

## Preferred citation style for this presentation

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# An Integrated and Adaptive Ant Colony and Genetic Algorithm for Transport Network Design

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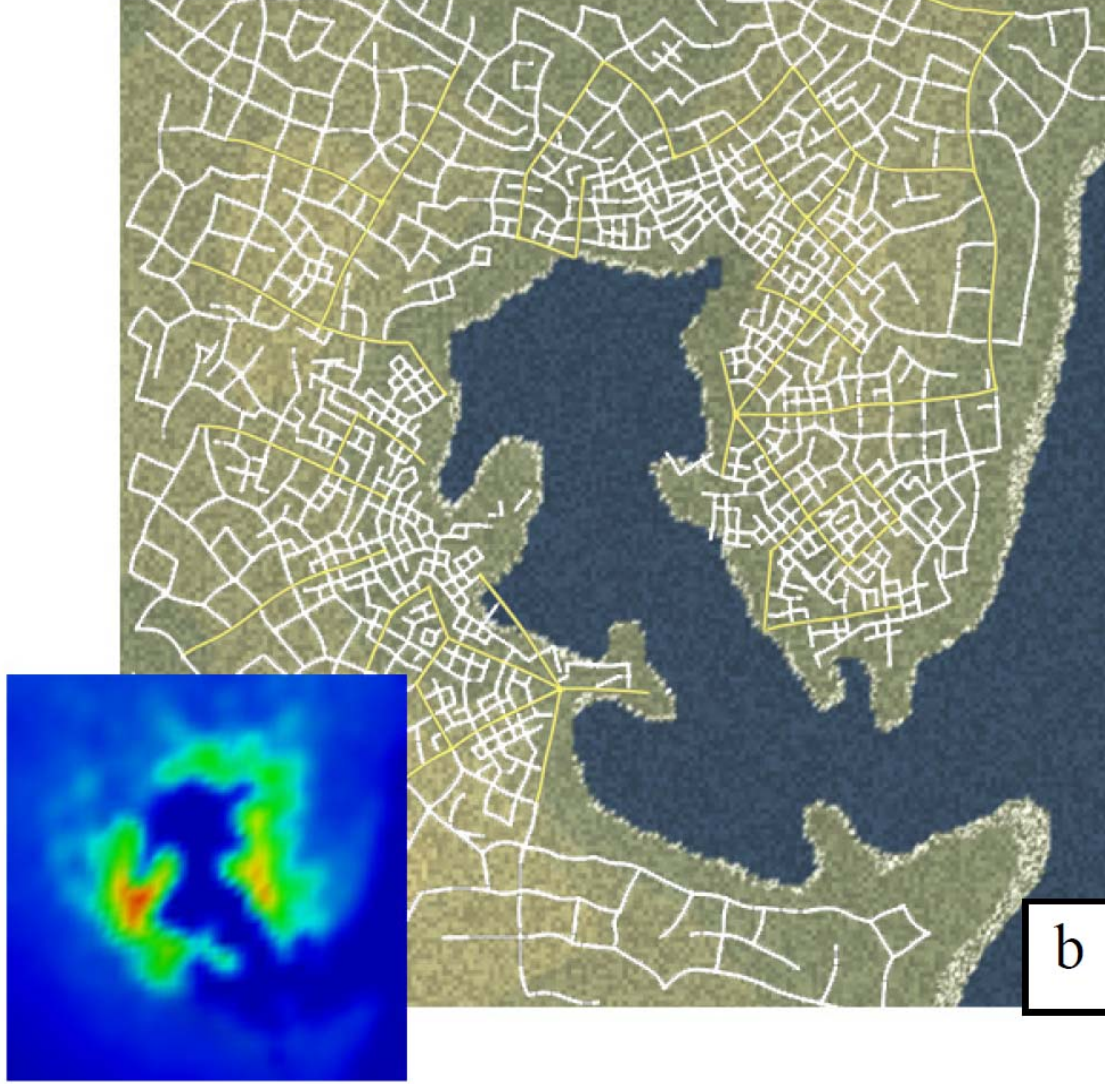
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# Background

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# Concern – network design

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## 1. Order

- Volume delay function
- Wardrop Equilibrium

## 2. Order

- Determination of a subset of candidate links and nodes
- Determination of network element types

