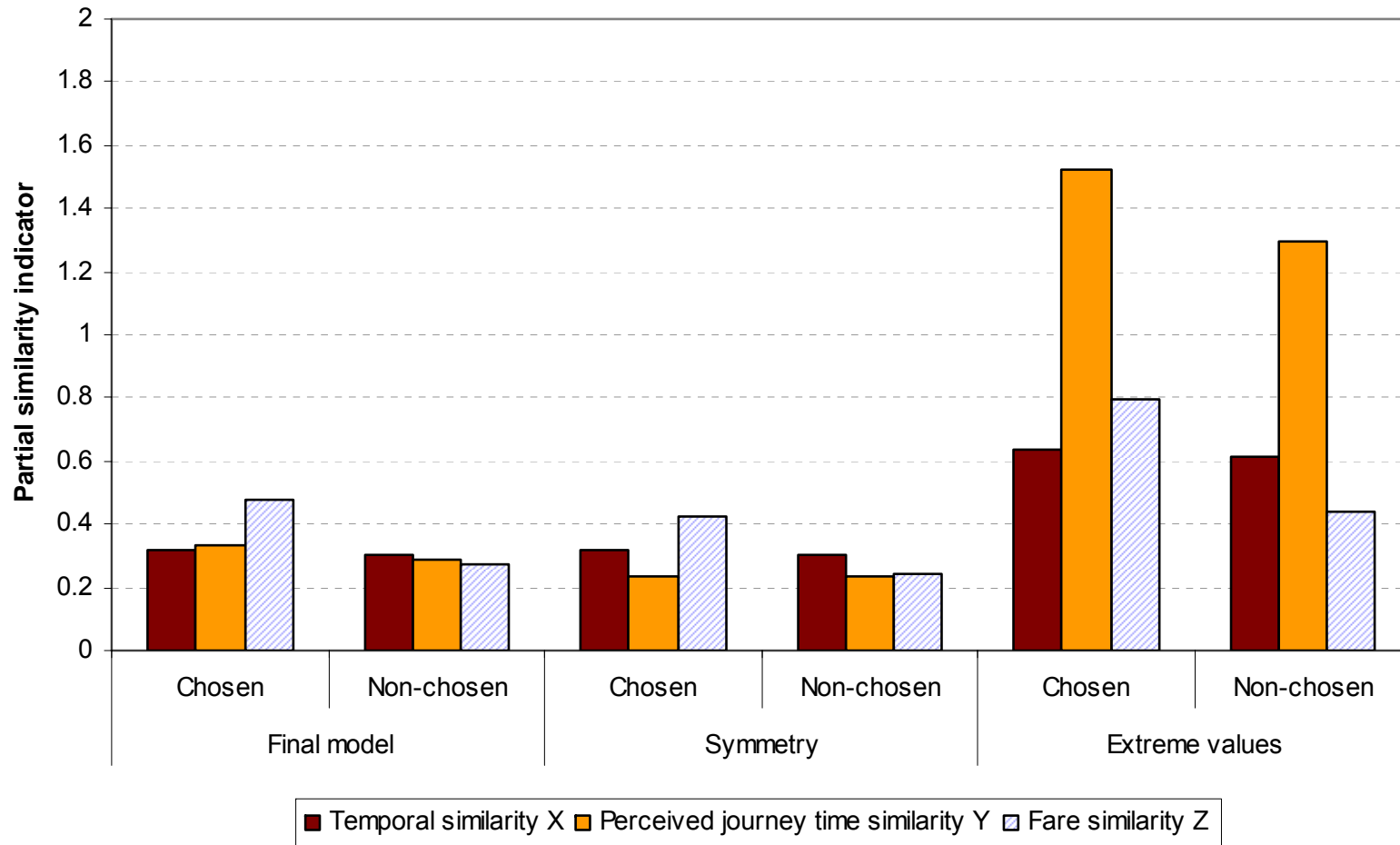
$s_x$ ,  $s_y$  and  $s_z$  set the range of influence of  $x_c(c')$ ,  $y_c(c')$  and  $z_c(c')$   
 $\gamma$  weights the right part of the formula