# Preliminaries – objective functions

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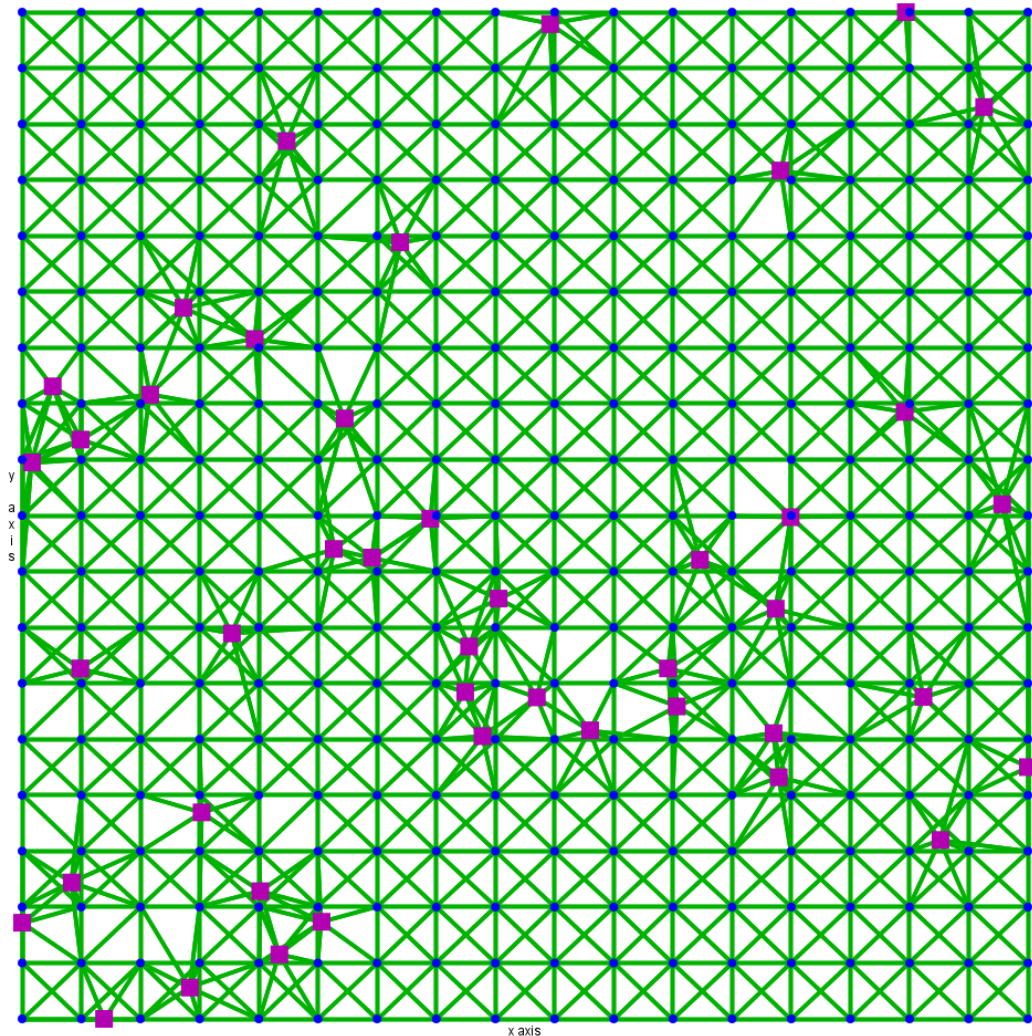
Costs:

$$f = (\textit{Generalized Costs}, \textit{External Costs}, \dots, \textit{Infrastructure Budget})$$

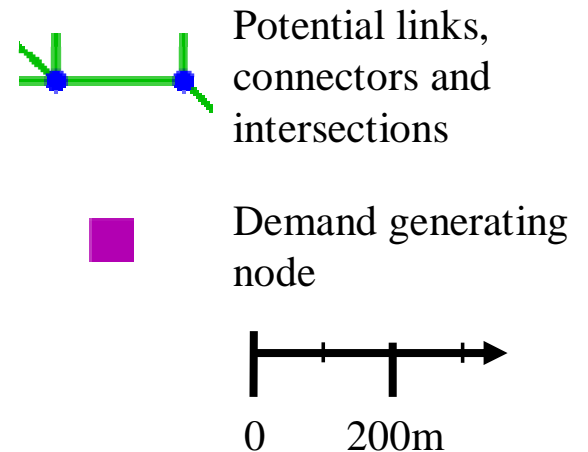
Accessibility:

$$f = \sum_{o=1}^O I_o \cdot \ln \left( \sum_{d=1}^D A_d \cdot \exp(-\beta \cdot t_{od}) \right) - \textit{Infrastructure Budget}$$

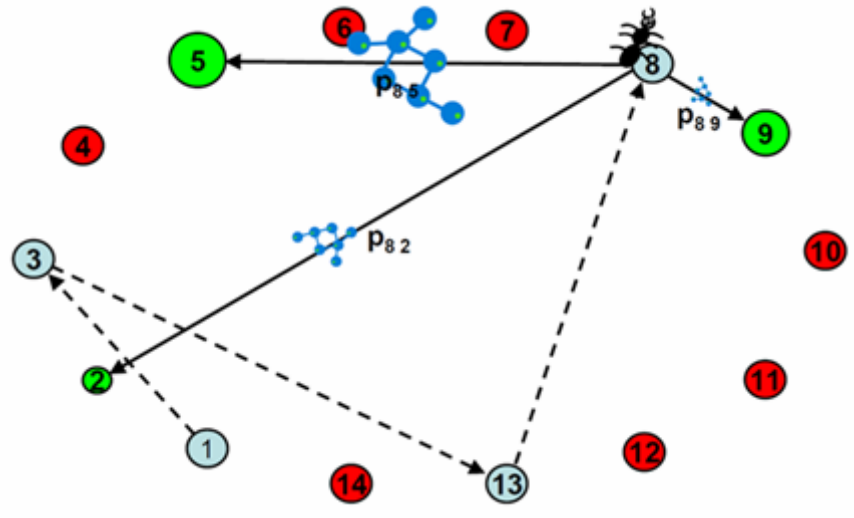
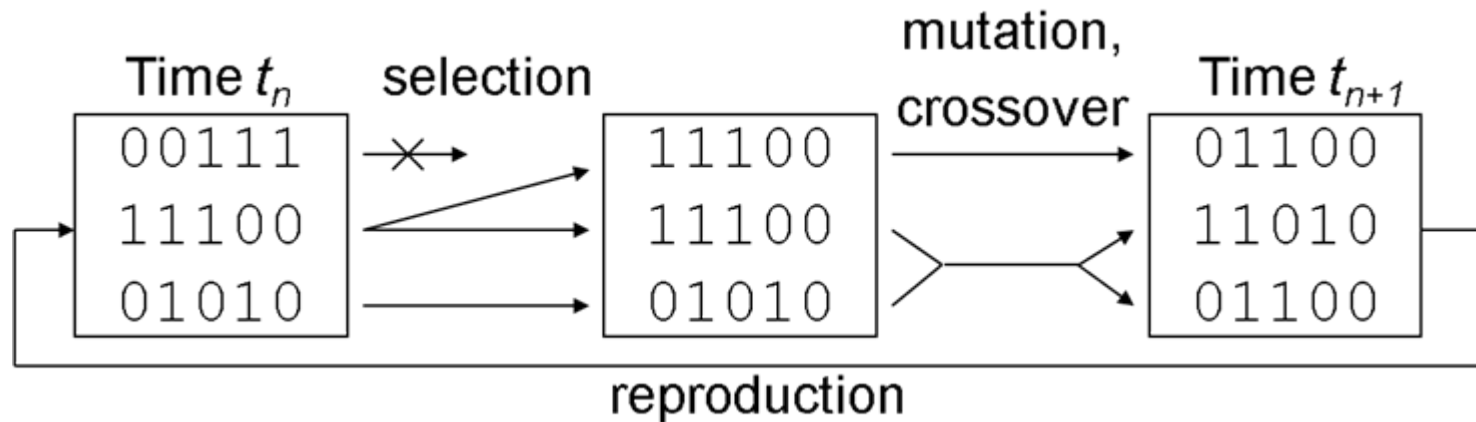
# Preliminaries – search space