## Parameter settings for the independence measure

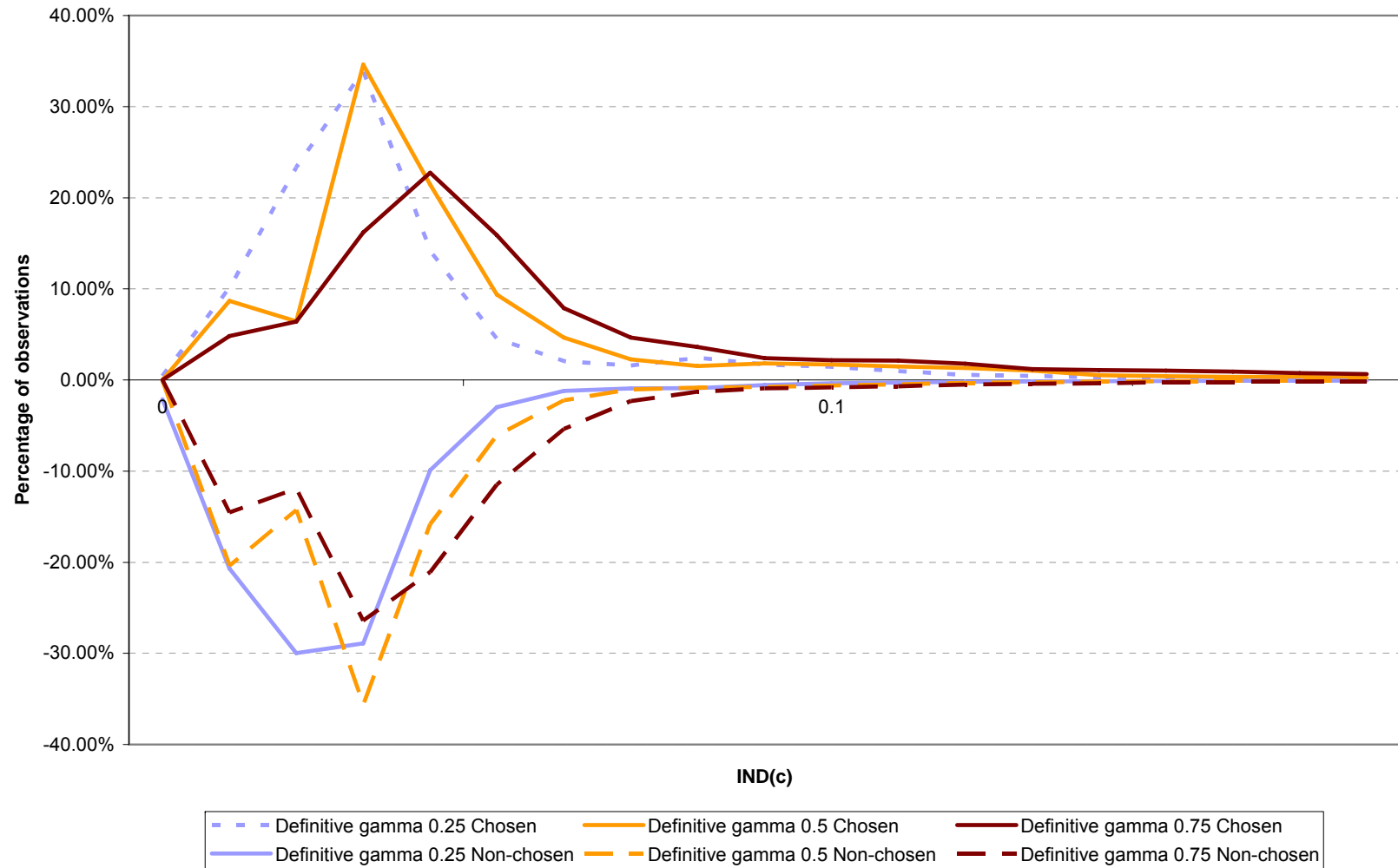
Parameter	S <sub>x</sub> , S <sub>y</sub> , S <sub>z</sub> tests		γ tests		Final model
	Symmetric setting	Extreme values	γ = 0.25	γ = 0.75	γ = 0.5
S <sub>x</sub>	720	360	720	720	720
S <sub>y</sub> <sup>+</sup>	780	180	780	780	780
S <sub>y</sub> <sup>-</sup>	780	120	540	540	540
S <sub>z</sub> <sup>+</sup>	1.7	0.9	1.5	1.5	1.5
S <sub>z</sub> <sup>-</sup>	1.7	0.9	1.5	1.5	1.5
γ	0.5	0.5	0.25	0.75	0.5