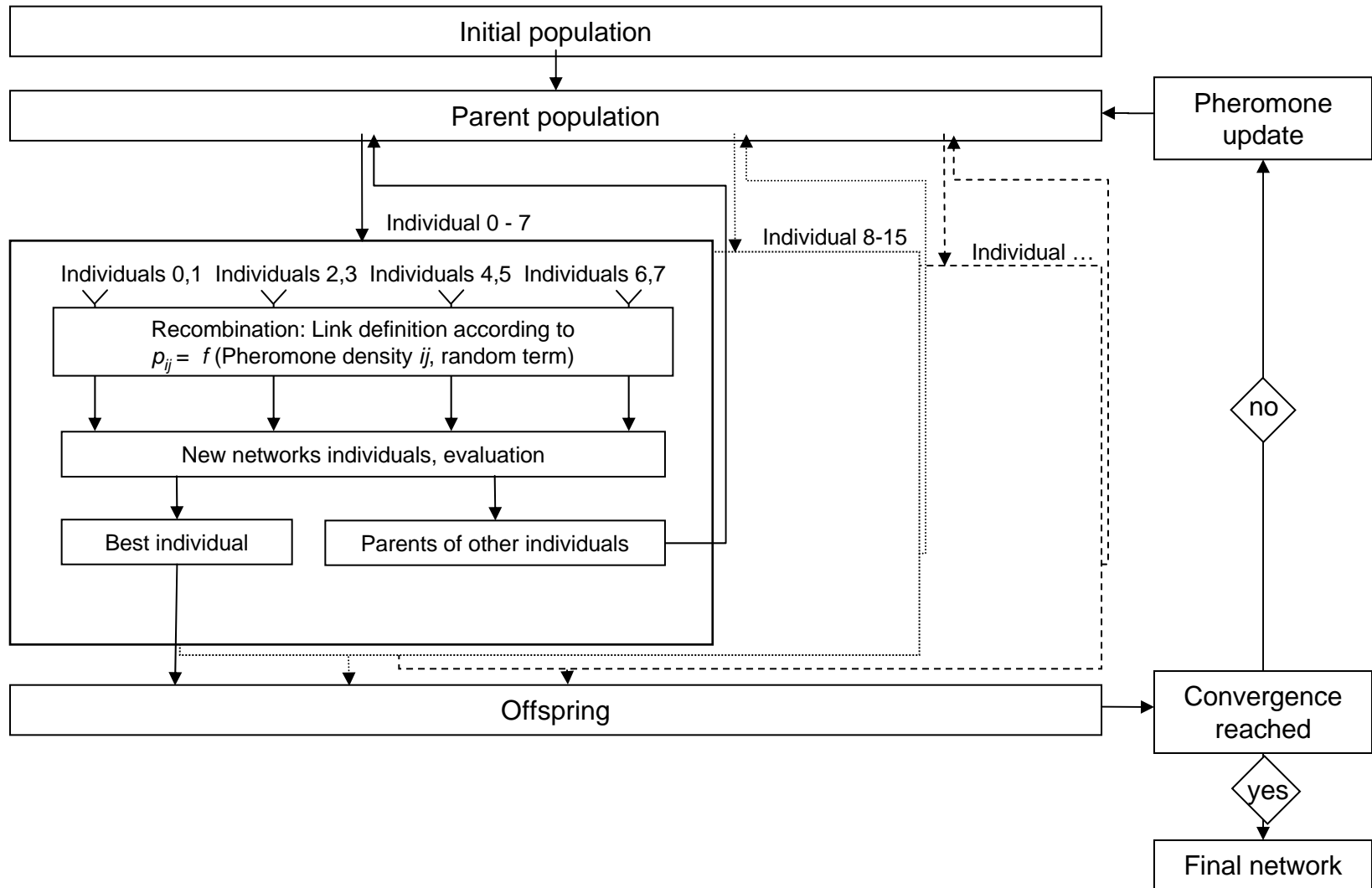
Potential solutions:  
100 nodes  $\rightarrow 10^{103}$   
400 nodes  $\rightarrow 10^{446}$   
625 nodes  $\rightarrow 10^{708}$



# Design – Genetic Algorithm vs. Ant Colony Optimization



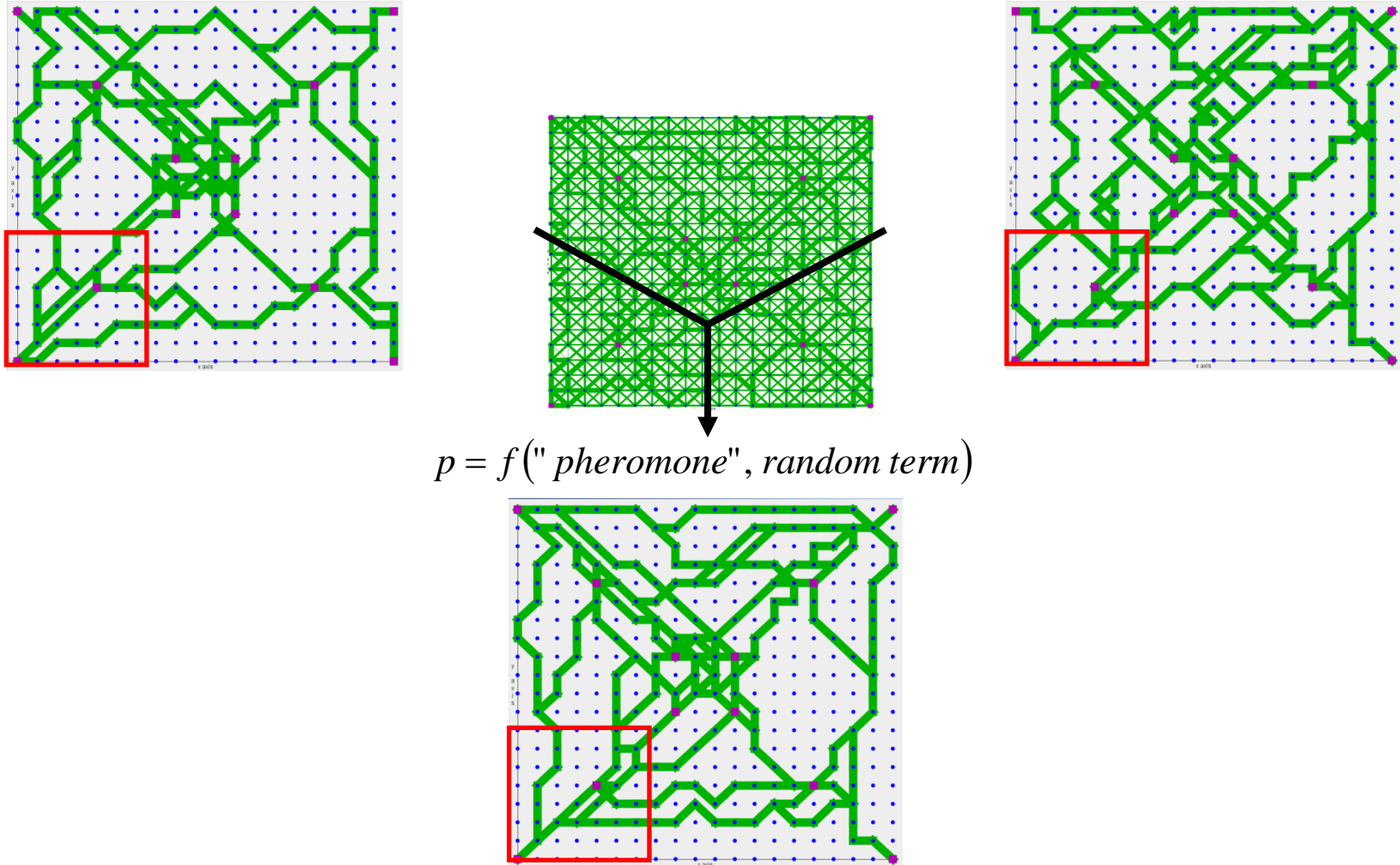
# Design - Integrated Ant Colony Genetic Algorithm





# Design – recombination procedure

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# Design – path picking and pheromones update

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$$p_{ij}^g = \begin{cases} \frac{e^{\alpha\tau_{ij}^g} e^{\beta r}}{\sum_{l_{ij} \in L_{Parents}} e^{\alpha\tau_{ij}^g} e^{\beta r}}, & \text{when } l_{ij} \in L_{Parents} \\ 0, & \text{otherwise} \end{cases}$$

$$\tau_{ij}^g = (1 - \delta) \cdot \tau_{ij}^{g-1} + \max(\Delta \tau_{ij}^g)$$

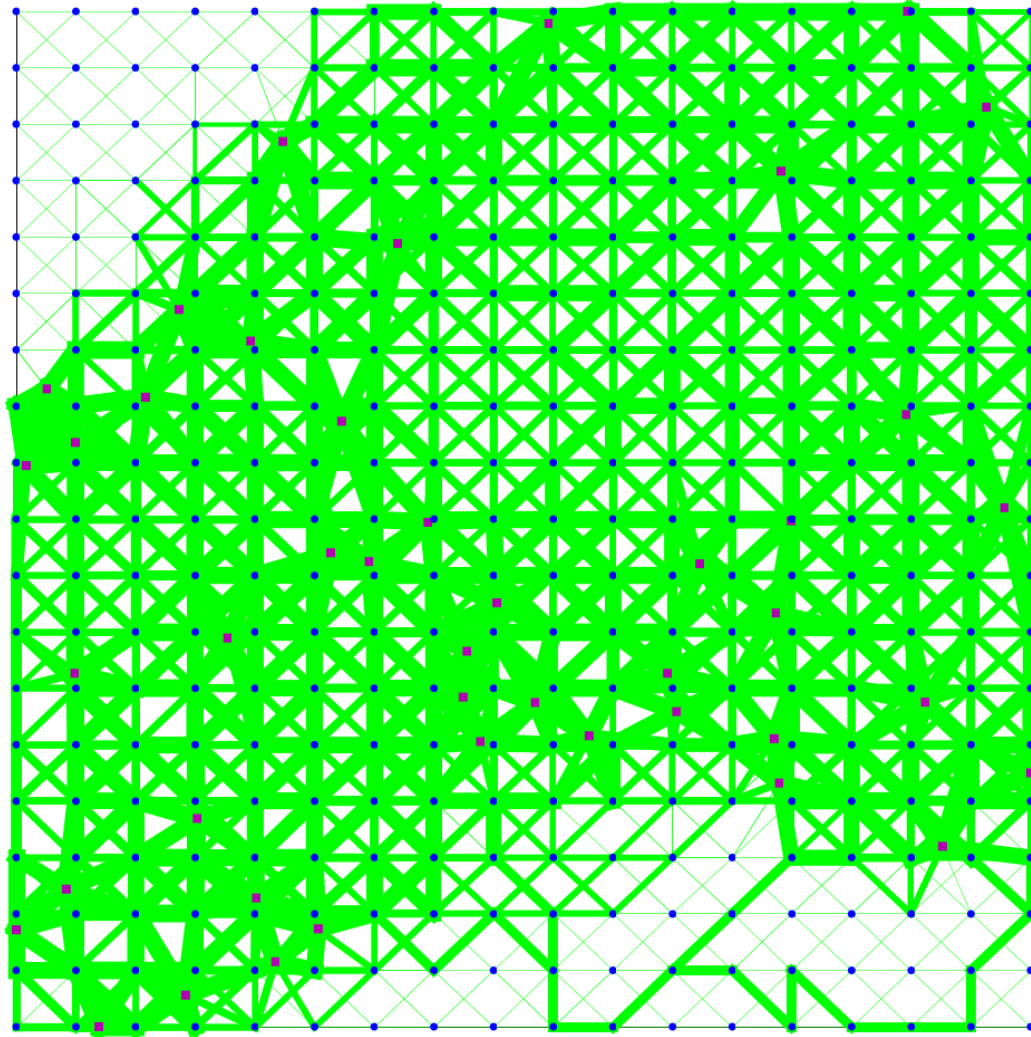
$\tau_{ij}^g$  : Pheromone density in iteration  $g$  on link  $i - j$ .