# Effect of varying $s_x$ , $s_y$ and $s_z$



# Effect of varying $\gamma$



## Available Data – Data Sources

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Marketing Data Information Transfer (MIDT) Dataset – booked tickets in November 2006

~ 200,000 bookings

Expedia Dataset observed prices on 70 origin-destination pairs between September and November 2006

~ 12,000,000 observations

Official Airline Guide (OAG) November – information on code share, type of aircraft, detailed waiting times can be extracted

Matching these datasets on several criteria leads to almost 19,000 observed choices

# Variables for connection choice model

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Alternatives are return flights with several characteristics:

- Carrier
- Code share
- Aircraft type (mainline jet, regional aircraft, propeller aircraft)
  
- Total travel time
- Number of transfers
  
- Fare without tax
  
- Combination of time of day of out- and inbound flight and return period
  
- Independence of the connection

## Modelling results

Model	MNL		MNL with IND(c)	
	Parameter	Robust t-test	Parameter	Robust t-test
<i>Carrier const.</i>		not presented		
Code share	-0.7465	-12.81	-0.7622	-12.29
Travel time	-0.0006	-5.86	0.0002	1.25
N.o. Transfers	-6.2404	-40.42	-6.6154	-37.75
Fare	-0.0057	-73.71	-0.0063	-66.68
Similarity	0.0000	0.00	-1.0362	-12.97
<i>Time of day</i>		not presented		
<i>Aircraft type</i>				
Regional	-0.2170	-8.55	-0.2087	-8.65
Propeller	-1.6427	-19.04	-1.6711	-18.40

## Modelling results for different parameter settings

Model	Parameter for IND(c)	Average for IND(c)	Final Log-Likelihood	Adjusted r-square	Difference r-square*
MNL	--	--	-48816	0.2948	--
$s_x=720, \gamma=0.25$	-1.1966	0.0386	-48712	0.2963	0.5%
$s_x=720, \gamma=0.5$	-1.0362	0.0473	-48684	0.2967	0.6%
$s_x=720, \gamma=0.75$	-0.7210	0.0621	-48752	0.2957	0.3%
$s_x=120, \gamma=0.5$	-0.1835	0.1650	-48798	0.2950	0.1%
$s_x=240, \gamma=0.5$	-0.6776	0.0984	-48622	0.2976	0.9%
$s_x=360, \gamma=0.5$	-0.7666	0.0734	-48640	0.2973	0.8%

\* Compared to MNL

# Conclusion

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Estimated parameters for the independence measure are highly significant and the model performance increases

Traveller's perception of similarity between air transport connections is multi-dimensional

The inclusion of multiple dimensions can lead to more insight in preferences without penalising other alternatives too strong

Setting of the parameters defining the range of influence has to be determined for specific data set

The sign of the parameter indicates that tra perceive similar alternatives as positive

# Outlook

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For the air connection choice data set:

- Testing the influence of the individual similarity components
- Comparison with other model structures, such as (cross)-nested model structures
- Closer look to the formation of the choice

Investigation of similarity measures based on a GPS data set:

- Investigation of other choice situations
- Testing different similarity measures
- Comparison to complex model structures



## The GPS data set

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- On-person GPS data for travellers living in Zurich, Winterthur and Geneva
- Complete multi-modal urban and inter-urban trip chains
- GPS records of 4878 persons comprising on average 6.64 days per persons
- No additional information about socio-demographics, trip details etc.