$\delta$  : Evaporation rate.

$\max(\Delta \tau_{ij}^g)$  : Score of the best individual out of all processed network individual.

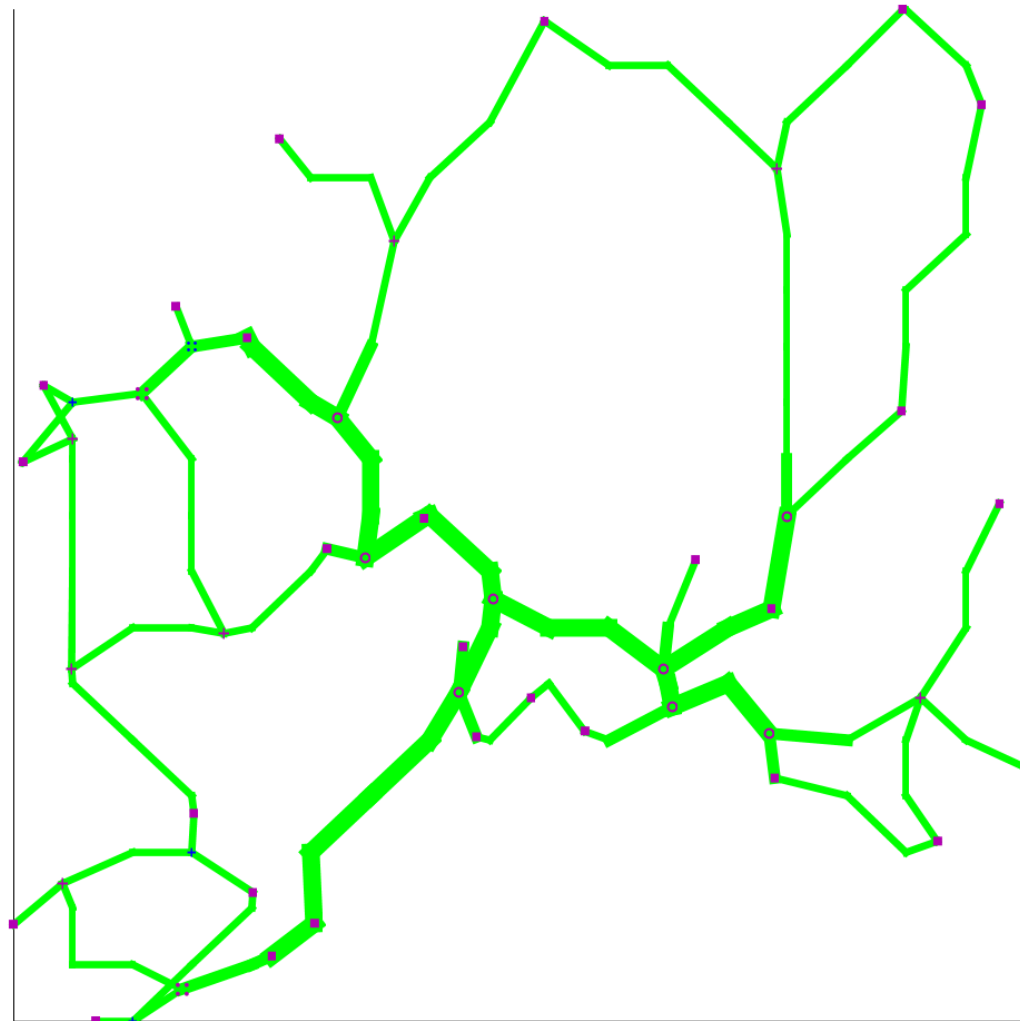
# Results – pheromone development (generation 100)

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# Results – capacities (generation 100)

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# Results – comparison of IACGA and GA (approximation)

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Network size [nodes]	Objective functions evaluated [numbers]			Total calculation time [h]		
	GA	IACGA	Difference	GA	IACGA	Difference
100	200'000	54'000	-73.00%	6	0.75	-88.5%
225	$1.7 \cdot 10^8$	140'000	-99.92%	5'100	2	-99.96%
400	$\sim 1.1 \cdot 10^9$	700'000	-99.94%	33'000	124	-99.62%

Source: Vitins and Axhausen (2010)

## Results – quality (420 candidate links, n = 73)

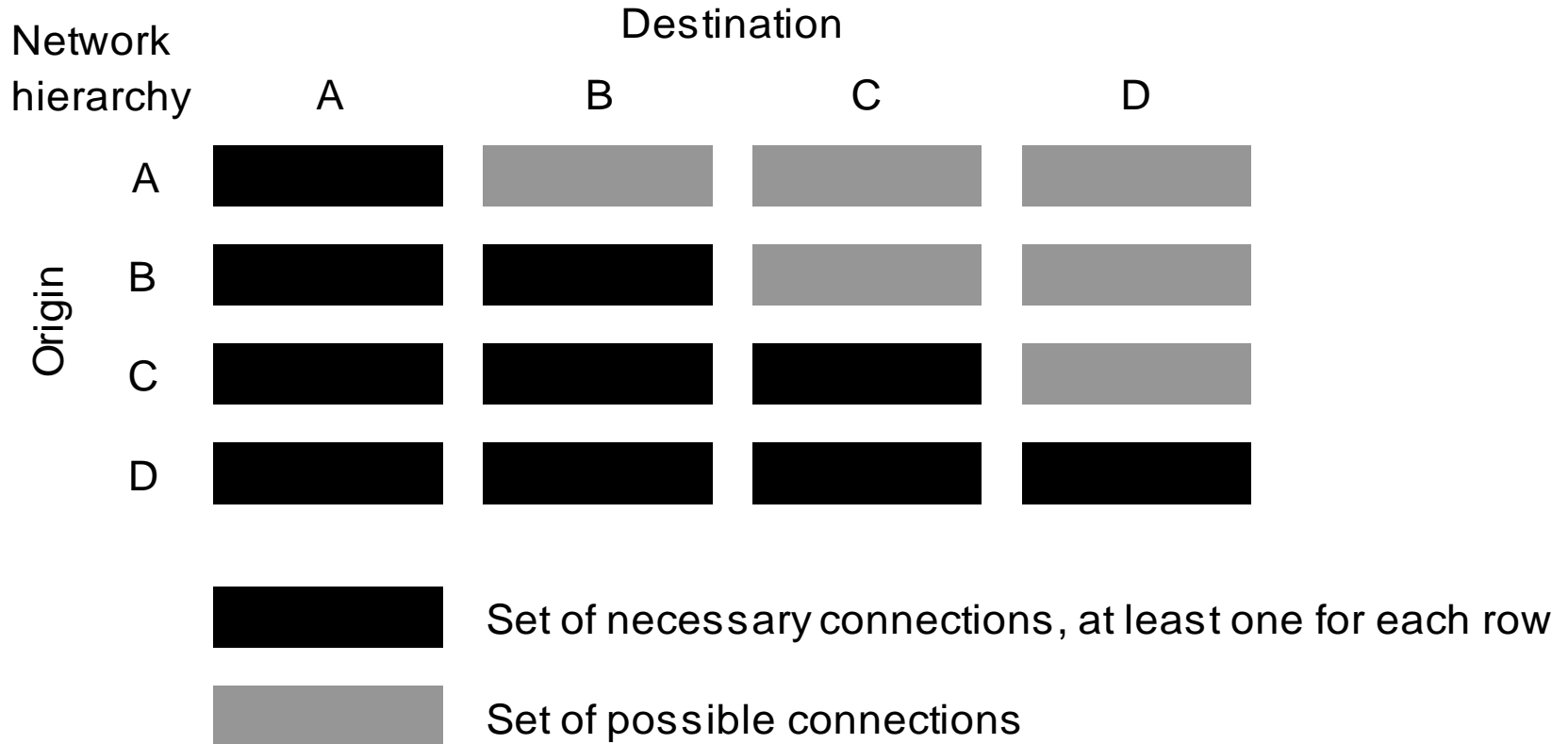
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Best possible score	Share of optimal networks	Standard deviation	Standard error
Without degraded initial population			
-2'432	51%	0.67%	3.37
With degraded initial population			
-2'432	55%	0.79%	3.90