# Modelling the GPS data

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Motorised private transport route choice

Public transport connection choice

Combined route and mode choice

Destination choice

Combined route, mode and destination choice

# Post-processing the GPS records

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Adaptation of the method by Tsui and Shalaby (2006) for

- Trip and activity detection
- Identification of single-mode segments
- Mode detection

Map-matching with method by Marchal, Hackney and Axhausen (2006)

Activity type and trip purpose classification

Validation with Swiss Microcensus 2005

Choice set generation

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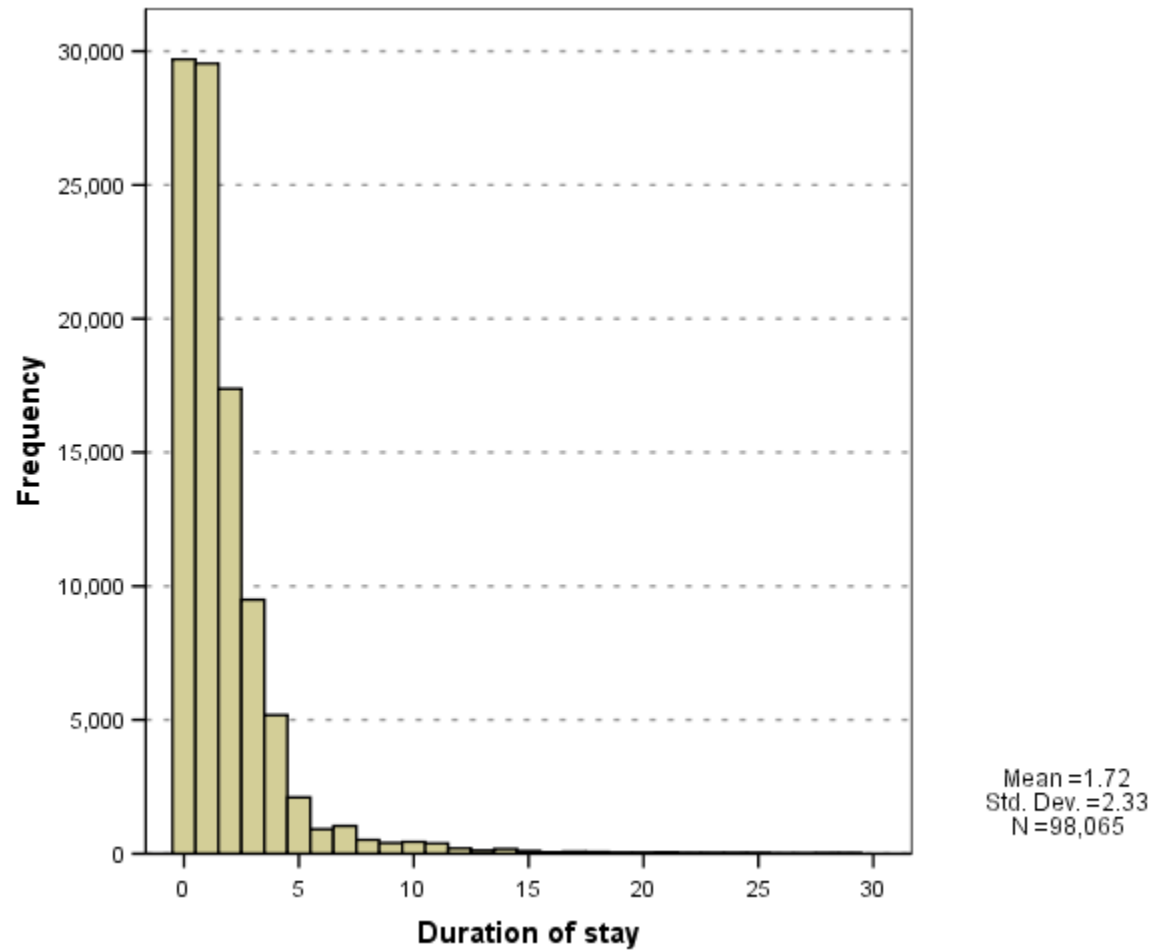
# Appendices