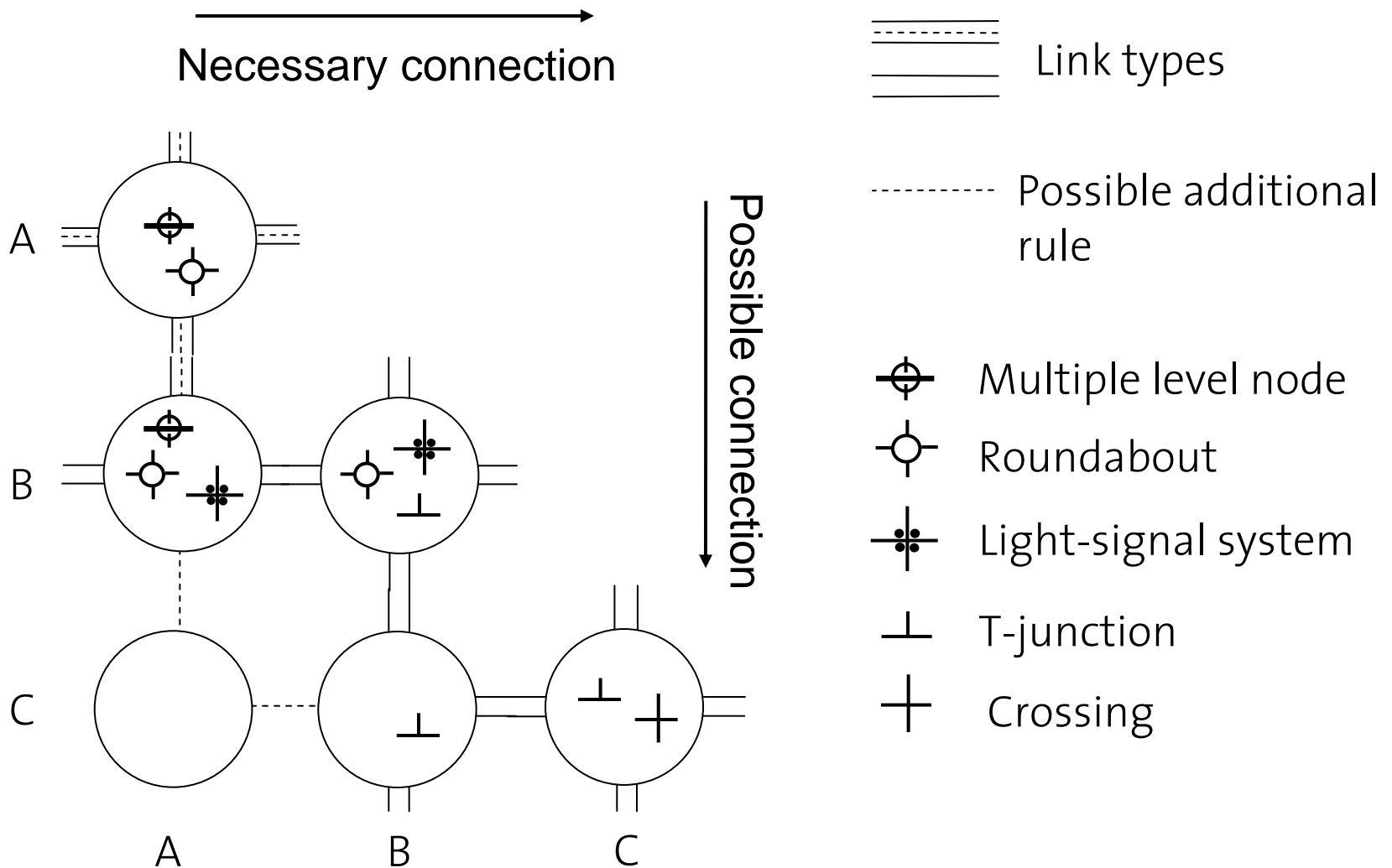
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# Application – abstract shape grammars

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# Application – possible shape grammars



Source: after Marshall (2005)



# Application – implemented shape grammars

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Shape grammar	Initial setting 1			Initial setting 2 (n = 3)	
	Average score	Relative difference	Wilcoxon rank-sum	Average score	Relative difference
A	-143'200	-		-300'192	-
B	-147'132	2.75%	0.0087% (n=20)	-317'145	5.65%
C	-116'550	-		-250'895	-
D	-129'297	10.94%	0.15% (n=10)	-303'507	20.97%

# Outlook

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Faster and more precise...

Implement other network elements and land use parameters

Include land use and variable demand

Visualization

# References

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Marshall, S. (2005) *Streets & Patterns*, Spon Press, London.

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Vitins, B.J. and K.W. Axhausen (2010) Patterns and Grammars for Transport Network Generation, paper presented at the *10th Swiss Transport Research Conference*, Ascona, September 2010.