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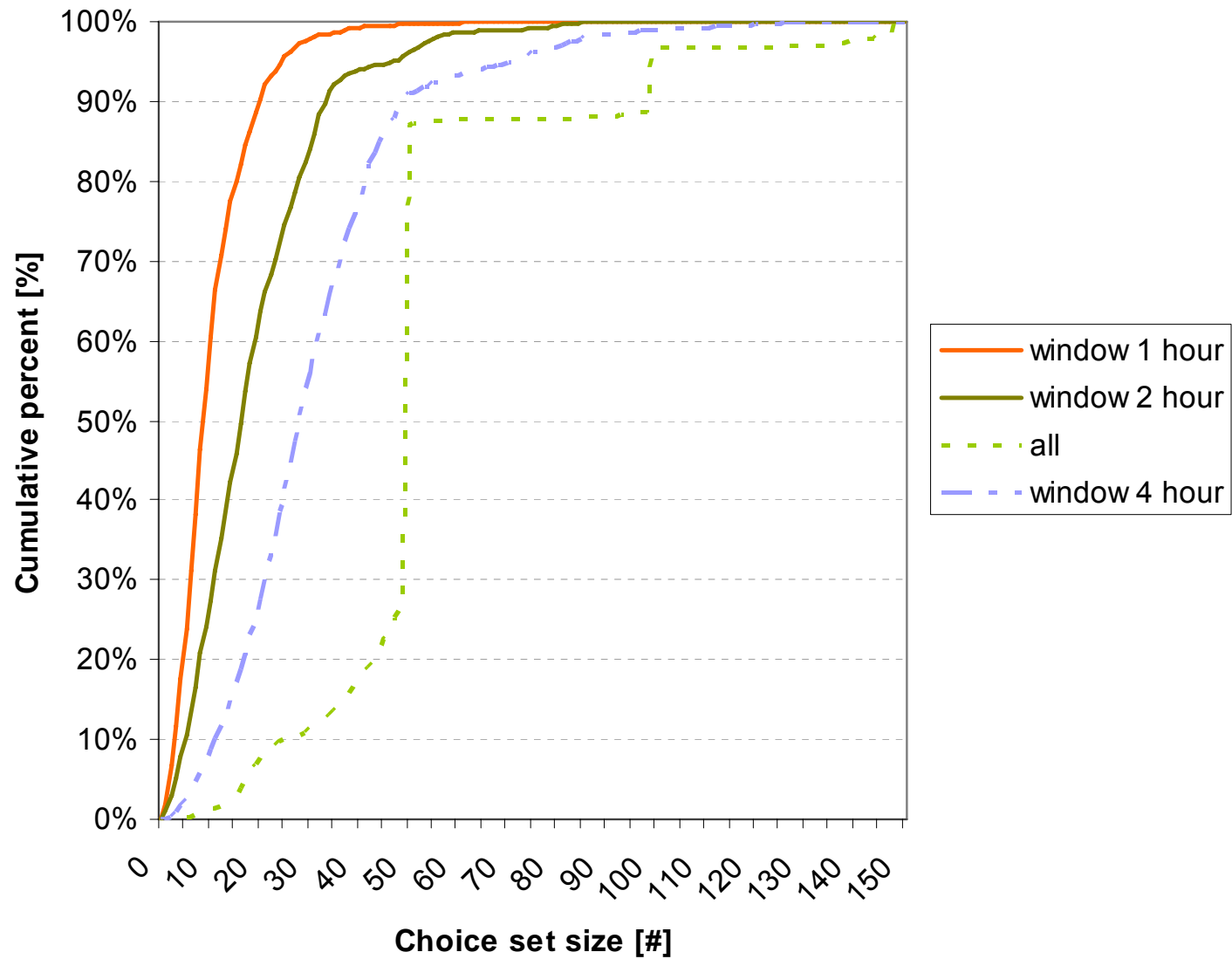
# Available Data – Duration of Stay

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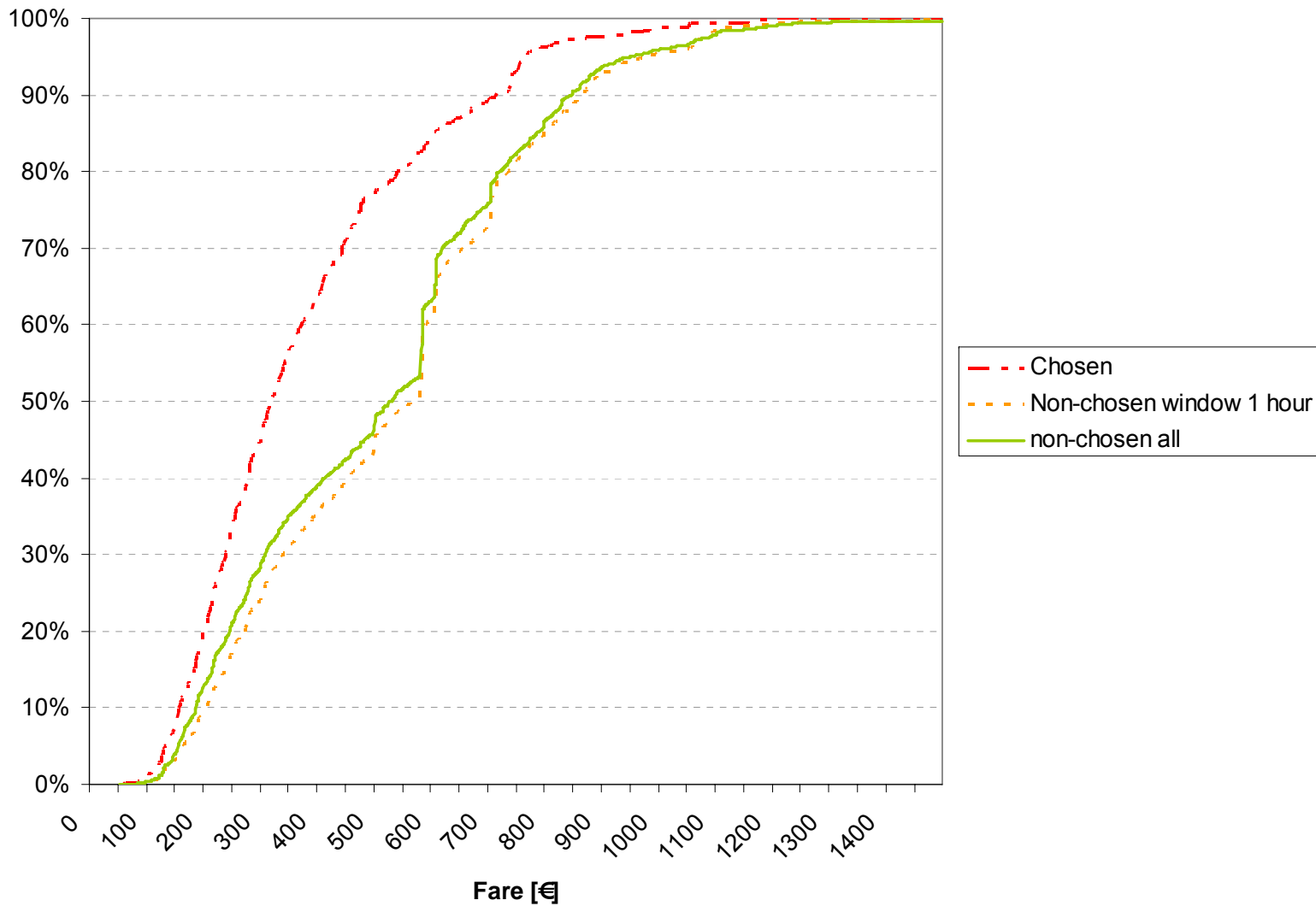


# Available Data – Choice Set Size

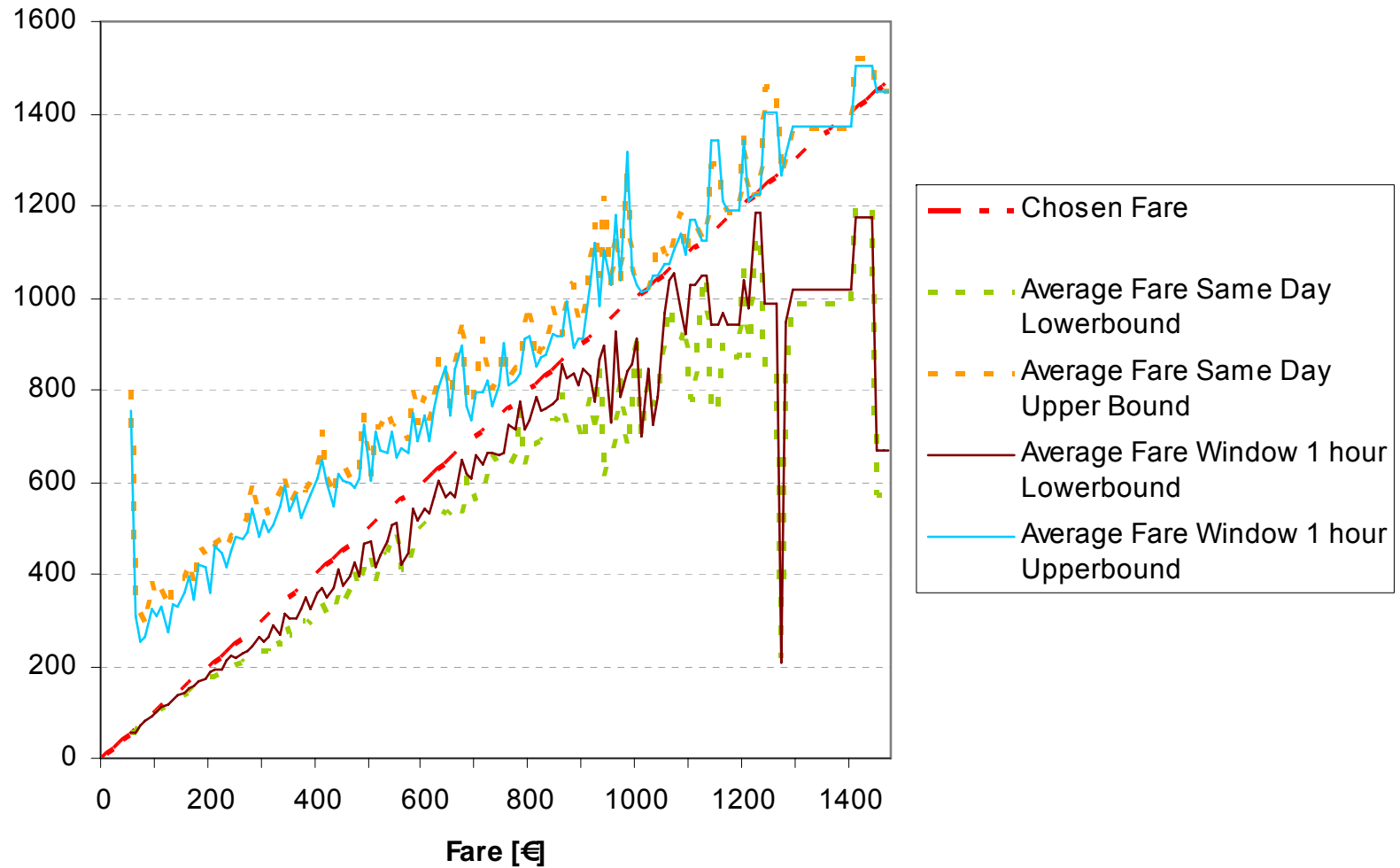
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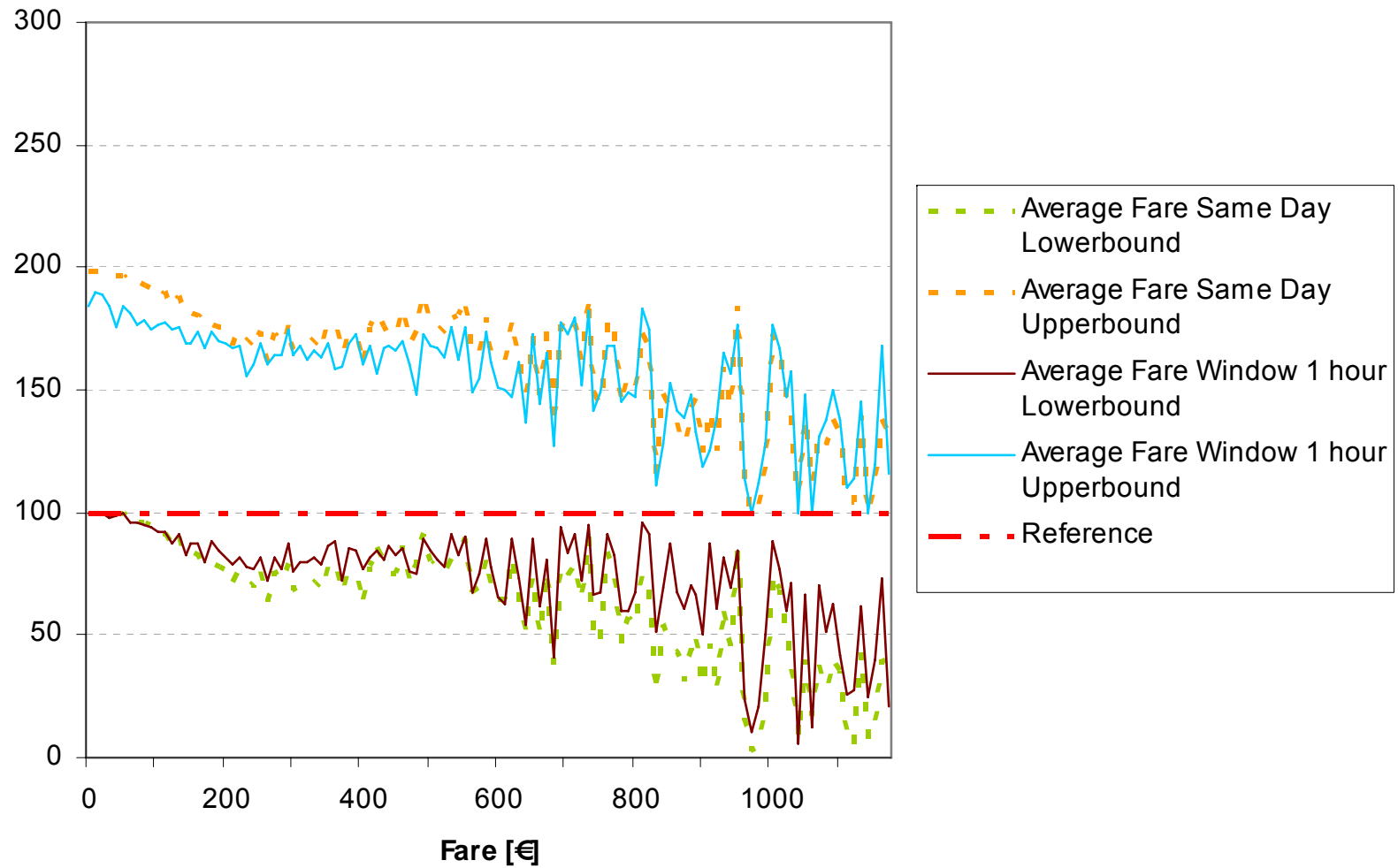
# Available Data – Comparison Choice Set Fare



# Available Data – Comparison Choice Set Fare



# Available data – Comparison Choice Set Fare



## Modelling results (2)

	MNL		MNL with IND(c)	
	Parameter	Robust t-test	Parameter	Robust t-test
<i>Same day return</i>				
Afternoon Out	-1.6057	-63.39	-1.5867	-61.10
Evening Out	-2.4960	-18.59	-2.087	-14.97
<i>Overnight stay</i>				
Afternoon Out	-0.7807	-24.92	-1.0462	-26.70
Evening Out	-0.8573	-26.15	-2.0964	-14.97
<i>Fortnight stay</i>				
Afternoon Out	-0.2829	-2.75	-0.5711	-4.85
Evening Out		not significant		
<i>Same day return</i>				
Afternoon In		not significant		
Evening In	0.1907	2.04	0.1958	1.88
<i>Overnight stay</i>				
Afternoon In	1.1967	12.90	1.2171	12.56
Evening In	1.5915	17.28	1.6055	16.63
<i>Fortnight stay In</i>		not significant		